

# Package ‘lrstat’

May 11, 2024

**Type** Package

**Title** Power and Sample Size Calculation for Non-Proportional Hazards and Beyond

**Version** 0.2.6

**Date** 2024-05-08

**Description** Performs power and sample size calculation for non-proportional hazards model using the Fleming-Harrington family of weighted log-rank tests. The sequentially calculated log-rank test score statistics are assumed to have independent increments as characterized in Anastasios A. Tsiatis (1982) <[doi:10.1080/01621459.1982.10477898](https://doi.org/10.1080/01621459.1982.10477898)>. The mean and variance of log-rank test score statistics are calculated based on Kaifeng Lu (2021) <[doi:10.1002/pst.2069](https://doi.org/10.1002/pst.2069)>. The boundary crossing probabilities are calculated using the recursive integration algorithm described in Christopher Jennison and Bruce W. Turnbull (2000, ISBN:0849303168). The package can also be used for continuous, binary, and count data. For continuous data, it can handle missing data through mixed-model for repeated measures (MMRM). In crossover designs, it can estimate direct treatment effects while accounting for carryover effects. For binary data, it can design Simon's 2-stage, modified toxicity probability-2 (mTPI-2), and Bayesian optimal interval (BOIN) trials. For count data, it can design group sequential trials for negative binomial endpoints with censoring. Additionally, it facilitates group sequential equivalence trials for all supported data types. Moreover, it can design adaptive group sequential trials for changes in sample size, error spending function, number and spacing of future looks. Finally, it offers various options for adjusted p-values, including graphical and gatekeeping procedures.

**License** GPL (>= 2)

**Imports** Rcpp (>= 1.0.9), mvtnorm (>= 1.1-3), lpSolve (>= 5.6.1), shiny (>= 1.7.1)

**LinkingTo** Rcpp

**Suggests** knitr, rmarkdown, testthat (>= 3.0.0), dplyr, tidyr, survival

**VignetteBuilder** knitr

**RoxygenNote** 7.3.1

**Encoding** UTF-8

**NeedsCompilation** yes

**Depends** R (>= 2.10)

**LazyData** true

**Author** Kaifeng Lu [aut, cre] (<<https://orcid.org/0000-0002-6160-7119>>)

**Maintainer** Kaifeng Lu <kaifenglu@gmail.com>

**Repository** CRAN

**Date/Publication** 2024-05-11 11:53:04 UTC

## R topics documented:

accrual . . . . .	5
adaptDesign . . . . .	6
BOINTable . . . . .	10
caltime . . . . .	12
ClopperPearsonCI . . . . .	13
covrmst . . . . .	14
errorSpent . . . . .	16
exitprob . . . . .	17
fadjpbon . . . . .	18
fadjpdun . . . . .	19
fadjpsim . . . . .	20
fmodmix . . . . .	21
fquantile . . . . .	22
fseqbon . . . . .	23
fstdmix . . . . .	25
fstp2seq . . . . .	26
ftrunc . . . . .	27
fwgtmat . . . . .	28
getAccrualDurationFromN . . . . .	29
getADCI . . . . .	30
getADRCI . . . . .	33
getBound . . . . .	37
getCI . . . . .	38
getCP . . . . .	40
getDesign . . . . .	44
getDesignAgreement . . . . .	48
getDesignANOVA . . . . .	50
getDesignANOVAContrast . . . . .	52
getDesignEquiv . . . . .	53
getDesignFisherExact . . . . .	58
getDesignLogistic . . . . .	60
getDesignMeanDiff . . . . .	63
getDesignMeanDiffCarryover . . . . .	66
getDesignMeanDiffEquiv . . . . .	70
getDesignMeanDiffMMRM . . . . .	73
getDesignMeanDiffXO . . . . .	78
getDesignMeanDiffXOEquiv . . . . .	81
getDesignMeanRatio . . . . .	84

getDesignMeanRatioEquiv . . . . .	88
getDesignMeanRatioXO . . . . .	91
getDesignMeanRatioXOEquiv . . . . .	94
getDesignOddsRatio . . . . .	97
getDesignOddsRatioEquiv . . . . .	101
getDesignOneMean . . . . .	104
getDesignOneMultinom . . . . .	107
getDesignOneProportion . . . . .	109
getDesignOneRateExact . . . . .	112
getDesignOneSlope . . . . .	114
getDesignOrderedBinom . . . . .	117
getDesignPairedMeanDiff . . . . .	119
getDesignPairedMeanDiffEquiv . . . . .	122
getDesignPairedMeanRatio . . . . .	125
getDesignPairedMeanRatioEquiv . . . . .	129
getDesignPairedPropMcNemar . . . . .	131
getDesignRepeatedANOVA . . . . .	135
getDesignRepeatedANOVAContrast . . . . .	137
getDesignRiskDiff . . . . .	138
getDesignRiskDiffEquiv . . . . .	142
getDesignRiskDiffExact . . . . .	145
getDesignRiskDiffExactEquiv . . . . .	146
getDesignRiskRatio . . . . .	148
getDesignRiskRatioEquiv . . . . .	151
getDesignRiskRatioExact . . . . .	154
getDesignRiskRatioExactEquiv . . . . .	156
getDesignRiskRatioFM . . . . .	157
getDesignSlopeDiff . . . . .	161
getDesignSlopeDiffMMRM . . . . .	165
getDesignTwoMultinom . . . . .	170
getDesignTwoOrdinal . . . . .	172
getDesignTwoWayANOVA . . . . .	173
getDesignUnorderedBinom . . . . .	175
getDesignUnorderedMultinom . . . . .	176
getDesignWilcoxon . . . . .	177
getDurationFromNevents . . . . .	181
getNeventsFromHazardRatio . . . . .	183
getRCI . . . . .	185
hedgesg . . . . .	187
kmdiff . . . . .	189
kmest . . . . .	191
kmpower . . . . .	192
kmpower1s . . . . .	196
kmpowerequiv . . . . .	200
kmsamplesize . . . . .	204
kmsamplesize1s . . . . .	208
kmsamplesizeequiv . . . . .	211
kmstat . . . . .	214

lpower	216
lpowerequiv	221
lrsamplesize	225
lrsamplesizeequiv	229
lrsim	232
lrsim2e	237
lrsim2e3a	241
lrsim3a	246
lrstat	250
lrtest	253
mnOddsRatioCI	254
mnRateDiffCI	256
mnRateRatioCI	257
mnRiskDiffCI	258
mnRiskRatioCI	259
mTPI2Table	261
nbpower	262
nbpower1s	267
nbpowerequiv	271
nbsamplesize	276
nbsamplesize1s	280
nbsamplesizeequiv	283
nbstat	286
ptpwexp	291
pwexpcuts	292
pwexploglik	293
qtpwexp	294
rawdata	295
remlOddsRatio	295
remlRateDiff	296
remlRateRatio	297
remlRiskDiff	298
remlRiskRatio	299
repeatedPValue	300
riskDiffExactCI	301
riskDiffExactPValue	302
riskRatioExactCI	303
riskRatioExactPValue	304
rmdiff	305
rmest	307
rmpower	308
rmpower1s	313
rmpowerequiv	316
rmsamplesize	320
rmsamplesize1s	324
rmsamplesizeequiv	328
rmst	330
rmstat	331

rtpwexp . . . . .	334
runShinyApp . . . . .	335
simon2stage . . . . .	335
survQuantile . . . . .	336
updateGraph . . . . .	338
zstatOddsRatio . . . . .	339
zstatRateDiff . . . . .	340
zstatRateRatio . . . . .	341
zstatRiskDiff . . . . .	342
zstatRiskRatio . . . . .	343

<b>Index</b>	<b>344</b>
--------------	------------

---

accrual	<i>Number of enrolled subjects</i>
---------	------------------------------------

---

### Description

Obtains the number of subjects enrolled by given calendar times.

