# Package 'fetwfe'

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Title Fused Extended Two-Way Fixed Effects

Version 1.5.0

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**Depends** R (>= 4.1.0)

Description Calculates the fused extended two-way fixed effects (FETWFE) estimator for unbiased and efficient estimation of difference-in-differences in panel data with staggered treatment adoption. This estimator eliminates bias inherent in conventional two-way fixed effects estimators, while also employing a novel bridge regression regularization approach to improve efficiency and yield valid standard errors. Also implements extended TWFE (etwfe) and bridge-penalized ETWFE (betwfe). Provides S3 classes for streamlined workflow and supports flexible tuning (ridge and rank-condition guarantees), automatic covariate centering/scaling, and detailed overall and cohort-specific effect estimates with valid standard errors. Includes simulation and formatting utilities, extensive diagnostic tools, vignettes, and examples. See Faletto (2025) (<doi:10.48550/arXiv.2312.05985>).

URL https://github.com/gregfaletto/fetwfePackage

BugReports https://github.com/gregfaletto/fetwfePackage/issues

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**Encoding** UTF-8

RoxygenNote 7.3.2

**Imports** expm, glmnet, grpreg, Matrix (>= 1.6-0)

Suggests bacondecomp, knitr, rmarkdown, dplyr, did

VignetteBuilder knitr

NeedsCompilation no

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## **Description**

 $\label{lem:attgtofetwfeDf()} attgtToFetwfeDf() \ reshapes \ and \ renames \ a \ panel \ dataset \ that \ is \ already \ formatted \ for \ did::att_gt() \ (Callaway \ and \ Sant'Anna \ 2021) \ so \ that \ it \ can \ be \ passed \ directly \ to \ fetwfe()oretwfe()from \ the fetwfe' \ package. \ In \ particular, \ it$ 

- creates an *absorbing-state* treatment dummy that equals 1 from the first treated period onward\* and 0 otherwise,
- (optionally) drops units that are already treated in the very first period of the sample (because fetwfe() removes them internally), and
- returns a tidy dataframe whose column names match the arguments that fetwfe()/etwfe() expect.

# Usage

```
attgtToFetwfeDf(
  data,
  yname,
  tname,
  idname,
  gname,
  covars = character(0),
```

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```
drop_first_period_treated = TRUE,
  out_names = list(time = "time_var", unit = "unit_var", treatment = "treatment",
    response = "response")
)
```

#### **Arguments**

data A data.frame in **long** format containing at least the four columns used by

did::att\_gt(): outcome yname, time tname, unit id idname, and the first-treatment

period gname (which is 0 for the never-treated group).

yname Character scalar. Name of the outcome column.

tname Character scalar. Name of the time variable (numeric or integer). This becomes

time in the returned dataframe.

idname Character scalar. Name of the unit identifier. Converted to character and re-

turned as unit\_var.

gname Character scalar. Name of the *group* variable holding the first period of treat-

ment. Values must be 0 for never-treated, or a positive integer representing the

first treated period.

covars Character vector of additional covariate column names to carry through (default

character(0)). These columns are left untouched and appear after the required

columns in the returned dataframe.

drop\_first\_period\_treated

Logical. If TRUE (default), units that are already treated in the first sample period are removed *before* creating the treatment dummy. fetwfe() would do this internally, but deapping them have keeps the returned detefance cleaner.

internally, but dropping them here keeps the returned dataframe cleaner.

out\_names A named list giving the column names to use in the resulting dataframe. De-

faults are list(time = "time", unit = "unit", treatment = "treatment", response = "y"). Override if you prefer different names (for instance, to keep

the original yname). The vector *must* contain exactly these four names.

## Value

A data.frame with columns time, unit, treatment, y, and any covariates requested in covars, ready to be fed to fetwfe()/etwfe(). All required columns are of the correct type: time is integer, unit is character, treatment is integer 0/1, and y is numeric.

#### References

Callaway, Brantly and Pedro H.C. Sant'Anna. "Difference-in- Differences with Multiple Time Periods." Journal of Econometrics, Vol. 225, No. 2, pp. 200-230, 2021. doi:10.1016/j.jeconom.2020.12.001, https://arxiv.org/abs/1803.09015.

```
head(mpdta)
tidy_df <- attgtToFetwfeDf(</pre>
 data = mpdta,
 yname = "lemp",
 tname = "year",
 idname = "countyreal",
 gname = "first.treat",
 covars = c("lpop"))
head(tidy_df)
## End(Not run)
## Now you can call fetwfe() ------
# res <- fetwfe(</pre>
   pdata
             = tidy_df,
  time_var = "time_var",
#
  unit_var = "unit_var",
  treatment = "treatment",
   response = "response",
#
             = c("lpop"))
   covs
```

betwfe

Bridge-penalized extended two-way fixed effects

## **Description**

Implementation of extended two-way fixed effects with a bridge penalty. Estimates overall ATT as well as CATT (cohort average treatment effects on the treated units).

## Usage

```
betwfe(
  pdata,
  time_var,
  unit_var,
  treatment,
  response,
  covs = c(),
  indep_counts = NA,
  sig_eps_sq = NA,
  sig_eps_c_sq = NA,
  lambda.max = NA,
  lambda.min = NA,
  nlambda = 100,
  q = 0.5,
```

```
verbose = FALSE,
alpha = 0.05,
add_ridge = FALSE
)
```

#### **Arguments**

pdata

Dataframe; the panel data set. Each row should represent an observation of a unit at a time. Should contain columns as described below.

time\_var

Character; the name of a single column containing a variable for the time period. This column is expected to contain integer values (for example, years). Recommended encodings for dates include format YYYY, YYYYMM, or YYYYMMDD, whichever is appropriate for your data.

unit\_var

Character; the name of a single column containing a variable for each unit. This column is expected to contain character values (i.e. the "name" of each unit).

treatment

Character; the name of a single column containing a variable for the treatment dummy indicator. This column is expected to contain integer values, and in particular, should equal 0 if the unit was untreated at that time and 1 otherwise. Treatment should be an absorbing state; that is, if unit i is treated at time t, then it must also be treated at all times t+1, ..., T. Any units treated in the first time period will be removed automatically. Please make sure yourself that at least some units remain untreated at the final time period ("never-treated units").

response

Character; the name of a single column containing the response for each unit at each time. The response must be an integer or numeric value.

covs

(Optional.) Character; a vector containing the names of the columns for covariates. All of these columns are expected to contain integer, numeric, or factor values, and any categorical values will be automatically encoded as binary indicators. If no covariates are provided, the treatment effect estimation will proceed, but it will only be valid under unconditional versions of the parallel trends and no anticipation assumptions. Default is c().

indep\_counts

(Optional.) Integer; a vector. If you have a sufficiently large number of units, you can optionally randomly split your data set in half (with N units in each data set). The data for half of the units should go in the pdata argument provided above. For the other N units, simply provide the counts for how many units appear in the untreated cohort plus each of the other R cohorts in this argument indep\_counts. The benefit of doing this is that the standard error for the average treatment effect will be (asymptotically) exact instead of conservative. The length of indep\_counts must equal 1 plus the number of treated cohorts in pdata. All entries of indep\_counts must be strictly positive (if you are concerned that this might not work out, maybe your data set is on the small side and it's best to just leave your full data set in pdata). The sum of all the counts in indep\_counts must match the total number of units in pdata. Default is NA (in which case conservative standard errors will be calculated if q < 1.)

sig\_eps\_sq

(Optional.) Numeric; the variance of the row-level IID noise assumed to apply to each observation. See Section 2 of Faletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be

estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.

sig\_eps\_c\_sq

(Optional.) Numeric; the variance of the unit-level IID noise (random effects) assumed to apply to each observation. See Section 2 of Faletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.

lambda.max

(Optional.) Numeric. A penalty parameter lambda will be selected over a grid search by BIC in order to select a single model. The largest lambda in the grid will be lambda.max. If no lambda.max is provided, one will be selected automatically. When q <= 1, the model will be sparse, and ideally all of the following are true at once: the smallest model (the one corresponding to lambda.max) selects close to 0 features, the largest model (the one corresponding to lambda.min) selects close to p features, nlambda is large enough so that models are considered at every feasible model size, and nlambda is small enough so that the computation doesn't become infeasible. You may want to manually tweak lambda.max, lambda.min, and nlambda to try to achieve these goals, particularly if the selected model size is very close to the model corresponding to lambda.max or lambda.min, which could indicate that the range of lambda values was too narrow or coarse. You can use the function outputs lambda.max\_model\_size, lambda.min\_model\_size, and lambda\_star\_model\_size to try to assess this. Default is NA.

lambda.min

(Optional.) Numeric. The smallest lambda penalty parameter that will be considered. See the description of lambda.max for details. Default is NA.

nlambda

(Optional.) Integer. The total number of lambda penalty parameters that will be considered. See the description of lambda.max for details. Default is 100.

q

(Optional.) Numeric; determines what  $L_q$  penalty is used for the regularization. q=1 is the lasso, and for 0 < q < 1, it is possible to get standard errors and confidence intervals. q=2 is ridge regression. See Faletto (2025) for details. Default is 0.5.

verbose

Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.

alpha

Numeric; function will calculate (1 - alpha) confidence intervals for the cohort average treatment effects that will be returned in catt\_df.

add\_ridge

(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

# Value

A named list with the following elements:

att\_hat The estimated overall average treatment effect for a randomly selected treated

unit.

att\_se If q < 1, a standard error for the ATT. If indep\_counts was provided, this stan-

dard error is asymptotically exact; if not, it is asymptotically conservative. If q

>= 1, this will be NA.

catt\_hats A named vector containing the estimated average treatment effects for each cohort. If q < 1, a named vector containing the (asymptotically exact, non-conservative) catt\_ses standard errors for the estimated average treatment effects within each cohort. cohort\_probs A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating att\_hat. If indep\_counts was provided, cohort\_probs was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in pdata. A dataframe displaying the cohort names, average treatment effects, standard catt\_df errors, and 1 - alpha confidence interval bounds. beta\_hat The full vector of estimated coefficients. treat inds The indices of beta\_hat corresponding to the treatment effects for each cohort at each time. treat\_int\_inds The indices of beta\_hat corresponding to the interactions between the treatment effects for each cohort at each time and the covariates. sig\_eps\_sq Either the provided sig\_eps\_sq or the estimated one, if a value wasn't provided. Either the provided sig\_eps\_c\_sq or the estimated one, if a value wasn't prosig\_eps\_c\_sq vided. lambda.max Either the provided lambda.max or the one that was used, if a value wasn't provided. (This is returned to help with getting a reasonable range of lambda values for grid search.) lambda.max\_model\_size The size of the selected model corresponding lambda.max (for q <= 1, this will be the smallest model size). As mentioned above, for q <= 1 ideally this value is close to 0. lambda.min Either the provided lambda.min or the one that was used, if a value wasn't provided. lambda.min\_model\_size The size of the selected model corresponding to lambda.min (for q <= 1, this will be the largest model size). As mentioned above, for  $q \le 1$  ideally this value is close to p. lambda star The value of lambda chosen by BIC. If this value is close to lambda.min or lambda.max, that could suggest that the range of lambda values should be expanded. lambda\_star\_model\_size The size of the model that was selected. If this value is close to lambda.max\_model\_size or lambda.min\_model\_size, That could suggest that the range of lambda values should be expanded.  $X_{ints}$ The design matrix created containing all interactions, time and cohort dummies, The vector of responses, containing nrow(X\_ints) entries. X\_final The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance

matrix for each unit.

y_final	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
N	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
Т	The number of time periods in the final data set.
R	The final number of treated cohorts that appear in the final data set.
d	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
р	The final number of columns in the full set of covariates used to estimate the model.

#### Author(s)

Gregory Faletto

#### References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. https://arxiv.org/abs/2312.05985. Pesaran, M. H. . Time Series and Panel Data Econometrics. Number 9780198759980 in OUP Catalogue. Oxford University Press, 2015. URL https://ideas.repec.org/b/oxp/obooks/9780198759980.html.