### Usage

```
accrual(
  time = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  accrualDuration = NA_real_
)
```

### Arguments

time	A vector of calendar times at which to calculate the number of enrolled subjects.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., <code>c(0, 3)</code> breaks the time axis into 2 accrual intervals: <code>[0, 3)</code> and <code>[3, Inf)</code> .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
accrualDuration	Duration of the enrollment period.

### Value

A vector of total number of subjects enrolled by the specified calendar times.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: Uniform enrollment with 20 patients per month for 12 months.
```

```
accrual(time = 3, accrualTime = 0, accrualIntensity = 20,
        accrualDuration = 12)
```

```
# Example 2: Piecewise accrual, 10 patients per month for the first
# 3 months, and 20 patients per month thereafter. Patient recruitment
# ends at 12 months for the study.
```

```
accrual(time = c(2, 9), accrualTime = c(0, 3),
        accrualIntensity = c(10, 20), accrualDuration = 12)
```

---

 adaptDesign

*Adaptive design at an interim look*


---

**Description**

Obtains the conditional power for specified incremental information given the interim results, parameter value, and data-dependent changes in the error spending function, and the number and spacing of interim looks. Conversely, obtains the incremental information needed to attain a specified conditional power given the interim results, parameter value, and data-dependent changes in the error spending function, and the number and spacing of interim looks.

**Usage**

```
adaptDesign(
  betaNew = NA_real_,
  INew = NA_real_,
  L = NA_integer_,
  zL = NA_real_,
  theta = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
```

```

    spendingTime = NA_real_,
    MullerSchafer = 0L,
    kNew = NA_integer_,
    informationRatesNew = NA_real_,
    efficacyStoppingNew = NA_integer_,
    futilityStoppingNew = NA_integer_,
    typeAlphaSpendingNew = "sfOF",
    parameterAlphaSpendingNew = NA_real_,
    typeBetaSpendingNew = "none",
    parameterBetaSpendingNew = NA_real_,
    userBetaSpendingNew = NA_real_,
    spendingTimeNew = NA_real_,
    varianceRatio = 1
  )

```

### Arguments

betaNew	The type II error for the secondary trial.
INew	The maximum information of the secondary trial. Either betaNew or INew should be provided while the other one should be missing.
L	The interim adaptation look of the primary trial.
zL	The z-test statistic at the interim adaptation look of the primary trial.
theta	The parameter value.
IMax	The maximum information of the primary trial. Must be provided if futilityBounds is missing and typeBetaSpending is not equal to "none", or if conditional power calculation is desired.
kMax	The maximum number of stages of the primary trial.
informationRates	The information rates of the primary trial.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.
alpha	The significance level of the primary trial. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending	The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending for the primary trial. Cumulative alpha spent up to each stage.
futilityBounds	The lower boundaries on the z-test statistic scale for futility stopping for the primary trial. Defaults to $\text{rep}(-6, k_{\text{Max}}-1)$ if left unspecified.
typeBetaSpending	The type of beta spending for the primary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value of beta spending for the primary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".
spendingTime	The error spending time of the primary trial. Defaults to missing, in which case, it is the same as informationRates.
MullerSchafer	Whether to use the Muller and Schafer (2001) method for trial adaptation.
kNew	The number of looks of the secondary trial.
informationRatesNew	The spacing of looks of the secondary trial.
efficacyStoppingNew	The indicators of whether efficacy stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.
futilityStoppingNew	The indicators of whether futility stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.
typeAlphaSpendingNew	The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpendingNew	The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
typeBetaSpendingNew	The type of beta spending for the secondary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".



parameterBetaSpendingNew	The parameter value of beta spending for the secondary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpendingNew	The user defined cumulative beta spending. Cumulative beta spent up to each stage of the secondary trial.
spendingTimeNew	The error spending time of the secondary trial. Defaults to missing, in which case, it is the same as informationRatesNew.
varianceRatio	The ratio of the variance under H0 to the variance under H1.

### Value

An adaptDesign object with two list components:

- primaryTrial: A list of selected information for the primary trial, including L, zL, theta, kMax, informationRates, efficacyBounds, futilityBounds, and MullerSchafer.
- secondaryTrial: A design object for the secondary trial.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### References

Lu Chi, H. M. James Hung, and Sue-Jane Wang. Modification of sample size in group sequential clinical trials. *Biometrics* 1999;55:853-857.

Hans-Helge Muller and Helmut Schafer. Adaptive group sequential designs for clinical trials: Combining the advantages of adaptive and of classical group sequential approaches. *Biometrics* 2001;57:886-891.

### See Also

[getDesign](#)

### Examples

```
# original group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4))

# interim look results
L = 1
n1 = n/3
delta1 = 4.5
```

```

sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

t = des1$byStageResults$informationRates

# conditional power with sample size increase
(des2 = adaptDesign(
  betaNew = NA, INew = 420/(4*sigma1^2),
  L, zL, theta = delta1,
  IMax = n/(4*sigma1^2), kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4))

# Muller & Schafer (2001) method to design the secondary trial:
# 3-look gamma(-2) spending with 84% power at delta = 4.5 and sigma = 20
(des2 = adaptDesign(
  betaNew = 0.16, INew = NA,
  L, zL, theta = delta1,
  IMax = n/(4*sigma1^2), kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2))

# incremental sample size for sigma = 20
(nNew = 4*sigma1^2*des2$secondaryTrial$overallResults$information)

```

---

BOINTable

*BOIN decision table*


---

## Description

Obtains the decision table for the Bayesian optimal interval (BOIN) design.

## Usage

```

BOINTable(
  nMax = NA_integer_,
  pT = 0.3,
  phi1 = 0.6 * pT,
  phi2 = 1.4 * pT,
  a = 1,
  b = 1,
  pExcessTox = 0.95
)

```

**Arguments**

nMax	The maximum number of subjects in a dose cohort.
pT	The target toxicity probability. Defaults to 0.3.
phi1	The lower equivalence limit for target toxicity probability.
phi2	The upper equivalence limit for target toxicity probability.
a	The prior toxicity parameter for the beta prior.
b	The prior non-toxicity parameter for the beta prior.
pExcessTox	The threshold for excessive toxicity, i.e., if $\text{Prob}(p > pT \mid \text{Data}) > \text{pExcessTox}$ , then the current and all higher doses will be excluded and never be used again in the remainder of the trial to avoid any other subjects receiving treatment at those doses. Defaults to 0.95.

**Value**

An S3 class BOINTable object with the following components:

- settings: The input settings data frame with the following variables:
  - nMax: The maximum number of subjects in a dose cohort.
  - pT: The target toxicity probability.
  - phi1: The lower equivalence limit for target toxicity probability.
  - phi2: The upper equivalence limit for target toxicity probability.
  - lambda1: The lower decision boundary for observed toxicity probability.
  - lambda2: The upper decision boundary for observed toxicity probability.
  - a: The prior toxicity parameter for the beta prior.
  - b: The prior non-toxicity parameter for the beta prior.
  - pExcessTox: The threshold for excessive toxicity.
- decisionDataFrame: The decision data frame for the BOIN design. It includes the following variables:
  - n: The sample size.
  - y: The number of toxicities.
  - decision: The dosing decision.
- decisionMatrix: The decision matrix corresponding to the decision data frame.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
BOINTable(nMax = 18, pT = 0.3, phi = 0.6*0.3, phi2 = 1.4*0.3)
```

---

caltime *Calendar times for target number of events*

---

### Description

Obtains the calendar times needed to reach the target number of subjects experiencing an event.

### Usage

```
caltime(
  nevents = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L
)
```

### Arguments

nevents	A vector of target number of events.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

**Value**

A vector of calendar times expected to yield the target number of events.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.
```

```
caltime(nevents = c(24, 80), allocationRatioPlanned = 1,
        accrualTime = seq(0, 8),
        accrualIntensity = 26/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        stratumFraction = c(0.2, 0.8),
        lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
        lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12,
        accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

---

ClopperPearsonCI

*Clopper-Pearson confidence interval for one-sample proportion*

---

**Description**

Obtains the Clopper-Pearson exact confidence interval for a one-sample proportion.

**Usage**

```
ClopperPearsonCI(n, y, cilevel = 0.95)
```

**Arguments**

n	The sample size.
y	The number of responses.
cilevel	The confidence interval level.

**Value**

A data frame with the following variables:

- n: The sample size.
- y: The number of responses.
- phat: The observed proportion of responses.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
ClopperPearsonCI(20, 3)
```

---

covrmst

*Covariance between restricted mean survival times*

---

**Description**

Obtains the covariance between restricted mean survival times at two different time points.

**Usage**

```
covrmst(  
  t2 = NA_real_,  
  tau1 = NA_real_,  
  tau2 = NA_real_,  
  allocationRatioPlanned = 1,  
  accrualTime = 0L,  
  accrualIntensity = NA_real_,  
  piecewiseSurvivalTime = 0L,  
  lambda1 = NA_real_,  
  lambda2 = NA_real_,  
  gamma1 = 0L,
```

```

    gamma2 = 0L,
    accrualDuration = NA_real_,
    maxFollowupTime = NA_real_
  )

```

### Arguments

t2	The calendar time for analysis 2.
tau1	The milestone time for analysis 1.
tau2	The milestone time for analysis 2.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
lambda1	A vector of hazard rates for the event for the active treatment group. One for each analysis time interval.
lambda2	A vector of hazard rates for the event for the control group. One for each analysis time interval.
gamma1	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
gamma2	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group.
accrualDuration	Duration of the enrollment period.
maxFollowupTime	Follow-up time for the first enrolled subject. For fixed followup, $\text{maxFollowupTime} = \text{minFollowupTime}$ . For variable followup, $\text{maxFollowupTime} = \text{accrualDuration} + \text{minFollowupTime}$ .

### Value

The covariance between the restricted mean survival times for each treatment group.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
covrmst(t2 = 25, tau1 = 16, tau2 = 18, allocationRatioPlanned = 1,
        accrualTime = c(0, 3), accrualIntensity = c(10, 20),
        piecewiseSurvivalTime = c(0, 6),
        lambda1 = c(0.0533, 0.0309), lambda2 = c(0.0533, 0.0533),
        gamma1 = -log(1-0.05)/12, gamma2 = -log(1-0.05)/12,
        accrualDuration = 12, maxFollowupTime = 30)
```

---

errorSpent	<i>Error spending</i>
------------	-----------------------

---

**Description**

Obtains the error spent at given spending times for the specified error spending function.

**Usage**

```
errorSpent(t, error, sf = "sfOF", sfpar = NA)
```

**Arguments**

t	A vector of spending times, typically equal to information fractions.
error	The total error to spend.
sf	The spending function. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, and "sfHSD" for Hwang, Shi & DeCani spending function. Defaults to "sfOF".
sfpar	The parameter for the spending function. Corresponds to rho for "sfKD" and gamma for "sfHSD".

**Value**

A vector of errors spent up to the interim look.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
errorSpent(t = 0.5, error = 0.025, sf = "sfOF")
errorSpent(t = c(0.5, 0.75, 1), error = 0.025, sf = "sfHSD", sfpar = -4)
```



---

exitprob                      *Stagewise exit probabilities*

---

**Description**

Obtains the stagewise exit probabilities for both efficacy and futility stopping.

**Usage**

```
exitprob(b, a = NA, theta = 0, I = NA)
```

**Arguments**

b	Upper boundaries on the z-test statistic scale.
a	Lower boundaries on the z-test statistic scale. Defaults to $c(\text{rep}(-6.0, \text{kMax}-1), \text{b}[\text{kMax}])$ if left unspecified, where $\text{kMax} = \text{length}(\text{b})$ .
theta	Stagewise parameter of interest, e.g., $-U/V$ for weighted log-rank test, where $U$ is the mean and $V$ is the variance of the weighted log-rank test score statistic at each stage. For proportional hazards and conventional log-rank test, use the scalar input, $\text{theta} = -\log(\text{HR})$ . Defaults to 0 corresponding to the null hypothesis.
I	Stagewise cumulative information, e.g., $V$ , the variance of the weighted log-rank test score statistic at each stage. For conventional log-rank test, information can be approximated by $\text{phi} \cdot (1-\text{phi}) \cdot D$ , where $\text{phi}$ is the probability of being allocated to the active arm, and $D$ is the total number of events at each stage. Defaults to $\text{seq}(1, \text{kMax})$ if left unspecified.

**Value**

A list of stagewise exit probabilities:

- `exitProbUpper`: The vector of efficacy stopping probabilities
- `exitProbLower`: The vector of futility stopping probabilities.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
exitprob(b = c(3.471, 2.454, 2.004), theta = -log(0.6),
         I = c(50, 100, 150)/4)
```

```
exitprob(b = c(2.963, 2.359, 2.014),
         a = c(-0.264, 0.599, 2.014),
         theta = c(0.141, 0.204, 0.289),
         I = c(81, 121, 160))
```

---

`fadjpbon`*Adjusted p-values for Bonferroni-based graphical approaches*

---

**Description**

Obtains the adjusted p-values for graphical approaches using weighted Bonferroni tests.

**Usage**

```
fadjpbon(w, G, p)
```

**Arguments**

<code>w</code>	The vector of initial weights for elementary hypotheses.
<code>G</code>	The initial transition matrix.
<code>p</code>	The raw p-values for elementary hypotheses.

**Value**

A matrix of adjusted p-values.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

Frank Bretz, Willi Maurer, Werner Brannath and Martin Posch. A graphical approach to sequentially rejective multiple test procedures. *Statistics in Medicine*. 2009; 28:586-604.

**Examples**

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                 nrow=2, ncol=4, byrow=TRUE)
w <- c(0.5,0.5,0,0)
g <- matrix(c(0,0,1,0,0,0,0,1,0,1,0,0,1,0,0,0),
           nrow=4, ncol=4, byrow=TRUE)
fadjpbon(w, g, pvalues)
```

---

fadjpdun	<i>Adjusted p-values for Dunnett-based graphical approaches</i>
----------	---

---

**Description**

Obtains the adjusted p-values for graphical approaches using weighted Dunnett tests.

**Usage**

```
fadjpdun(wgtmat, p, family = NULL, corr = NULL)
```

**Arguments**

wgtmat	The weight matrix for intersection hypotheses.
p	The raw p-values for elementary hypotheses.
family	The matrix of family indicators for elementary hypotheses.
corr	The correlation matrix that should be used for the parametric test. Can contain NAs for unknown correlations between families.

**Value**

A matrix of adjusted p-values.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

Frank Bretz, Martin Posch, Ekkehard Glimm, Florian Klinglmueller, Willi Maurer, and Kornelius Rohmeyer. Graphical approach for multiple comparison procedures using weighted Bonferroni, Simes, or parameter tests. *Biometrical Journal*. 2011; 53:894-913.

**Examples**

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                 nrow=2, ncol=4, byrow=TRUE)
w <- c(0.5,0.5,0,0)
g <- matrix(c(0,0,1,0,0,0,0,1,0,1,0,0,1,0,0,0),
           nrow=4, ncol=4, byrow=TRUE)
wgtmat = fwgtmat(w,g)

family = matrix(c(1,1,0,0,0,0,1,1), nrow=2, ncol=4, byrow=TRUE)
corr = matrix(c(1,0.5,NA,NA, 0.5,1,NA,NA,
              NA,NA,1,0.5, NA,NA,0.5,1),
             nrow = 4, byrow = TRUE)
fadjpdun(wgtmat, pvalues, family, corr)
```

---

`fadjpsim`*Adjusted p-values for Simes-based graphical approaches*

---

**Description**

Obtains the adjusted p-values for graphical approaches using weighted Simes tests.