```
set.seed(23451)
library(bacondecomp)
data(divorce)
# sig_eps_sq and sig_eps_c_sq, calculated in a separate run of `fetwfe(),
# are provided to speed up the computation of the example
res <- betwfe(
   pdata = divorce[divorce$sex == 2, ],
    time_var = "year",
   unit_var = "st",
    treatment = "changed",
    covs = c("murderrate", "lnpersinc", "afdcrolls"),
    response = "suiciderate_elast_jag",
    sig_{eps_{q}} = 0.1025361,
    sig_eps_c_sq = 4.227651e-35,
    verbose = TRUE)
# Average treatment effect on the treated units (in percentage point
# units)
100 * res$att_hat
# Conservative 95% confidence interval for ATT (in percentage point units)
```

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```
low_att <- 100 * (res$att_hat - qnorm(1 - 0.05 / 2) * res$att_se)
high_att <- 100 * (res$att_hat + qnorm(1 - 0.05 / 2) * res$att_se)

c(low_att, high_att)

# Cohort average treatment effects and confidence intervals (in percentage
# point units)

catt_df_pct <- res$catt_df
catt_df_pct[["Estimated TE"]] <- 100 * catt_df_pct[["Estimated TE"]]
catt_df_pct[["SE"]] <- 100 * catt_df_pct[["SE"]]
catt_df_pct[["ConfIntLow"]] <- 100 * catt_df_pct[["ConfIntLow"]]
catt_df_pct[["ConfIntHigh"]] <- 100 * catt_df_pct[["ConfIntHigh"]]</pre>
```

betwfeWithSimulatedData

Run BETWFE on Simulated Data

#### **Description**

This function runs the bridge-penalized extended two-way fixed effects estimator (betwfe()) on simulated data. It is simply a wrapper for betwfe(): it accepts an object of class "FETWFE\_simulated" (produced by simulateData()) and unpacks the necessary components to pass to betwfe(). So the outputs match betwfe(), and the needed inputs match their counterparts in betwfe().

#### Usage

```
betwfeWithSimulatedData(
    simulated_obj,
    lambda.max = NA,
    lambda.min = NA,
    nlambda = 100,
    q = 0.5,
    verbose = FALSE,
    alpha = 0.05,
    add_ridge = FALSE
)
```

#### **Arguments**

 $1 {\sf ambda.max}$ 

simulated\_obj An object of class "FETWFE\_simulated" containing the simulated panel data

and design matrix.

(Optional.) Numeric. A penalty parameter lambda will be selected over a grid search by BIC in order to select a single model. The largest lambda in the grid will be lambda.max. If no lambda.max is provided, one will be selected

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automatically. For lambda <= 1, the model will be sparse, and ideally all of the following are true at once: the smallest model (the one corresponding to lambda.max) selects close to 0 features, the largest model (the one corresponding to lambda.min) selects close to p features, nlambda is large enough so that models are considered at every feasible model size, and nlambda is small enough so that the computation doesn't become infeasible. You may want to manually tweak lambda.max, lambda.min, and nlambda to try to achieve these goals, particularly if the selected model size is very close to the model corresponding to lambda.max or lambda.min, which could indicate that the range of lambda values was too narrow. You can use the function outputs lambda.max\_model\_size, lambda.min\_model\_size, and lambda\_star\_model\_size to try to assess this. Default is NA.

lambda.min

(Optional.) Numeric. The smallest lambda penalty parameter that will be considered. See the description of lambda.max for details. Default is NA.

nlambda

(Optional.) Integer. The total number of lambda penalty parameters that will be considered. See the description of lambda.max for details. Default is 100.

q

(Optional.) Numeric; determines what  $L_q$  penalty is used for the fusion regularization. q=1 is the lasso, and for 0 < q < 1, it is possible to get standard errors and confidence intervals. q=2 is ridge regression. See Faletto (2025) for

details. Default is 0.5.

verbose

Logical; if TRUE, more details on the progress of the function will be printed as

the function executes. Default is FALSE.

alpha

Numeric; function will calculate (1 - alpha) confidence intervals for the cohort

average treatment effects that will be returned in catt\_df.

add\_ridge

(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

#### Value

A named list with the following elements:

att\_hat The estimated overall average treatment effect for a randomly selected treated

unit

att\_se If q < 1, a standard error for the ATT. If indep\_counts was provided, this stan-

dard error is asymptotically exact; if not, it is asymptotically conservative. If q

>= 1, this will be NA.

catt\_hats A named vector containing the estimated average treatment effects for each co-

hort.

catt\_ses If q < 1, a named vector containing the (asymptotically exact, non-conservative)

standard errors for the estimated average treatment effects within each cohort.

cohort\_probs A vector of the estimated probabilities of being in each cohort conditional on

being treated, which was used in calculating att\_hat. If indep\_counts was provided, cohort\_probs was calculated from that; otherwise, it was calculated

from the counts of units in each treated cohort in pdata.

catt\_df A dataframe displaying the cohort names, average treatment effects, standard

errors, and 1 - alpha confidence interval bounds.