**Usage**

```
fadjpsim(wgtmat, p, family = NULL)
```

**Arguments**

<code>wgtmat</code>	The weight matrix for intersection hypotheses.
<code>p</code>	The raw p-values for elementary hypotheses.
<code>family</code>	The matrix of family indicators for elementary hypotheses.

**Value**

A matrix of adjusted p-values.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

Frank Bretz, Martin Posch, Ekkehard Glimm, Florian Klinglmueller, Willi Maurer, and Kornelius Rohmeyer. Graphical approach for multiple comparison procedures using weighted Bonferroni, Simes, or parameter tests. *Biometrical Journal*. 2011; 53:894-913.

Kaifeng Lu. Graphical approaches using a Bonferroni mixture of weighted Simes tests. *Statistics in Medicine*. 2016; 35:4041-4055.

**Examples**

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                 nrow=2, ncol=4, byrow=TRUE)
w <- c(0.5,0.5,0,0)
g <- matrix(c(0,0,1,0,0,0,0,1,0,1,0,0,1,0,0,0),
           nrow=4, ncol=4, byrow=TRUE)
wgtmat = fwgtmat(w,g)

family = matrix(c(1,1,0,0,0,0,1,1), nrow=2, ncol=4, byrow=TRUE)
fadjpsim(wgtmat, pvalues, family)
```

---

`fmodmix`*Adjusted p-values for modified mixture gatekeeping procedures*

---

**Description**

Obtains the adjusted p-values for the modified gatekeeping procedures for multiplicity problems involving serial and parallel logical restrictions.

**Usage**

```
fmodmix(  
  p,  
  family = NULL,  
  serial,  
  parallel,  
  gamma,  
  test = "hommel",  
  exhaust = 1  
)
```

**Arguments**

<code>p</code>	The raw p-values for elementary hypotheses.
<code>family</code>	The matrix of family indicators for the hypotheses.
<code>serial</code>	The matrix of serial rejection set for the hypotheses.
<code>parallel</code>	The matrix of parallel rejection set for the hypotheses.
<code>gamma</code>	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
<code>test</code>	The component multiple testing procedure. Options include "holm", "hochberg", or "hommel". Defaults to "hommel".
<code>exhaust</code>	Whether to use alpha-exhausting component testing procedure for the last family with active hypotheses. It defaults to TRUE.

**Value**

A matrix of adjusted p-values.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

## References

Alex Dmitrienko, George Kordzakhia, and Thomas Brechenmacher. Mixture-based gatekeeping procedures for multiplicity problems with multiple sequences of hypotheses. *Journal of Biopharmaceutical Statistics*. 2016; 26(4):758–780.

George Kordzakhia, Thomas Brechenmacher, Eiji Ishida, Alex Dmitrienko, Winston Wenxiang Zheng, and David Fuyuan Li. An enhanced mixture method for constructing gatekeeping procedures in clinical trials. *Journal of Biopharmaceutical Statistics*. 2018; 28(1):113–128.

## Examples

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
family = matrix(c(1, 1, 0, 0, 0, 0, 0, 0,
                 0, 0, 1, 1, 0, 0, 0, 0,
                 0, 0, 0, 0, 1, 1, 0, 0,
                 0, 0, 0, 0, 0, 0, 1, 1),
               nrow=4, byrow=TRUE)

serial = matrix(c(0, 0, 0, 0, 0, 0, 0, 0,
                 0, 0, 0, 0, 0, 0, 0, 0,
                 1, 0, 0, 0, 0, 0, 0, 0,
                 0, 1, 0, 0, 0, 0, 0, 0,
                 0, 0, 1, 0, 0, 0, 0, 0,
                 0, 0, 0, 1, 0, 0, 0, 0,
                 0, 0, 0, 0, 1, 0, 0, 0,
                 0, 0, 0, 0, 0, 1, 0, 0),
               nrow=8, byrow=TRUE)

parallel = matrix(0, 8, 8)
gamma = c(0.6, 0.6, 0.6, 1)
fmodmix(p, family, serial, parallel, gamma, test = "hommel", exhaust = 1)
```

---

fquantile

*The quantiles of a survival distribution*

---

## Description

Obtains the quantiles of a survival distribution.

## Usage

```
fquantile(S, probs, ...)
```

## Arguments

S	The survival function of a univariate survival time.
probs	The numeric vector of probabilities.
...	Additional arguments to be passed to S.

**Value**

A vector of length(probs) for the quantiles.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
fquantile(pweibull, probs = c(0.25, 0.5, 0.75),
          shape = 1.37, scale = 1/0.818, lower.tail = FALSE)
```

---

fseqbon

*Group sequential trials using Bonferroni-based graphical approaches*

---

**Description**

Obtains the test results for group sequential trials using graphical approaches based on weighted Bonferroni tests.

**Usage**

```
fseqbon(
  w,
  G,
  alpha = 0.025,
  kMax,
  typeAlphaSpending = NULL,
  parameterAlphaSpending = NULL,
  incidenceMatrix = NULL,
  maxInformation = NULL,
  p,
  information,
  spendingTime = NULL
)
```

**Arguments**

w	The vector of initial weights for elementary hypotheses.
G	The initial transition matrix.
alpha	The significance level. Defaults to 0.025.
kMax	The maximum number of stages.

<code>typeAlphaSpending</code>	The vector of alpha spending functions. Each element is one of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF" if not provided.
<code>parameterAlphaSpending</code>	The vector of parameter values for the alpha spending functions. Each element corresponds to the value of Delta for "WT", rho for "sfKD", or gamma for "sfHSD". Defaults to missing if not provided.
<code>incidenceMatrix</code>	The incidence matrix indicating whether the specific hypothesis will be tested at the given look. The number of columns of <code>incidenceMatrix</code> must be equal to the maximum number of study looks ( <code>kMax</code> ). If not provided, defaults to testing each hypothesis at all study looks.
<code>maxInformation</code>	The vector of target maximum information for each hypothesis. Defaults to a vector of 1s if not provided.
<code>p</code>	The matrix of raw p-values for each hypothesis by study look.
<code>information</code>	The matrix of observed information for each hypothesis by study look.
<code>spendingTime</code>	The spending time for alpha spending by study look. If not provided, it is the same as <code>informationRates</code> calculated from <code>information</code> and <code>maxInformation</code> .

**Value**

A vector to indicate the first look the specific hypothesis is rejected (0 if the hypothesis is not rejected).

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

Willi Maurer and Frank Bretz. Multiple testing in group sequential trials using graphical approaches. *Statistics in Biopharmaceutical Research*. 2013; 5:311-320.

**Examples**

```
# Case study from Maurer & Bretz (2013)

fseqbon(
  w = c(0.5, 0.5, 0, 0),
  G = matrix(c(0, 0.5, 0.5, 0, 0.5, 0, 0, 0.5,
              0, 1, 0, 0, 1, 0, 0, 0),
            nrow=4, ncol=4, byrow=TRUE),
  alpha = 0.025,
  kMax = 3,
```



```

typeAlphaSpending = rep("sfOF", 4),
maxInformation = rep(1, 4),
p = matrix(c(0.0062, 0.017, 0.009, 0.13,
            0.0002, 0.0035, 0.002, 0.06),
          nrow=4, ncol=2),
information = matrix(c(rep(1/3, 4), rep(2/3, 4)),
                    nrow=4, ncol=2))

```

fstdmix

*Adjusted p-values for standard mixture gatekeeping procedures***Description**

Obtains the adjusted p-values for the standard gatekeeping procedures for multiplicity problems involving serial and parallel logical restrictions.

**Usage**