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beta_hat	The full vector of estimated coefficients.
treat_inds	The indices of beta_hat corresponding to the treatment effects for each cohort at each time.
treat_int_inds	The indices of beta_hat corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
sig_eps_sq	Either the provided sig_eps_sq or the estimated one, if a value wasn't provided.
sig_eps_c_sq	Either the provided sig_eps_c_sq or the estimated one, if a value wasn't provided.
lambda.max	Either the provided lambda.max or the one that was used, if a value wasn't provided. (This is returned to help with getting a reasonable range of lambda values for grid search.)
lambda.max_mode	
	The size of the selected model corresponding lambda.max (for $q \le 1$ , this will be the smallest model size). As mentioned above, for $q \le 1$ ideally this value is close to 0.
lambda.min	Either the provided lambda.min or the one that was used, if a value wasn't provided.
lambda.min_mode	
	The size of the selected model corresponding to lambda.min (for $q \le 1$ , this will be the largest model size). As mentioned above, for $q \le 1$ ideally this value is close to p.
lambda_star	The value of lambda chosen by BIC. If this value is close to lambda.min or lambda.max, that could suggest that the range of lambda values should be expanded.
lambda_star_mod	•
	The size of the model that was selected. If this value is close to lambda.max_model_size or lambda.min_model_size, That could suggest that the range of lambda values should be expanded.
X_ints	The design matrix created containing all interactions, time and cohort dummies, etc.
у	The vector of responses, containing nrow(X_ints) entries.
X_final	The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
y_final	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
N	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
Т	The number of time periods in the final data set.
R	The final number of treated cohorts that appear in the final data set.
d	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
p	The final number of columns in the full set of covariates used to estimate the model.

## **Examples**

```
## Not run:
    # Generate coefficients
    coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
    sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

    result <- betwfeWithSimulatedData(sim_data)

## End(Not run)</pre>
```

etwfe

Extended two-way fixed effects

# **Description**

Implementation of extended two-way fixed effects. Estimates overall ATT as well as CATT (cohort average treatment effects on the treated units).

#### Usage

```
etwfe(
  pdata,
  time_var,
  unit_var,
  treatment,
  response,
  covs = c(),
  indep_counts = NA,
  sig_eps_sq = NA,
  sig_eps_c_sq = NA,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)
```

## **Arguments**

pdata

Dataframe; the panel data set. Each row should represent an observation of a unit at a time. Should contain columns as described below.

time\_var

Character; the name of a single column containing a variable for the time period. This column is expected to contain integer values (for example, years). Recommended encodings for dates include format YYYY, YYYYMM, or YYYYMMDD, whichever is appropriate for your data.

unit\_var

Character; the name of a single column containing a variable for each unit. This column is expected to contain character values (i.e. the "name" of each unit).

treatment

Character; the name of a single column containing a variable for the treatment dummy indicator. This column is expected to contain integer values, and in particular, should equal 0 if the unit was untreated at that time and 1 otherwise. Treatment should be an absorbing state; that is, if unit i is treated at time t, then it must also be treated at all times t+1, ..., T. Any units treated in the first time period will be removed automatically. Please make sure yourself that at least some units remain untreated at the final time period ("never-treated units").

response

Character; the name of a single column containing the response for each unit at each time. The response must be an integer or numeric value.

covs

(Optional.) Character; a vector containing the names of the columns for covariates. All of these columns are expected to contain integer, numeric, or factor values, and any categorical values will be automatically encoded as binary indicators. If no covariates are provided, the treatment effect estimation will proceed, but it will only be valid under unconditional versions of the parallel trends and no anticipation assumptions. Default is c().

indep\_counts

(Optional.) Integer; a vector. If you have a sufficiently large number of units, you can optionally randomly split your data set in half (with N units in each data set). The data for half of the units should go in the pdata argument provided above. For the other N units, simply provide the counts for how many units appear in the untreated cohort plus each of the other R cohorts in this argument indep\_counts. The benefit of doing this is that the standard error for the average treatment effect will be (asymptotically) exact instead of conservative. The length of indep\_counts must equal 1 plus the number of treated cohorts in pdata. All entries of indep\_counts must be strictly positive (if you are concerned that this might not work out, maybe your data set is on the small side and it's best to just leave your full data set in pdata). The sum of all the counts in indep\_counts must match the total number of units in pdata. Default is NA (in which case conservative standard errors will be calculated if q < 1.)

sig\_eps\_sq

(Optional.) Numeric; the variance of the row-level IID noise assumed to apply to each observation. See Section 2 of Faletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.

sig\_eps\_c\_sq

(Optional.) Numeric; the variance of the unit-level IID noise (random effects) assumed to apply to each observation. See Section 2 of Faletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.

verbose

Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.

alpha

Numeric; function will calculate (1 - alpha) confidence intervals for the cohort average treatment effects that will be returned in catt\_df.

add\_ridge (Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

# Value

A named list with the following elements:

att_hat	The estimated overall average treatment effect for a randomly selected treated unit.
att_se	A standard error for the ATT. If the Gram matrix is not invertible, this will be NA.
catt_hats	A named vector containing the estimated average treatment effects for each cohort.
catt_ses	A named vector containing the (asymptotically exact) standard errors for the estimated average treatment effects within each cohort.
cohort_probs	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating att_hat. If indep_counts was provided, cohort_probs was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in pdata.
catt_df	A dataframe displaying the cohort names, average treatment effects, standard errors, and 1 - alpha confidence interval bounds.
beta_hat	The full vector of estimated coefficients.
treat_inds	The indices of beta_hat corresponding to the treatment effects for each cohort at each time.
treat_int_inds	The indices of beta_hat corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
sig_eps_sq	Either the provided sig_eps_sq or the estimated one, if a value wasn't provided.
sig_eps_c_sq	Either the provided sig_eps_c_sq or the estimated one, if a value wasn't provided.
X_ints	The design matrix created containing all interactions, time and cohort dummies, etc.
У	The vector of responses, containing nrow(X_ints) entries.
X_final	The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
y_final	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
N	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
T	The number of time periods in the final data set.
R	The final number of treated cohorts that appear in the final data set.
d	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
p	The final number of columns in the full set of covariates used to estimate the model.

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#### Author(s)

Gregory Faletto

#### References

Wooldridge, J. M. (2021). Two-way fixed effects, the two-way mundlak regression, and difference-in-differences estimators. *Available at SSRN 3906345*. doi:10.2139/ssrn.3906345.

etwfe-class

Extended Two-Way Fixed Effects Output Class

## **Description**

S3 class for the output of etwfe().

etwfeToFetwfeDf

Convert data prepared for etwfe::etwfe() to the format required by fetwfe() and fetwfe::etwfe()

## Description

etwfeToFetwfeDf() reshapes and renames a panel dataset that is already formatted for etwfe::etwfe() (McDermott 2024) so that it can be passed directly to fetwfe()oretwfe()from thefetwfe' package. In particular, it

- creates an absorbing-state treatment dummy that equals 1 from the first treated period onward\* and 0 otherwise,
- (optionally) drops units that are already treated in the very first period of the sample (because fetwfe() removes them internally), and
- returns a tidy dataframe whose column names match the arguments that fetwfe()/etwfe() expect.

# Usage

```
etwfeToFetwfeDf(
  data,
  yvar,
  tvar,
  idvar,
  gvar,
  covars = character(0),
  drop_first_period_treated = TRUE,
  out_names = list(time = "time_var", unit = "unit_var", treatment = "treatment",
      response = "response")
)
```

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# **Arguments**

data	A long-format data.frame that you could already feed to etwfe().
yvar	Character. Column name of the outcome (left-hand side in your fml).
tvar	Character. Column name of the time variable that you pass to etwfe() as tvar.
idvar	Character. Column name of the unit identifier (the variable you would cluster on, or pass to etwfe(, ivar = idvar) if you were using unit FEs).
gvar	Character. Column name of the "first treated" cohort variable passed to etwfe() as gvar. Must be 0 for never-treated units, or the (strictly positive) first treated period.
covars	Character vector of $additional$ covariate columns to keep (default character (0)).
drop_first_peri	od_treated
	Logical. Should units already treated in the very first sample period be removed? (fetwfe() will drop them internally anyway, but doing it here keeps the returned dataframe clean.) Default TRUE.
out_names	Named list giving the column names that the returned dataframe should have. The default (time, unit, treatment, y) matches the arguments usually supplied to fetwfe(). <b>Do not change the </b> <i>names</i> <b> of this list</b> – only the <i>values</i> – and keep all four.

#### Value

A tidy data. frame with (in this order)

- time integer,
- unit character,
- treatment integer 0/1 absorbing-state dummy,
- response numeric outcome,
- any covariates requested in covars. Ready to pass straight to fetwfe() or fetwfe::etwfe().

#### References

McDermott G (2024). *etwfe: Extended Two-Way Fixed Effects*. doi:10.32614/CRAN.package.etwfe doi:10.32614/CRAN.package.etwfe, R package version 0.5.0, https://CRAN.R-project.org/package=etwfe.

```
## toy example -----
## Not run:
library(did) # provides the mpdta example dataframe
data(mpdta)

head(mpdta)

tidy_df <- etwfeToFetwfeDf(
  data = mpdta,</pre>
```

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```
yvar = "lemp",
 tvar = "year",
 idvar = "countyreal",
 gvar = "first.treat",
 covars = c("lpop"))
head(tidy_df)
## End(Not run)
## Now you can call fetwfe() -------
# res <- fetwfe(</pre>
   pdata
         = tidy_df,
   time_var = "time_var"
   unit_var = "unit_var",
   treatment = "treatment",
#
   response = "response",
            = c("lpop"))
   covs
```

etwfeWithSimulatedData

Run ETWFE on Simulated Data

# Description

This function runs the extended two-way fixed effects estimator (etwfe()) on simulated data. It is simply a wrapper for etwfe(): it accepts an object of class "FETWFE\_simulated" (produced by simulateData()) and unpacks the necessary components to pass to etwfe(). So the outputs match etwfe(), and the needed inputs match their counterparts in etwfe().

#### Usage

```
etwfeWithSimulatedData(
    simulated_obj,
    verbose = FALSE,
    alpha = 0.05,
    add_ridge = FALSE
)
```

## **Arguments**

 $\verb|simulated_obj| An object of class "FETWFE\_simulated" containing the simulated panel data|\\$ 

and design matrix.

verbose Logical; if TRUE, more details on the progress of the function will be printed as

the function executes. Default is FALSE.

alpha Numeric; function will calculate (1 - alpha) confidence intervals for the cohort

average treatment effects that will be returned in catt\_df.

add\_ridge (Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the

(untransformed) coefficients to stabilize estimation. Default is FALSE.

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# Value

A named list with the following elements:

71 numed not with	the following elements.
att_hat	The estimated overall average treatment effect for a randomly selected treated unit.
att_se	A standard error for the ATT. If the Gram matrix is not invertible, this will be NA.
catt_hats	A named vector containing the estimated average treatment effects for each cohort.
catt_ses	A named vector containing the (asymptotically exact) standard errors for the estimated average treatment effects within each cohort.
cohort_probs	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating att_hat. If indep_counts was provided, cohort_probs was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in pdata.
catt_df	A dataframe displaying the cohort names, average treatment effects, standard errors, and 1 - alpha confidence interval bounds.
beta_hat	The full vector of estimated coefficients.
treat_inds	The indices of beta_hat corresponding to the treatment effects for each cohort at each time.
treat_int_inds	The indices of beta_hat corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
sig_eps_sq	Either the provided sig_eps_sq or the estimated one, if a value wasn't provided.
sig_eps_c_sq	Either the provided sig_eps_c_sq or the estimated one, if a value wasn't provided.
X_ints	The design matrix created containing all interactions, time and cohort dummies, etc.
у	The vector of responses, containing nrow(X_ints) entries.
X_final	The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
y_final	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
N	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
T	The number of time periods in the final data set.
R	The final number of treated cohorts that appear in the final data set.
d	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
p	The final number of columns in the full set of covariates used to estimate the model.

#### **Examples**

```
## Not run:
    # Generate coefficients
    coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
    sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

    result <- etwfeWithSimulatedData(sim_data)

## End(Not run)</pre>
```

fetwfe

Fused extended two-way fixed effects

# **Description**

Implementation of fused extended two-way fixed effects. Estimates overall ATT as well as CATT (cohort average treatment effects on the treated units).

## Usage

```
fetwfe(
  pdata,
  time_var,
  unit_var,
  treatment,
  response,
  covs = c(),
  indep\_counts = NA,
  sig_eps_sq = NA,
  sig_eps_c_sq = NA,
  lambda.max = NA,
  lambda.min = NA,
  nlambda = 100,
 q = 0.5,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)
```

# Arguments

pdata

Dataframe; the panel data set. Each row should represent an observation of a unit at a time. Should contain columns as described below.

time\_var Character; the n

Character; the name of a single column containing a variable for the time period. This column is expected to contain integer values (for example, years). Recommended encodings for dates include format YYYY, YYYYMM, or YYYYM-MDD, which were is expressint a for your date.

MDD, whichever is appropriate for your data.

unit\_var Character; the name of a single column containing a variable for each unit. This

column is expected to contain character values (i.e. the "name" of each unit).

Character; the name of a single column containing a variable for the treatment dummy indicator. This column is expected to contain integer values, and in particular, should equal 0 if the unit was untreated at that time and 1 otherwise. Treatment should be an absorbing state; that is, if unit i is treated at time t, then it must also be treated at all times t + 1, ..., T. Any units treated in the first time period will be removed automatically. Please make sure yourself that at least some units remain untreated at the final time period ("never-treated units").

Character; the name of a single column containing the response for each unit at each time. The response must be an integer or numeric value.

(Optional.) Character; a vector containing the names of the columns for covariates. All of these columns are expected to contain integer, numeric, or factor values, and any categorical values will be automatically encoded as binary indicators. If no covariates are provided, the treatment effect estimation will proceed, but it will only be valid under unconditional versions of the parallel trends

and no anticipation assumptions. Default is c().

(Optional.) Integer; a vector. If you have a sufficiently large number of units, you can optionally randomly split your data set in half (with N units in each data set). The data for half of the units should go in the pdata argument provided above. For the other N units, simply provide the counts for how many units appear in the untreated cohort plus each of the other R cohorts in this argument indep\_counts. The benefit of doing this is that the standard error for the average treatment effect will be (asymptotically) exact instead of conservative. The length of indep\_counts must equal 1 plus the number of treated cohorts in pdata. All entries of indep\_counts must be strictly positive (if you are concerned that this might not work out, maybe your data set is on the small side and it's best to just leave your full data set in pdata). The sum of all the counts in indep\_counts must match the total number of units in pdata. Default is NA (in which case conservative standard errors will be calculated if q < 1.)

(Optional.) Numeric; the variance of the row-level IID noise assumed to apply to each observation. See Section 2 of Faletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.

(Optional.) Numeric; the variance of the unit-level IID noise (random effects) assumed to apply to each observation. See Section 2 of Faletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.

treatment

response

covs

indep\_counts

sig\_eps\_sq

sig\_eps\_c\_sq

1	am	hd	la	max

(Optional.) Numeric. A penalty parameter lambda will be selected over a grid search by BIC in order to select a single model. The largest lambda in the grid will be lambda.max. If no lambda.max is provided, one will be selected automatically. When q <= 1, the model will be sparse, and ideally all of the following are true at once: the smallest model (the one corresponding to lambda.max) selects close to 0 features, the largest model (the one corresponding to lambda.min) selects close to p features, nlambda is large enough so that models are considered at every feasible model size, and nlambda is small enough so that the computation doesn't become infeasible. You may want to manually tweak lambda.max, lambda.min, and nlambda to try to achieve these goals, particularly if the selected model size is very close to the model corresponding to lambda.max or lambda.min, which could indicate that the range of lambda values was too narrow or coarse. You can use the function outputs lambda.max\_model\_size, lambda.min\_model\_size, and lambda\_star\_model\_size to try to assess this. Default is NA.

lambda.min

(Optional.) Numeric. The smallest lambda penalty parameter that will be considered. See the description of lambda.max for details. Default is NA.

nlambda

(Optional.) Integer. The total number of lambda penalty parameters that will be considered. See the description of lambda.max for details. Default is 100.

q

(Optional.) Numeric; determines what  $L_q$  penalty is used for the fusion regularization. q=1 is the lasso, and for 0 < q < 1, it is possible to get standard errors and confidence intervals. q=2 is ridge regression. See Faletto (2025) for details. Default is 0.5.

verbose

 $Logical; if \ TRUE, more \ details \ on \ the \ progress \ of \ the \ function \ will \ be \ printed \ as$ 

the function executes. Default is FALSE.

alpha

Numeric; function will calculate (1 - alpha) confidence intervals for the cohort average treatment effects that will be returned in catt\_df.

add\_ridge

(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

#### Value

An object of class fetwfe containing the following elements:

att_hat	The estimated overall average treatment effect for a randomly selected treated unit.
att_se	If $q < 1$ , a standard error for the ATT. If indep_counts was provided, this standard error is asymptotically exact; if not, it is asymptotically conservative. If $q >= 1$ , this will be NA.
catt_hats	A named vector containing the estimated average treatment effects for each cohort.
catt_ses	If q < 1, a named vector containing the (asymptotically exact, non-conservative) standard errors for the estimated average treatment effects within each cohort.
cohort_probs	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating att_hat. If indep_counts was provided, cohort_probs was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in pdata.

catt\_df A dataframe displaying the cohort names, average treatment effects, standard errors, and 1 - alpha confidence interval bounds. beta\_hat The full vector of estimated coefficients. The indices of beta\_hat corresponding to the treatment effects for each cohort treat\_inds at each time. The indices of beta\_hat corresponding to the interactions between the treattreat\_int\_inds ment effects for each cohort at each time and the covariates. Either the provided sig\_eps\_sq or the estimated one, if a value wasn't provided. sig\_eps\_sq Either the provided sig\_eps\_c\_sq or the estimated one, if a value wasn't prosig\_eps\_c\_sq vided. lambda.max Either the provided lambda.max or the one that was used, if a value wasn't provided. (This is returned to help with getting a reasonable range of lambda values for grid search.) lambda.max\_model\_size The size of the selected model corresponding to lambda.max (for q <= 1, this will be the smallest model size). As mentioned above, for q <= 1 ideally this value is close to 0. lambda.min Either the provided lambda.min or the one that was used, if a value wasn't provided. lambda.min\_model\_size The size of the selected model corresponding to lambda.min (for  $q \le 1$ , this will be the largest model size). As mentioned above, for  $q \le 1$  ideally this value is close to p. The value of lambda chosen by BIC. If this value is close to lambda.min or lambda\_star lambda.max, that could suggest that the range of lambda values should be expanded. lambda\_star\_model\_size The size of the model that was selected. If this value is close to lambda.max\_model\_size or lambda.min\_model\_size, that could suggest that the range of lambda values should be expanded. N The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period). The number of time periods in the final data set. Т R The final number of treated cohorts that appear in the final data set. The final number of covariates that appear in the final data set (after any co-Ч variates may have been removed because they contained missing values or all contained the same value for every unit). The final number of columns in the full set of covariates used to estimate the p model. alpha The alpha level used for confidence intervals. internal A list containing internal outputs that are typically not needed for interpretation: **X** ints The design matrix created containing all interactions, time and cohort

dummies, etc.

- y The vector of responses, containing nrow(X\_ints) entries.
- **X\_final** The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.

**y\_final** The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.

calc ses Logical indicating whether standard errors were calculated.

The object has methods for print(), summary(), and coef(). By default, print() and summary() only show the essential outputs. To see internal details, use  $print(x, show_internal = TRUE)$  or  $summary(x, show_internal = TRUE)$ . The coef() method returns the vector of estimated coefficients (beta\_hat).

## Author(s)

Gregory Faletto

#### References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. https://arxiv.org/abs/2312.05985. Pesaran, M. H. . Time Series and Panel Data Econometrics. Number 9780198759980 in OUP Catalogue. Oxford University Press, 2015. URL https://ideas.repec.org/b/oxp/obooks/9780198759980.html.