```

fstdmix(
  p,
  family = NULL,
  serial,
  parallel,
  gamma,
  test = "hommel",
  exhaust = 1
)

```

**Arguments**

p	The raw p-values for elementary hypotheses.
family	The matrix of family indicators for the hypotheses.
serial	The matrix of serial rejection set for the hypotheses.
parallel	The matrix of parallel rejection set for the hypotheses.
gamma	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
test	The component multiple testing procedure. Options include "holm", "hochberg", or "hommel". Defaults to "hommel".
exhaust	Whether to use alpha-exhausting component testing procedure for the last family with active hypotheses. It defaults to TRUE.

**Value**

A matrix of adjusted p-values.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

Alex Dmitrienko and Ajit C Tamhane. Mixtures of multiple testing procedures for gatekeeping applications in clinical trials. *Statistics in Medicine*. 2011; 30(13):1473–1488.

**Examples**

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
family = matrix(c(1, 1, 0, 0, 0, 0, 0, 0, 0,
                 0, 0, 1, 1, 0, 0, 0, 0, 0,
                 0, 0, 0, 0, 1, 1, 0, 0, 0,
                 0, 0, 0, 0, 0, 0, 1, 1),
               nrow=4, byrow=TRUE)

serial = matrix(c(0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
                 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
                 1, 0, 0, 0, 0, 0, 0, 0, 0, 0,
                 0, 1, 0, 0, 0, 0, 0, 0, 0, 0,
                 0, 0, 1, 0, 0, 0, 0, 0, 0, 0,
                 0, 0, 0, 1, 0, 0, 0, 0, 0, 0,
                 0, 0, 0, 0, 1, 0, 0, 0, 0, 0,
                 0, 0, 0, 0, 0, 1, 0, 0, 0, 0),
               nrow=8, byrow=TRUE)

parallel = matrix(0, 8, 8)
gamma = c(0.6, 0.6, 0.6, 1)
fstdmix(p, family, serial, parallel, gamma, test = "hommel", exhaust = 0)
```

---

fstp2seq

---

*Adjusted p-values for stepwise testing procedures for two sequences*


---

**Description**

Obtains the adjusted p-values for the stepwise gatekeeping procedures for multiplicity problems involving two sequences of hypotheses.

**Usage**

```
fstp2seq(p, gamma, test = "hochberg", retest = TRUE)
```

**Arguments**

p	The raw p-values for elementary hypotheses.
gamma	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
test	The component multiple testing procedure. It is either "Holm" or "Hochberg", and it defaults to "Hochberg".
retest	Whether to allow retesting. It defaults to TRUE.

**Value**

A matrix of adjusted p-values.

**Author(s)**

Kaifeng Lu, <kweifenglu@gmail.com>

**Examples**

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
gamma = c(0.6, 0.6, 0.6, 1)
fstp2seq(p, gamma, test="hochberg", retest=1)
```

---

ftrunc

*Adjusted p-values for Holm, Hochberg, and Hommel procedures*


---

**Description**

Obtains the adjusted p-values for possibly truncated Holm, Hochberg, and Hommel procedures.

**Usage**

```
ftrunc(p, test = "hommel", gamma = 1)
```

**Arguments**

p	The raw p-values for elementary hypotheses.
test	The test to use, e.g., "holm", "hochberg", or "hommel" (default).
gamma	The value of the truncation parameter. Defaults to 1 for the regular Holm, Hochberg, or Hommel procedure.

**Value**

A matrix of adjusted p-values.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

Alex Dmitrienko, Ajit C. Tamhane, and Brian L. Wiens. General multistage gatekeeping procedures. *Biometrical Journal*. 2008; 5:667-677.

**Examples**

```
pvalues <- matrix(c(0.01,0.005,0.015,0.022, 0.02,0.015,0.010,0.023),
                 nrow=2, ncol=4, byrow=TRUE)
ftrunc(pvalues, "hochberg")
```

---

fwgtmat

*Weight matrix for all intersection hypotheses*


---

**Description**

Obtains the weight matrix for all intersection hypotheses.

**Usage**

```
fwgtmat(w = NA_real_, G = NA_real_)
```

**Arguments**

w                    The vector of weights for elementary hypotheses.  
G                    The transition matrix.

**Value**

The weight matrix starting with the global null hypothesis.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
w = c(0.5,0.5,0,0)
g = matrix(c(0,0,1,0, 0,0,0,1, 0,1,0,0, 1,0,0,0),
          nrow=4, ncol=4, byrow=TRUE)
(wgtmat = fwgtmat(w,g))
```

---

```
getAccrualDurationFromN
```

*Accrual duration to enroll target number of subjects*

---

**Description**

Obtains the accrual duration to enroll the target number of subjects.

**Usage**

```
getAccrualDurationFromN(  
  nsubjects = NA_real_,  
  accrualTime = 0L,  
  accrualIntensity = NA_real_  
)
```

**Arguments**

`nsubjects`        The vector of target number of subjects.

`accrualTime`      A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., `c(0, 3)` breaks the time axis into 2 accrual intervals: `[0, 3)` and `[3, Inf)`.

`accrualIntensity`    A vector of accrual intensities. One for each accrual time interval.

**Value**

A vector of accrual durations.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
getAccrualDurationFromN(nsubjects = c(20, 150), accrualTime = c(0, 3),  
  accrualIntensity = c(10, 20))
```

---

<code>getADCI</code>	<i>Confidence interval after adaptation</i>
----------------------	---

---

### Description

Obtains the p-value, median unbiased point estimate, and confidence interval after the end of an adaptive trial.

### Usage

```
getADCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.25,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_,
  L2 = NA_integer_,
  zL2 = NA_real_,
  INew = NA_real_,
  MullerSchafer = 0L,
  informationRatesNew = NA_real_,
  efficacyStoppingNew = NA_integer_,
  typeAlphaSpendingNew = "sfOF",
  parameterAlphaSpendingNew = NA_real_,
  spendingTimeNew = NA_real_
)
```

### Arguments

<code>L</code>	The interim adaptation look of the primary trial.
<code>zL</code>	The z-test statistic at the interim adaptation look of the primary trial.
<code>IMax</code>	The maximum information of the primary trial.
<code>kMax</code>	The maximum number of stages of the primary trial.
<code>informationRates</code>	The information rates of the primary trial.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
<code>criticalValues</code>	The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.

<code>alpha</code>	The significance level of the primary trial. Defaults to 0.025.
<code>typeAlphaSpending</code>	The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>spendingTime</code>	The error spending time of the primary trial. Defaults to missing, in which case, it is the same as <code>informationRates</code> .
<code>L2</code>	The termination look of the secondary trial.
<code>zL2</code>	The z-test statistic at the termination look of the secondary trial.
<code>INew</code>	The maximum information of the secondary trial.
<code>MullerSchafer</code>	Whether to use the Muller and Schafer (2001) method for trial adaptation.
<code>informationRatesNew</code>	The spacing of looks of the secondary trial up to look L2.
<code>efficacyStoppingNew</code>	The indicators of whether efficacy stopping is allowed at each look of the secondary trial up to look L2. Defaults to true if left unspecified.
<code>typeAlphaSpendingNew</code>	The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpendingNew</code>	The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>spendingTimeNew</code>	The error spending time of the secondary trial up to look L2. Defaults to missing, in which case, it is the same as <code>informationRatesNew</code> .

## Value

A data frame with the following variables:

- `pvalue`: p-value for rejecting the null hypothesis.
- `thetahat`: Median unbiased point estimate of the parameter.
- `cilevel`: Confidence interval level.
- `lower`: Lower bound of confidence interval.
- `upper`: Upper bound of confidence interval.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

Ping Gao, Lingyun Liu and Cyrus Mehta. Exact inference for adaptive group sequential designs. Stat Med. 2013;32(23):3991-4005.

**See Also**

[adaptDesign](#)

**Examples**