```
set.seed(23451)
library(bacondecomp)
data(divorce)
# sig_eps_sq and sig_eps_c_sq, calculated in a separate run of `fetwfe(),
# are provided to speed up the computation of the example
res <- fetwfe(
   pdata = divorce[divorce$sex == 2, ],
    time_var = "year",
   unit_var = "st",
   treatment = "changed",
   covs = c("murderrate", "lnpersinc", "afdcrolls"),
    response = "suiciderate_elast_jag",
    sig_eps_sq = 0.1025361,
    sig_eps_c_sq = 4.227651e-35,
    verbose = TRUE)
# Print results with internal details
print(res, max_cohorts = Inf)
```

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fetwfe-class

Fused Extended Two-Way Fixed Effects Output Class

#### Description

S3 class for the output of fetwfe().

fetwfeWithSimulatedData

Run FETWFE on Simulated Data

#### **Description**

This function runs the fused extended two-way fixed effects estimator (fetwfe()) on simulated data. It is simply a wrapper for fetwfe(): it accepts an object of class "FETWFE\_simulated" (produced by simulateData()) and unpacks the necessary components to pass to fetwfe(). So the outputs match fetwfe(), and the needed inputs match their counterparts in fetwfe().

## Usage

```
fetwfeWithSimulatedData(
    simulated_obj,
    lambda.max = NA,
    lambda.min = NA,
    nlambda = 100,
    q = 0.5,
    verbose = FALSE,
    alpha = 0.05,
    add_ridge = FALSE
)
```

## Arguments

simulated\_obj

An object of class "FETWFE\_simulated" containing the simulated panel data and design matrix.

lambda.max

(Optional.) Numeric. A penalty parameter lambda will be selected over a grid search by BIC in order to select a single model. The largest lambda in the grid will be lambda.max. If no lambda.max is provided, one will be selected automatically. For lambda <= 1, the model will be sparse, and ideally all of the following are true at once: the smallest model (the one corresponding to lambda.max) selects close to 0 features, the largest model (the one corresponding to lambda.min) selects close to p features, nlambda is large enough so that models are considered at every feasible model size, and nlambda is small enough so that the computation doesn't become infeasible. You may want to manually

	tweak lambda.max, lambda.min, and nlambda to try to achieve these goals, particularly if the selected model size is very close to the model corresponding to lambda.max or lambda.min, which could indicate that the range of lambda values was too narrow. You can use the function outputs lambda.max_model_size, lambda.min_model_size, and lambda_star_model_size to try to assess this. Default is NA.
lambda.min	(Optional.) Numeric. The smallest lambda penalty parameter that will be considered. See the description of lambda.max for details. Default is NA.
nlambda	(Optional.) Integer. The total number of lambda penalty parameters that will be considered. See the description of lambda.max for details. Default is 100.
q	(Optional.) Numeric; determines what $L_q$ penalty is used for the fusion regularization. $q=1$ is the lasso, and for $0 < q < 1$ , it is possible to get standard errors and confidence intervals. $q=2$ is ridge regression. See Faletto (2025) for details. Default is 0.5.
verbose	Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.
alpha	Numeric; function will calculate (1 - alpha) confidence intervals for the cohort average treatment effects that will be returned in catt_df.
add_ridge	(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

# Value

An object of class fetwfe containing the following elements:

att_hat	The estimated overall average treatment effect for a randomly selected treated unit.
att_se	If $q < 1$ , a standard error for the ATT. If indep_counts was provided, this standard error is asymptotically exact; if not, it is asymptotically conservative. If $q >= 1$ , this will be NA.
catt_hats	A named vector containing the estimated average treatment effects for each cohort.
catt_ses	If q < 1, a named vector containing the (asymptotically exact, non-conservative) standard errors for the estimated average treatment effects within each cohort.
cohort_probs	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating att_hat. If indep_counts was provided, cohort_probs was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in pdata.
catt_df	A dataframe displaying the cohort names, average treatment effects, standard errors, and 1 - alpha confidence interval bounds.
beta_hat	The full vector of estimated coefficients.
treat_inds	The indices of beta_hat corresponding to the treatment effects for each cohort at each time.
treat_int_inds	The indices of beta_hat corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.

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Either the provided sig\_eps\_sq or the estimated one, if a value wasn't provided. sig\_eps\_sq Either the provided sig\_eps\_c\_sq or the estimated one, if a value wasn't prosig\_eps\_c\_sq vided. lambda.max Either the provided lambda.max or the one that was used, if a value wasn't provided. (This is returned to help with getting a reasonable range of lambda values for grid search.) lambda.max\_model\_size The size of the selected model corresponding to lambda.max (for q <= 1, this will be the smallest model size). As mentioned above, for q <= 1 ideally this lambda.min Either the provided lambda.min or the one that was used, if a value wasn't provided. lambda.min\_model\_size The size of the selected model corresponding to lambda.min (for q <= 1, this will be the largest model size). As mentioned above, for q <= 1 ideally this value is close to p. lambda\_star The value of lambda chosen by BIC. If this value is close to lambda.min or lambda.max, that could suggest that the range of lambda values should be expanded. lambda\_star\_model\_size The size of the model that was selected. If this value is close to lambda.max\_model\_size or lambda.min\_model\_size, that could suggest that the range of lambda values should be expanded. Ν The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period). Т The number of time periods in the final data set. The final number of treated cohorts that appear in the final data set. R The final number of covariates that appear in the final data set (after any co-Ч variates may have been removed because they contained missing values or all contained the same value for every unit). The final number of columns in the full set of covariates used to estimate the p model. alpha The alpha level used for confidence intervals. internal A list containing internal outputs that are typically not needed for interpretation: **X\_ints** The design matrix created containing all interactions, time and cohort dummies, etc.

y The vector of responses, containing nrow(X\_ints) entries.

**X\_final** The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.

**y\_final** The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.

calc\_ses Logical indicating whether standard errors were calculated.

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The object has methods for print(), summary(), and coef(). By default, print() and summary() only show the essential outputs. To see internal details, use  $print(x, show_internal = TRUE)$  or  $summary(x, show_internal = TRUE)$ . The coef() method returns the vector of estimated coefficients (beta\_hat).

#### **Examples**