```
# original group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                 alpha = 0.05, typeAlphaSpending = "sfHSD",
                 parameterAlphaSpending = -4))

# interim look results
L = 1
n1 = n/3
delta1 = 4.5
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

t = des1$byStageResults$informationRates

# Muller & Schafer (2001) method to design the secondary trial:
des2 = adaptDesign(
  betaNew = 0.2, L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2)

n2 = ceiling(des2$secondaryTrial$overallResults$information*4*20^2)
ns = round(n2*(1:3)/3)
(des2 = adaptDesign(
  INew = n2/(4*20^2), L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, informationRatesNew = ns/n2,
  typeAlphaSpendingNew = "sfHSD",
```



```

parameterAlphaSpendingNew = -2))

# termination at the second look of the secondary trial
L2 = 2
delta2 = 6.86
sigma2 = 21.77
zL2 = delta2/sqrt(4/197*sigma2^2)

t2 = des2$secondaryTrial$byStageResults$informationRates[1:L2]

# confidence interval
getADRCI(L = L, zL = zL,
         IMax = n/(4*sigma1^2), kMax = 3,
         informationRates = t,
         alpha = 0.05, typeAlphaSpending = "sfHSD",
         parameterAlphaSpending = -4,
         L2 = L2, zL2 = zL2,
         INew = n2/(4*sigma2^2),
         MullerSchafer = TRUE,
         informationRatesNew = t2,
         typeAlphaSpendingNew = "sfHSD",
         parameterAlphaSpendingNew = -2)

```

---

getADRCI

*Repeated confidence interval after adaptation*


---

### Description

Obtains the repeated p-value, conservative point estimate, and repeated confidence interval for an adaptive group sequential trial.

### Usage

```

getADRCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_,
  L2 = NA_integer_,
  zL2 = NA_real_,
  INew = NA_real_,

```

```

MullerSchafer = 0L,
informationRatesNew = NA_real_,
efficacyStoppingNew = NA_integer_,
typeAlphaSpendingNew = "sfOF",
parameterAlphaSpendingNew = NA_real_,
spendingTimeNew = NA_real_
)

```

## Arguments

L	The interim adaptation look of the primary trial.
zL	The z-test statistic at the interim adaptation look of the primary trial.
IMax	The maximum information of the primary trial.
kMax	The maximum number of stages of the primary trial.
informationRates	The information rates of the primary trial.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.
alpha	The significance level of the primary trial. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
spendingTime	The error spending time of the primary trial. Defaults to missing, in which case, it is the same as informationRates.
L2	The look of interest in the secondary trial.
zL2	The z-test statistic at the look of the secondary trial.
INew	The maximum information of the secondary trial.
MullerSchafer	Whether to use the Muller and Schafer (2001) method for trial adaptation.
informationRatesNew	The spacing of looks of the secondary trial.
efficacyStoppingNew	The indicators of whether efficacy stopping is allowed at each look of the secondary trial up to look L2. Defaults to true if left unspecified.

**typeAlphaSpendingNew**

The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpendingNew**

The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**spendingTimeNew**

The error spending time of the secondary trial. up to look L2. Defaults to missing, in which case, it is the same as informationRatesNew.

**Value**

A data frame with the following variables:

- pvalue: Repeated p-value for rejecting the null hypothesis.
- thetihat: Point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of repeated confidence interval.
- upper: Upper bound of repeated confidence interval.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

Cyrus R. Mehta, Peter Bauer, Martin Posch and Werner Brannath. Repeated confidence intervals for adaptive group sequential trials. *Stat Med.* 2007;26:5422–5433.

**See Also**

[adaptDesign](#)

**Examples**

```
# original group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4))

# interim look results
```

```

L = 1
n1 = n/3
delta1 = 4.5
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

t = des1$byStageResults$informationRates

# Muller & Schafer (2001) method to design the secondary trial:
des2 = adaptDesign(
  betaNew = 0.2, L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2)

n2 = ceiling(des2$secondaryTrial$overallResults$information*4*20^2)
ns = round(n2*(1:3)/3)
(des2 = adaptDesign(
  INew = n2/(4*20^2), L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, informationRatesNew = ns/n2,
  typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2))

# termination at the second look of the secondary trial
L2 = 2
delta2 = 6.86
sigma2 = 21.77
zL2 = delta2/sqrt(4/197*sigma2^2)

t2 = des2$secondaryTrial$byStageResults$informationRates[1:L2]

# repeated confidence interval
getADRCI(L = L, zL = zL,
  IMax = n/(4*sigma1^2), kMax = 3,
  informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  L2 = L2, zL2 = zL2,
  INew = n2/(4*sigma2^2),
  MullerSchafer = TRUE,
  informationRatesNew = t2,
  typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2)

```

---

getBound	<i>Efficacy boundaries for group sequential design</i>
----------	--

---

### Description

Obtains the efficacy stopping boundaries for a group sequential design.

### Usage

```
getBound(
  k = NA,
  informationRates = NA,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA,
  userAlphaSpending = NA,
  spendingTime = NA,
  efficacyStopping = NA
)
```

### Arguments

k	Look number for the current analysis.
informationRates	Information rates up to the current look. Must be increasing and less than or equal to 1.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length k for the error spending time at each analysis. Must be increasing and less than or equal to 1. Defaults to missing, in which case, it is the same as informationRates.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

**Details**

If typeAlphaSpending is "OF", "P", or "WT", then the boundaries will be based on equally spaced looks.

**Value**

A numeric vector of critical values up to the current look.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
getBound(k = 2, informationRates = c(0.5,1),
         alpha = 0.025, typeAlphaSpending = "sfOF")
```

---

getCI

*Confidence interval after trial termination*

---

**Description**

Obtains the p-value, median unbiased point estimate, and confidence interval after the end of a group sequential trial.

**Usage**

```
getCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

**Arguments**

L	The termination look.
zL	The z-test statistic at the termination look.
IMax	The maximum information of the trial.
informationRates	The information rates up to look L.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage up to look L. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping up to look L.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value of alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
spendingTime	The error spending time up to look L. Defaults to missing, in which case, it is the same as informationRates.

**Value**

A data frame with the following components:

- pvalue: p-value for rejecting the null hypothesis.
- thetihat: Median unbiased point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of confidence interval.
- upper: Upper bound of confidence interval.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

Anastasios A. Tsiatis, Gary L. Rosner and Cyrus R. Mehta. Exact confidence intervals following a group sequential test. *Biometrics* 1984;40:797-803.

**Examples**

```

# group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                 alpha = 0.05, typeAlphaSpending = "sfHSD",
                 parameterAlphaSpending = -4))

# crossed the boundary at the second look
L = 2
n1 = n*2/3
delta1 = 7
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

# confidence interval
getCI(L = L, zL = zL, IMax = n/(4*sigma1^2),
      informationRates = c(1/3, 2/3), alpha = 0.05,
      typeAlphaSpending = "sfHSD", parameterAlphaSpending = -4)

```

---

getCP

*Conditional power allowing for varying parameter values*


---

**Description**

Obtains the conditional power for specified incremental information given the interim results, parameter values, and data-dependent changes in the error spending function, as well as the number and spacing of interim looks.

**Usage**

```

getCP(
  INew = NA_real_,
  L = NA_integer_,
  zL = NA_real_,
  theta = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,

```



```

userAlphaSpending = NA_real_,
futilityBounds = NA_real_,
typeBetaSpending = "none",
parameterBetaSpending = NA_real_,
spendingTime = NA_real_,
MullerSchafer = 0L,
kNew = NA_integer_,
informationRatesNew = NA_real_,
efficacyStoppingNew = NA_integer_,
futilityStoppingNew = NA_integer_,
typeAlphaSpendingNew = "sfOF",
parameterAlphaSpendingNew = NA_real_,
typeBetaSpendingNew = "none",
parameterBetaSpendingNew = NA_real_,
spendingTimeNew = NA_real_,
varianceRatio = 1
)

```

## Arguments

I <sub>New</sub>	The maximum information of the secondary trial.
L	The interim adaptation look of the primary trial.
z <sub>L</sub>	The z-test statistic at the interim adaptation look of the primary trial.
theta	A scalar or a vector of parameter values of length k <sub>Max</sub> + k <sub>Max</sub> - L if MullerSchafer = FALSE or length k <sub>Max</sub> + k <sub>New</sub> if MullerSchafer = TRUE.
I <sub>Max</sub>	The maximum information of the primary trial.
k <sub>Max</sub>	The maximum number of stages of the primary trial.
informationRates	The information rates of the primary trial.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.
alpha	The significance level of the primary trial. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending	The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending for the primary trial. Cumulative alpha spent up to each stage.
futilityBounds	The lower boundaries on the z-test statistic scale for futility stopping for the primary trial. Defaults to $\text{rep}(-6, k_{\text{Max}}-1)$ if left unspecified.
typeBetaSpending	The type of beta spending for the primary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value of beta spending for the primary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".
spendingTime	The error spending time of the primary trial. Defaults to missing, in which case, it is the same as informationRates.
MullerSchafer	Whether to use the Muller and Schafer (2001) method for trial adaptation.
kNew	The number of looks of the secondary trial.
informationRatesNew	The spacing of looks of the secondary trial.
efficacyStoppingNew	The indicators of whether efficacy stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.
futilityStoppingNew	The indicators of whether futility stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.
typeAlphaSpendingNew	The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpendingNew	The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
typeBetaSpendingNew	The type of beta spending for the secondary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpendingNew  
 The parameter value of beta spending for the secondary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

spendingTimeNew  
 The error spending time of the secondary trial. Defaults to missing, in which case, it is the same as informationRatesNew.

varianceRatio  
 The ratio of the variance under H0 to the variance under H1.

### Value

The conditional power given the interim results, parameter values, and data-dependent design changes.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### References

Cyrus R. Mehta and Stuart J. Pocock. Adaptive increase in sample size when interim results are promising: A practical guide with examples. *Stat Med.* 2011;30:3267–3284.

### See Also

[getDesign](#)

### Examples

```
# Conditional power calculation with delayed treatment effect

# Two interim analyses have occurred with 179 and 266 events,
# respectively. The observed hazard ratio at the second interim
# look is 0.81.

trialsdt = as.Date("2020-03-04")           # trial start date
iadt = c(as.Date("2022-02-01"), as.Date("2022-11-01")) # interim dates
mo1 = as.numeric(iadt - trialsdt + 1)/30.4375 # interim months

# Assume a piecewise Poisson enrollment process with a 8-month ramp-up
# and 521 patients were enrolled after 17.94 months
N = 521 # total number of patients
Ta = 17.94 # enrollment duration
Ta1 = 8 # assumed end of enrollment ramp-up
enrate = N / (Ta - Ta1/2) # enrollment rate after ramp-up

# Assume a median survival of 16.7 months for the control group, a
# 5-month delay in treatment effect, and a hazard ratio of 0.7 after
# the delay
lam1 = log(2)/16.7 # control group hazard of exponential distribution
t1 = 5 # months of delay in treatment effect
```

```

hr = 0.7          # hazard ratio after delay
lam2 = hr*lam1    # treatment group hazard after delay

# Assume an annual dropout rate of 5%
gam = -log(1-0.05)/12 # hazard for dropout

# The original target number of events was 298 and the new target is 335
mo2 <- caltime(
  nevents = c(298, 335),
  allocationRatioPlanned = 1,
  accrualTime = seq(0, Ta1),
  accrualIntensity = enrate*seq(1, Ta1+1)/(Ta1+1),
  piecewiseSurvivalTime = c(0, t1),
  lambda1 = c(lam1, lam2),
  lambda2 = c(lam1, lam1),
  gamma1 = gam,
  gamma2 = gam,
  accrualDuration = Ta,
  followupTime = 1000)

# expected number of events and average hazard ratios
(lr1 <- lrstat(
  time = c(mo1, mo2),
  accrualTime = seq(0, Ta1),
  accrualIntensity = enrate*seq(1, Ta1+1)/(Ta1+1),
  piecewiseSurvivalTime = c(0, t1),
  lambda1 = c(lam1, lam2),
  lambda2 = c(lam1, lam1),
  gamma1 = gam,
  gamma2 = gam,
  accrualDuration = Ta,
  followupTime = 1000,
  predictTarget = 3))

hr2 = 0.81          # observed hazard ratio at interim 2
z2 = (-log(hr2))*sqrt(266/4) # corresponding z-test statistic value

# expected mean of -log(HR) at the original looks and the new final look
theta = -log(lr1$HR[c(1,2,3,4)])

# conditional power with sample size increase
getCP(INew = (335 - 266)/4,
  L = 2, zL = z2, theta = theta,
  IMax = 298/4, kMax = 3,
  informationRates = c(179, 266, 298)/298,
  alpha = 0.025, typeAlphaSpending = "sfOF")

```

**Description**

Obtains the maximum information and stopping boundaries for a generic group sequential design assuming a constant treatment effect, or obtains the power given the maximum information and stopping boundaries.

**Usage**

```
getDesign(
  beta = NA_real_,
  IMax = NA_real_,
  theta = NA_real_,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_,
  varianceRatio = 1
)
```

**Arguments**

beta	The type II error.
IMax	The maximum information. Either beta or IMax should be provided while the other one should be missing.
theta	The parameter value.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.

typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
varianceRatio	The ratio of the variance under H0 to the variance under H1.

## Value

An S3 class design object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).

- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale.
  - `futilityBounds`: The futility boundaries on the Z-scale.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.
  - `efficacyTheta`: The efficacy boundaries on the parameter scale.
  - `futilityTheta`: The futility boundaries on the parameter scale.
  - `efficacyP`: The efficacy boundaries on the p-value scale.
  - `futilityP`: The futility boundaries on the p-value scale.
  - `information`: The cumulative information.
  - `efficacyStopping`: Whether to allow efficacy stopping.
  - `futilityStopping`: Whether to allow futility stopping.
  - `rejectPerStageH0`: The probability for efficacy stopping under H0.
  - `futilityPerStageH0`: The probability for futility stopping under H0.
  - `cumulativeRejectionH0`: The cumulative probability for efficacy stopping under H0.
  - `cumulativeFutilityH0`: The cumulative probability for futility stopping under H0.
- `settings`: A list containing the following input parameters:
  - `typeAlphaSpending`: The type of alpha spending.
  - `parameterAlphaSpending`: The parameter value for alpha spending.
  - `userAlphaSpending`: The user defined alpha spending.
  - `typeBetaSpending`: The type of beta spending.
  - `parameterBetaSpending`: The parameter value for beta spending.
  - `userBetaSpending`: The user defined beta spending.
  - `spendingTime`: The error spending time at each analysis.
  - `varianceRatio`: The ratio of the variance under H0 to the variance under H1.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### References

Christopher Jennison, Bruce W. Turnbull. Group Sequential Methods with Applications to Clinical Trials. Chapman & Hall/CRC: Boca Raton, 2000, ISBN:0849303168

### Examples

```
# Example 1: obtain the maximum information given power
(design1 <- getDesign(
  beta = 0.2, theta = -log(0.7),
```