```
## Not run:
    # Generate coefficients
    coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
    sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

    result <- fetwfeWithSimulatedData(sim_data)

## End(Not run)</pre>
```

genCoefs

Generate Coefficient Vector for Data Generation

## **Description**

This function generates a coefficient vector beta for simulation studies of the fused extended two-way fixed effects estimator. It returns an S3 object of class "FETWFE\_coefs" containing beta along with simulation parameters R, T, and d. See the simulation studies section of Faletto (2025) for details.

#### Usage

```
genCoefs(R, T, d, density, eff_size, seed = NULL)
```

#### **Arguments**

R	Integer. The number of treated cohorts (treatment is assumed to start in periods 2 to R + 1).
T	Integer. The total number of time periods.
d	Integer. The number of time-invariant covariates. If $d > 0$ , additional terms corresponding to covariate main effects and interactions are included in beta.
density	Numeric in $(0,1)$ . The probability that any given entry in the initial sparse coefficient vector theta is nonzero.
eff_size	Numeric. The magnitude used to scale nonzero entries in theta. Each nonzero entry is set to eff_size or -eff_size (with a 60 percent chance for a positive value).
seed	(Optional) Integer. Seed for reproducibility.

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#### **Details**

The length of beta is given by

$$p = R + (T - 1) + d + dR + d(T - 1) + num\_treats + (num\_treats \times d)$$

, where the number of treatment parameters is defined as

$$num\_treats = T \times R - \frac{R(R+1)}{2}$$

The function operates in two steps:

- 1. It first creates a sparse vector theta of length p, with nonzero entries occurring with probability density. Nonzero entries are set to eff\_size or -eff\_size (with a 60\
- 2. The full coefficient vector beta is then computed by applying an inverse fusion transform to theta using internal routines (e.g., genBackwardsInvFusionTransformMat() and genInvTwoWayFusionTransformM

#### Value

An object of class "FETWFE\_coefs", which is a list containing:

**beta** A numeric vector representing the full coefficient vector after the inverse fusion transform.

**theta** A numeric vector representing the coefficient vector in the transformed feature space. theta is a sparse vector, which aligns with an assumption that deviations from the restrictions encoded in the FETWFE model are sparse. beta is derived from theta.

- **R** The provided number of treated cohorts.
- **T** The provided number of time periods.
- **d** The provided number of covariates.

**seed** The provided seed.

#### References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. https://arxiv.org/abs/2312.05985.

```
## Not run:
    # Generate coefficients
    coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
    sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

## End(Not run)</pre>
```

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gencoerscore Generale Coefficient vector for Data Generation	genCoefsCore	Generate Coefficient Vector for Data Generation
--	--------------	---

#### **Description**

This function generates a coefficient vector beta along with a sparse auxiliary vector theta for simulation studies of the fused extended two-way fixed effects estimator. The returned beta is formatted to align with the design matrix created by genRandomData(), and is a valid input for the beta argument of that function. The vector theta is sparse, with nonzero entries occurring with probability density and scaled by eff\_size. See the simulation studies section of Faletto (2025) for details.

## Usage

```
genCoefsCore(R, T, d, density, eff_size, seed = NULL)
```

## **Arguments**

R	Integer. The number of treated cohorts (treatment is assumed to start in periods $2$ to $R+1$ ).
Т	Integer. The total number of time periods.
d	Integer. The number of time-invariant covariates. If $d > 0$ , additional terms corresponding to covariate main effects and interactions are included in beta.
density	Numeric in $(0,1)$ . The probability that any given entry in the initial sparse coefficient vector theta is nonzero.
eff_size	Numeric. The magnitude used to scale nonzero entries in theta. Each nonzero entry is set to eff_size or -eff_size (with a 60 percent chance for a positive value).
seed	(Optional) Integer. Seed for reproducibility.

#### **Details**

The length of beta is given by

$$p = R + (T - 1) + d + dR + d(T - 1) + num\_treats + (num\_treats \times d)$$

, where the number of treatment parameters is defined as

$$num\_treats = T \times R - \frac{R(R+1)}{2}$$

The function operates in two steps:

- 1. It first creates a sparse vector theta of length p, with nonzero entries occurring with probability density. Nonzero entries are set to eff\_size or -eff\_size (with a 60\
- 2. The full coefficient vector beta is then computed by applying an inverse fusion transform to theta using internal routines (e.g., genBackwardsInvFusionTransformMat() and genInvTwoWayFusionTransformM

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#### Value

A list with two elements:

beta A numeric vector representing the full coefficient vector after the inverse fusion transform.

**theta** A numeric vector representing the coefficient vector in the transformed feature space. theta is a sparse vector, which aligns with an assumption that deviations from the restrictions encoded in the FETWFE model are sparse. beta is derived from theta.

#### References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. https://arxiv.org/abs/2312.05985.

```
## Not run:
     # Set parameters for the coefficient generation
                              # Number of treated cohorts
     R <- 3
     T <- 6
                                                  # Total number of time periods
     d <- 2
                                            # Number of covariates
     density <- 0.1 # Probability that an entry in the initial vector is nonzero
     eff_size <- 1.5 # Scaling factor for nonzero coefficients
     seed <- 789
                                                # Seed for reproducibility
     # Generate coefficients using genCoefsCore()
     coefs_core <- genCoefsCore(R = R, T = T, d = d, density = density,</pre>
     eff_size = eff_size, seed = seed)
     beta <- coefs_core$beta
     theta <- coefs_core$theta
     # For diagnostic purposes, compute the expected length of beta.
     # The length p is defined internally as:
                p = R + (T - 1) + d + d*R + d*(T - 1) + num_treats + num_treats*d,
     # where num_treats = T * R - (R*(R+1))/2.
     num_treats <- T * R - (R * (R + 1)) / 2
     p_{exp} = T + (T - 1) + d + d + R + d + (T - 1) + num_{treats} +
     cat("Length of beta:", length(beta), "\nExpected length:", p_expected, "\n")
## End(Not run)
```

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## **Description**

This function extracts the true treatment effects from a full coefficient vector as generated by genCoefs(). It calculates the overall average treatment effect on the treated (ATT) as the equal-weighted average of the cohort-specific treatment effects, and also returns the individual treatment effects for each treated cohort.

# Usage

```
getTes(coefs_obj)
```

#### **Arguments**

coefs\_obj

An object of class "FETWFE\_coefs" containing the coefficient vector and simulation parameters.

#### **Details**

The function internally uses auxiliary routines getNumTreats(), getP(), getFirstInds(), getTreatInds(), and getActualCohortTes() to determine the correct indices of treatment effect coefficients in beta. The overall treatment effect is computed as the simple average of these cohort-specific effects.

#### Value

A named list with two elements:

**att\_true** A numeric value representing the overall average treatment effect on the treated. It is computed as the (equal-weighted) mean of the cohort-specific treatment effects.

**actual\_cohort\_tes** A numeric vector containing the true cohort-specific treatment effects, calculated by averaging the coefficients corresponding to the treatment dummies for each cohort.

```
## Not run:
# Generate coefficients
coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)
# Compute the true treatment effects:
te_results <- getTes(coefs)
# Overall average treatment effect on the treated:
print(te_results$att_true)
# Cohort-specific treatment effects:
print(te_results$actual_cohort_tes)
## End(Not run)</pre>
```

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simulateData

Generate Random Panel Data for FETWFE Simulations

## **Description**

Generates a random panel data set for simulation studies of the fused extended two-way fixed effects (FETWFE) estimator by taking an object of class "FETWFE\_coefs" (produced by genCoefs()) and using it to simulate data. The function creates a balanced panel with N units over T time periods, assigns treatment status across R treated cohorts (with equal marginal probabilities for treatment and non-treatment), and constructs a design matrix along with the corresponding outcome. The covariates are generated according to the specified distribution: by default, covariates are drawn from a normal distribution; if distribution = "uniform", they are drawn uniformly from  $[-\sqrt{3},\sqrt{3}]$ . When d=0 (i.e. no covariates), no covariate-related columns or interactions are generated. See the simulation studies section of Faletto (2025) for details.

## Usage

```
simulateData(
  coefs_obj,
 Ν,
  sig_eps_sq,
  sig_eps_c_sq,
 distribution = "gaussian",
  guarantee_rank_condition = FALSE
)
```

#### **Arguments**

An object of class "FETWFE\_coefs" containing the coefficient vector and simucoefs\_obj lation parameters. Ν

Integer. Number of units in the panel.

Numeric. Variance of the idiosyncratic (observation-level) noise. sig\_eps\_sq

Numeric. Variance of the unit-level random effects. sig\_eps\_c\_sq

distribution Character. Distribution to generate covariates. Defaults to "gaussian". If set to

"uniform", covariates are drawn uniformly from  $[-\sqrt{3}, \sqrt{3}]$ .

guarantee\_rank\_condition

(Optional). Logical. If TRUE, the returned data set is guaranteed to have at least d + 1 units per cohort, which is necessary for the final design matrix to have full column rank. Default is FALSE, in which case no such condition is enforced.

#### **Details**

This function extracts simulation parameters from the FETWFE\_coefs object and passes them, along with additional simulation parameters, to the internal function simulateDataCore(). It validates that all necessary components are returned and assigns the S3 class "FETWFE\_simulated" to the output.

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The argument distribution controls the generation of covariates. For "gaussian", covariates are drawn from rnorm; for "uniform", they are drawn from runif on the interval  $[-\sqrt{3}, \sqrt{3}]$  (which ensures that the covariates have unit variance regardless of which distribution is chosen).

When d=0 (i.e. no covariates), the function omits any covariate-related columns and their interactions.

#### Value

An object of class "FETWFE\_simulated", which is a list containing:

**pdata** A dataframe containing generated data that can be passed to fetwfe().

**X** The design matrix X, with p columns with interactions.

y A numeric vector of length  $N \times T$  containing the generated responses.

**covs** A character vector containing the names of the generated features (if d > 0), or simply an empty vector (if d = 0)

time\_var The name of the time variable in pdata

unit\_var The name of the unit variable in pdata

treatment The name of the treatment variable in pdata

response The name of the response variable in pdata

**coefs** The coefficient vector  $\beta$  used for data generation.

first\_inds A vector of indices indicating the first treatment effect for each treated cohort.

**N\_UNTREATED** The number of never-treated units.

**assignments** A vector of counts (of length R+1) indicating how many units fall into the nevertreated group and each of the R treated cohorts.

**indep\_counts** Independent cohort assignments (for auxiliary purposes).

- **p** The number of columns in the design matrix X.
- N Number of units.
- T Number of time periods.
- R Number of treated cohorts.
- **d** Number of covariates.

sig\_eps\_sq The idiosyncratic noise variance.

sig\_eps\_c\_sq The unit-level noise variance.

#### References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. https://arxiv.org/abs/2312.05985.

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#### **Examples**

```
## Not run:
    # Generate coefficients
    coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
    sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

## End(Not run)</pre>
```

simulateDataCore

Generate Random Panel Data for FETWFE Simulations

#### **Description**

Generates a random panel data set for simulation studies of the fused extended two-way fixed effects (FETWFE) estimator. The function creates a balanced panel with N units over T time periods, assigns treatment status across R treated cohorts (with equal marginal probabilities for treatment and non-treatment), and constructs a design matrix along with the corresponding outcome. When  $\text{gen\_ints} = \text{TRUE}$  the full design matrix is returned (including interactions between covariates and fixed effects and treatment indicators). When  $\text{gen\_ints} = \text{FALSE}$  the design matrix is generated in a simpler format (with no interactions) as expected by fetwfe(). Moreover, the covariates are generated according to the specified distribution: by default, covariates are drawn from a normal distribution; if distribution = "uniform", they are drawn uniformly from  $[-\sqrt{3}, \sqrt{3}]$ .

When d=0 (i.e. no covariates), no covariate-related columns or interactions are generated.

See the simulation studies section of Faletto (2025) for details.

# Usage

```
simulateDataCore(
   N,
   T,
   R,
   d,
   sig_eps_sq,
   sig_eps_c_sq,
   beta,
   seed = NULL,
   gen_ints = FALSE,
   distribution = "gaussian",
   guarantee_rank_condition = FALSE
)
```

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#### **Arguments**

N	Integer. Number of units in the panel.	
T	Integer. Number of time periods.	
R	Integer. Number of treated cohorts (with treatment starting in periods 2 to T).	
d	Integer. Number of time-invariant covariates.	
sig_eps_sq	Numeric. Variance of the idiosyncratic (observation-level) noise.	
sig_eps_c_sq	Numeric. Variance of the unit-level random effects.	
beta	Numeric vector. Coefficient vector for data generation. Its required length depends on the value of gen_ints:	
	• If gen_ints = TRUE and d > 0, the expected length is $p=R+(T-1)+d+dR+d(T-1)+num\_treats+num\_treats\times d$ , where $num\_treats=T\times R-\frac{R(R+1)}{2}$ .	
	• If gen_ints = TRUE and d = 0, the expected length is $p=R+(T-1)+num\_treats$ .	
	• If gen_ints = FALSE, the expected length is $p=R+(T-1)+d+num\_treats$ .	
seed	(Optional) Integer. Seed for reproducibility.	
gen_ints	Logical. If TRUE, generate the full design matrix with interactions; if FALSE (the default), generate a design matrix without any interaction terms.	
distribution	Character. Distribution to generate covariates. Defaults to "gaussian". If set to "uniform", covariates are drawn uniformly from $[-\sqrt{3},\sqrt{3}]$ .	
guarantee_rank_condition		

(Optional). Logical. If TRUE, the returned data set is guaranteed to have at least d + 1 units per cohort, which is necessary for the final design matrix to have full column rank. Default is FALSE, in which case no such condition is enforced.

#### **Details**

When gen\_ints = TRUE, the function constructs the design matrix by first generating base fixed effects and a long-format covariate matrix (via generateBaseEffects()), then appending interactions between the covariates and cohort/time fixed effects (via generateFEInts()) and finally treatment indicator columns and treatment-covariate interactions (via genTreatVarsSim() and genTreatInts()). When gen\_ints = FALSE, the design matrix consists only of the base fixed effects, covariates, and treatment indicators.

The argument distribution controls the generation of covariates. For "gaussian", covariates are drawn from rnorm; for "uniform", they are drawn from runif on the interval  $[-\sqrt{3}, \sqrt{3}]$ .

When d=0 (i.e. no covariates), the function omits any covariate-related columns and their interactions.

#### Value

An object of class "FETWFE\_simulated", which is a list containing:

**pdata** A dataframe containing generated data that can be passed to fetwfe().

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**X** The design matrix. When gen\_ints = TRUE, X has p columns with interactions; when gen\_ints = FALSE, X has no interactions.

 ${\bf y}~{\bf A}$  numeric vector of length  $N\times T$  containing the generated responses.

**covs** A character vector containing the names of the generated features (if d > 0), or simply an empty vector (if d = 0)

time\_var The name of the time variable in pdata

unit\_var The name of the unit variable in pdata

**treatment** The name of the treatment variable in pdata

response The name of the response variable in pdata

**coefs** The coefficient vector  $\beta$  used for data generation.

first inds A vector of indices indicating the first treatment effect for each treated cohort.

**N\_UNTREATED** The number of never-treated units.

**assignments** A vector of counts (of length R+1) indicating how many units fall into the nevertreated group and each of the R treated cohorts.

indep\_counts Independent cohort assignments (for auxiliary purposes).

- **p** The number of columns in the design matrix X.
- N Number of units.
- T Number of time periods.
- R Number of treated cohorts.
- **d** Number of covariates.

sig\_eps\_sq The idiosyncratic noise variance.

sig\_eps\_c\_sq The unit-level noise variance.

#### References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv* preprint arXiv:2312.05985. https://arxiv.org/abs/2312.05985.

```
## Not run:
 # Set simulation parameters
 N <- 100 # Number of units in the panel
 T <- 5
                   # Number of time periods
 R <- 3
                   # Number of treated cohorts
 d <- 2
                   # Number of time-invariant covariates
 sig_eps_sq <- 1  # Variance of observation-level noise</pre>
 sig_eps_c_sq <- 0.5 # Variance of unit-level random effects</pre>
 # Generate coefficient vector using genCoefsCore()
  # (Here, density controls sparsity and eff_size scales nonzero entries)
 coefs_core <- genCoefsCore(R = R, T = T, d = d, density = 0.2, eff_size = 2, seed = 123)</pre>
 # Now simulate the data. Setting gen_ints = TRUE generates the full design
 matrix with interactions.
```

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```
sim_data <- simulateDataCore(
   N = N,
   T = T,
   R = R,
   d = d,
   sig_eps_sq = sig_eps_sq,
   sig_eps_c_sq = sig_eps_c_sq,
   beta = coefs_core$beta,
   seed = 456,
   gen_ints = TRUE,
   distribution = "gaussian"
)

# Examine the returned list:
   str(sim_data)

## End(Not run)</pre>
```

twfeCovs

Two-way fixed effects with covariates and separate treatment effects for each cohort

## **Description**

WARNING: This function should NOT be used for estimation. It is a biased estimator of treatment effects. Implementation of two-way fixed effects with covariates and separate treatment effects for each cohort. Estimates overall ATT as well as CATT (cohort average treatment effects on the treated units). It is implemented only for the sake of the simulation studies in Faletto (2025). This estimator is only unbiased under the assumptions that treatment effects are homogeneous across covariates and are identical within cohorts across all times since treatment.

## Usage

```
twfeCovs(
  pdata,
  time_var,
  unit_var,
  treatment,
  response,
  covs = c(),
  indep_counts = NA,
  sig_eps_sq = NA,
  sig_eps_c_sq = NA,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)
```

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#### **Arguments**

pdata Dataframe; the panel data set. Each row should represent an observation of a

unit at a time. Should contain columns as described below.

time\_var Character; the name of a single column containing a variable for the time period.
This column is expected to contain integer values (for example, years). Recom-

mended encodings for dates include format YYYY, YYYYMM, or YYYYM-

MDD, whichever is appropriate for your data.

unit\_var Character; the name of a single column containing a variable for each unit. This

column is expected to contain character values (i.e. the "name" of each unit).

Character; the name of a single column containing a variable for the treatment dummy indicator. This column is expected to contain integer values, and in particular, should equal 0 if the unit was untreated at that time and 1 otherwise. Treatment should be an absorbing state; that is, if unit i is treated at time t, then it must also be treated at all times t + 1, ..., T. Any units treated in the first time period will be removed automatically. Please make sure yourself that at least

some units remain untreated at the final time period ("never-treated units").

Character; the name of a single column containing the response for each unit at each time. The response must be an integer or numeric value.

(Optional.) Character; a vector containing the names of the columns for covariates. All of these columns are expected to contain integer, numeric, or factor values, and any categorical values will be automatically encoded as binary indicators. If no covariates are provided, the treatment effect estimation will proceed, but it will only be valid under unconditional versions of the parallel trends

and no anticipation assumptions. Default is c().

(Optional.) Integer; a vector. If you have a sufficiently large number of units, you can optionally randomly split your data set in half (with N units in each data set). The data for half of the units should go in the pdata argument provided above. For the other N units, simply provide the counts for how many units appear in the untreated cohort plus each of the other R cohorts in this argument indep\_counts. The benefit of doing this is that the standard error for the average treatment effect will be (asymptotically) exact instead of conservative. The length of indep\_counts must equal 1 plus the number of treated cohorts in pdata. All entries of indep\_counts must be strictly positive (if you are concerned that this might not work out, maybe your data set is on the small side and it's best to just leave your full data set in pdata). The sum of all the counts in indep\_counts must match the total number of units in pdata. Default is NA

(Optional.) Numeric; the variance of the row-level IID noise assumed to apply to each observation. See Section 2 of Faletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.

(in which case conservative standard errors will be calculated if q < 1.)

(Optional.) Numeric; the variance of the unit-level IID noise (random effects) assumed to apply to each observation. See Section 2 of Faletto (2025) for details. It is best to provide this variance if it is known (for example, if you are using

sig\_eps\_sq

sig\_eps\_c\_sq

treatment

response

covs

indep\_counts

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	simulated data). If this variance is unknown, this argument can be omitted, and the variance will be estimated using the estimator from Pesaran (2015, Section 26.5.1) with ridge regression. Default is NA.
verbose	Logical; if TRUE, more details on the progress of the function will be printed as the function executes. Default is FALSE.
alpha	Numeric; function will calculate (1 - alpha) confidence intervals for the cohort average treatment effects that will be returned in catt_df.
add_ridge	(Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the (untransformed) coefficients to stabilize estimation. Default is FALSE.

# Value

A named list with the following elements:

att_hat	The estimated overall average treatment effect for a randomly selected treated unit.
att_se	A standard error for the ATT. If the Gram matrix is not invertible, this will be NA.
catt_hats	A named vector containing the estimated average treatment effects for each cohort.
catt_ses	A named vector containing the (asymptotically exact) standard errors for the estimated average treatment effects within each cohort.
cohort_probs	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating att_hat. If indep_counts was provided, cohort_probs was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in pdata.
catt_df	A dataframe displaying the cohort names, average treatment effects, standard errors, and 1 – alpha confidence interval bounds.
beta_hat	The full vector of estimated coefficients.
treat_inds	The indices of beta_hat corresponding to the treatment effects for each cohort at each time.
treat_int_inds	The indices of beta_hat corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
sig_eps_sq	Either the provided sig_eps_sq or the estimated one, if a value wasn't provided.
sig_eps_c_sq	Either the provided sig_eps_c_sq or the estimated one, if a value wasn't provided.
X_ints	The design matrix created containing all interactions, time and cohort dummies,
	etc.
У	etc.  The vector of responses, containing nrow(X_ints) entries.
y X_final	

N	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
Т	The number of time periods in the final data set.
R	The final number of treated cohorts that appear in the final data set.
d	The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).
p	The final number of columns in the full set of covariates used to estimate the model.

#### Author(s)

Gregory Faletto

#### References

Faletto, G (2025). Fused Extended Two-Way Fixed Effects for Difference-in-Differences with Staggered Adoptions. *arXiv preprint arXiv:2312.05985*. https://arxiv.org/abs/2312.05985.

twfeCovsWithSimulatedData

Run twfeCovs on Simulated Data

# Description

This function runs the bridge-penalized extended two-way fixed effects estimator (twfeCovs()) on simulated data. It is simply a wrapper for twfeCovs(): it accepts an object of class "FETWFE\_simulated" (produced by simulateData()) and unpacks the necessary components to pass to twfeCovs(). So the outputs match twfeCovs(), and the needed inputs match their counterparts in twfeCovs().

#### Usage

```
twfeCovsWithSimulatedData(
  simulated_obj,
  verbose = FALSE,
  alpha = 0.05,
  add_ridge = FALSE
)
```

## **Arguments**

simulated\_obj An object of class "FETWFE\_simulated" containing the simulated panel data

and design matrix.

verbose Logical; if TRUE, more details on the progress of the function will be printed as

the function executes. Default is FALSE.

alpha Numeric; function will of	alculate (1 - alpha	a) confidence intervals for the cohort
---------------------------------	---------------------	--

average treatment effects that will be returned in catt\_df.

add\_ridge (Optional.) Logical; if TRUE, adds a small amount of ridge regularization to the

(untransformed) coefficients to stabilize estimation. Default is FALSE.

# Value

A named list with the following elements:

att_hat	The estimated overall average treatment effect for a randomly selected treated unit.
att_se	If $q < 1$ , a standard error for the ATT. If indep_counts was provided, this standard error is asymptotically exact; if not, it is asymptotically conservative. If $q >= 1$ , this will be NA.
catt_hats	A named vector containing the estimated average treatment effects for each cohort.
catt_ses	If $q < 1$ , a named vector containing the (asymptotically exact, non-conservative) standard errors for the estimated average treatment effects within each cohort.
cohort_probs	A vector of the estimated probabilities of being in each cohort conditional on being treated, which was used in calculating att_hat. If indep_counts was provided, cohort_probs was calculated from that; otherwise, it was calculated from the counts of units in each treated cohort in pdata.
catt_df	A dataframe displaying the cohort names, average treatment effects, standard errors, and 1 – alpha confidence interval bounds.
beta_hat	The full vector of estimated coefficients.
treat_inds	The indices of beta_hat corresponding to the treatment effects for each cohort at each time.
treat_int_inds	The indices of beta_hat corresponding to the interactions between the treatment effects for each cohort at each time and the covariates.
sig_eps_sq	Either the provided sig_eps_sq or the estimated one, if a value wasn't provided.
sig_eps_c_sq	Either the provided sig_eps_c_sq or the estimated one, if a value wasn't provided.
X_ints	The design matrix created containing all interactions, time and cohort dummies, etc.
У	The vector of responses, containing nrow(X_ints) entries.
X_final	The design matrix after applying the change in coordinates to fit the model and also multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
y_final	The final response after multiplying on the left by the square root inverse of the estimated covariance matrix for each unit.
N	The final number of units that were in the data set used for estimation (after any units may have been removed because they were treated in the first time period).
T	The number of time periods in the final data set.
R	The final number of treated cohorts that appear in the final data set.

d The final number of covariates that appear in the final data set (after any covariates may have been removed because they contained missing values or all contained the same value for every unit).

p The final number of columns in the full set of covariates used to estimate the model.

```
## Not run:
    # Generate coefficients
    coefs <- genCoefs(R = 5, T = 30, d = 12, density = 0.1, eff_size = 2, seed = 123)

# Simulate data using the coefficients
    sim_data <- simulateData(coefs, N = 120, sig_eps_sq = 5, sig_eps_c_sq = 5)

    result <- twfeCovsWithSimulatedData(sim_data)

## End(Not run)</pre>
```

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