```

kMax = 2, informationRates = c(0.5,1),
alpha = 0.025, typeAlphaSpending = "sf0F",
typeBetaSpending = "sfP"))

# Example 2: obtain power given the maximum information
(design2 <- getDesign(
  IMax = 72.5, theta = -log(0.7),
  kMax = 3, informationRates = c(0.5, 0.75, 1),
  alpha = 0.025, typeAlphaSpending = "sf0F",
  typeBetaSpending = "sfP"))

```

---

getDesignAgreement      *Power and sample size for Cohen's kappa*

---

## Description

Obtains the power given sample size or obtains the sample size given power for Cohen's kappa.

## Usage

```

getDesignAgreement(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  kappaH0 = NA_real_,
  kappa = NA_real_,
  p1 = NA_real_,
  p2 = NA_real_,
  rounding = TRUE,
  alpha = 0.025
)

```

## Arguments

beta	The type II error.
n	The total sample size.
ncats	The number of categories.
kappaH0	The kappa coefficient under the null hypothesis.
kappa	The kappa coefficient under the alternative hypothesis.
p1	The marginal probabilities for the first rater.
p2	The marginal probabilities for the second rater. Defaults to be equal to the marginal probabilities for the first rater if not provided.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.



## Details

The kappa coefficient is defined as

$$\kappa = \frac{\pi_o - \pi_e}{1 - \pi_e},$$

where  $\pi_o = \sum_i \pi_{ii}$  is the observed agreement, and  $\pi_e = \sum_i \pi_{i.} \pi_{.i}$  is the expected agreement by chance.

By Fleiss et al. (1969), the variance of  $\hat{\kappa}$  is given by

$$Var(\hat{\kappa}) = \frac{v_1}{n},$$

where

$$v_1 = \frac{Q_1 + Q_2 - Q_3 - Q_4}{(1 - \pi_e)^4},$$

$$Q_1 = \pi_o(1 - \pi_e)^2,$$

$$Q_2 = (1 - \pi_o)^2 \sum_i \sum_j \pi_{ij}(\pi_{i.} + \pi_{.j})^2,$$

$$Q_3 = 2(1 - \pi_o)(1 - \pi_e) \sum_i \pi_{ii}(\pi_{i.} + \pi_{.i}),$$

$$Q_4 = (\pi_o \pi_e - 2\pi_e + \pi_o)^2.$$

Given  $\kappa$  and marginals  $\{(\pi_{i.}, \pi_{.i}) : i = 1, \dots, k\}$ , we obtain  $\pi_o$ . The only unknowns are the double summation in  $Q_2$  and the single summation in  $Q_3$ .

We find the optimal configuration of cell probabilities that yield the maximum variance of  $\hat{\kappa}$  by treating the problem as a linear programming problem with constraints to match the given marginal probabilities and the observed agreement and ensure that the cell probabilities are nonnegative. This is an extension of Flack et al. (1988) by allowing unequal marginal probabilities of the two raters.

We perform the optimization under the null and alternative hypotheses to obtain  $\max Var(\hat{\kappa}|\kappa = \kappa_0)$  and  $\max Var(\hat{\kappa}|\kappa = \kappa_1)$  for a single subject, and then calculate the sample size or power according to the following equation:

$$\sqrt{n}|\kappa - \kappa_0| = z_{1-\alpha} \sqrt{\max Var(\hat{\kappa}|\kappa = \kappa_0)} + z_{1-\beta} \sqrt{\max Var(\hat{\kappa}|\kappa = \kappa_1)}.$$

## Value

An S3 class `designAgreement` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The one-sided significance level.
- `n`: The total sample size.
- `ncats`: The number of categories.
- `kappaH0`: The kappa coefficient under the null hypothesis.
- `kappa`: The kappa coefficient under the alternative hypothesis.
- `p1`: The marginal probabilities for the first rater.
- `p2`: The marginal probabilities for the second rater.
- `piH0`: The cell probabilities that maximize the variance of estimated kappa under H0.
- `pi`: The cell probabilities that maximize the variance of estimated kappa under H1.
- `rounding`: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

V. F. Flack, A. A. Afifi, and P. A. Lachenbruch. Sample size determinations for the two rater kappa statistic. *Psychometrika* 1988; 53:321-325.

**Examples**

```
(design1 <- getDesignAgreement(  
  beta = 0.2, n = NA, ncats = 4, kappaH0 = 0.4, kappa = 0.6,  
  p1 = c(0.1, 0.2, 0.3, 0.4), p2 = c(0.15, 0.2, 0.24, 0.41),  
  rounding = TRUE, alpha = 0.05))
```

---

getDesignANOVA

*Power and sample size for one-way ANOVA*

---

**Description**

Obtains the power and sample size for one-way analysis of variance.

**Usage**

```
getDesignANOVA(  
  beta = NA_real_,  
  n = NA_real_,  
  ngroups = 2,  
  means = NA_real_,  
  stDev = 1,  
  allocationRatioPlanned = NA_real_,  
  rounding = TRUE,  
  alpha = 0.05  
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The common standard deviation.

allocationRatioPlanned	Allocation ratio for the treatment groups. It has length <code>ngroups - 1</code> or <code>ngroups</code> . If it is of length <code>ngroups - 1</code> , then the last treatment group will assume value 1 for allocation ratio.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

### Details

Let  $\{\mu_i : i = 1, \dots, k\}$  denote the group means, and  $\{r_i : i = 1, \dots, k\}$  denote the randomization probabilities to the  $k$  treatment groups. Let  $\sigma$  denote the common standard deviation, and  $n$  denote the total sample size. Then the  $F$ -statistic

$$F = \frac{SSR/(k-1)}{SSE/(n-k)} \sim F_{k-1, n-k, \lambda},$$

where

$$\lambda = n \sum_{i=1}^k r_i (\mu_i - \bar{\mu})^2 / \sigma^2$$

is the noncentrality parameter, and  $\bar{\mu} = \sum_{i=1}^k r_i \mu_i$ .

### Value

An S3 class `designANOVA` object with the following components:

- `power`: The power to reject the null hypothesis that there is no difference among the treatment groups.
- `alpha`: The two-sided significance level.
- `n`: The number of subjects.
- `ngroups`: The number of treatment groups.
- `means`: The treatment group means.
- `stDev`: The common standard deviation.
- `effectsize`: The effect size.
- `allocationRatioPlanned`: Allocation ratio for the treatment groups.
- `rounding`: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
(design1 <- getDesignANOVA(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 3.5, allocationRatioPlanned = c(2, 2, 2, 1),
  alpha = 0.05))
```

---

```
getDesignANOVAContrast
```

*Power and sample size for one-way ANOVA contrast*

---

## Description

Obtains the power and sample size for a single contrast in one-way analysis of variance.

## Usage

```
getDesignANOVAContrast(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  contrast = NA_real_,
  meanContrastH0 = 0,
  allocationRatioPlanned = NA_real_,
  rounding = TRUE,
  alpha = 0.025
)
```

## Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The common standard deviation.
contrast	The coefficients for the single contrast.
meanContrastH0	The mean of the contrast under the null hypothesis.
allocationRatioPlanned	Allocation ratio for the treatment groups. It has length <code>ngroups - 1</code> or <code>ngroups</code> . If it is of length <code>ngroups - 1</code> , then the last treatment group will assume value 1 for allocation ratio.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

## Value

An S3 class `designANOVAContrast` object with the following components:

- `power`: The power to reject the null hypothesis for the treatment contrast.

- alpha: The one-sided significance level.
- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The common standard deviation.
- contrast: The coefficients for the single contrast.
- meanContrastH0: The mean of the contrast under the null hypothesis.
- meanContrast: The mean of the contrast under the alternative hypothesis.
- effectsize: The effect size.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
(design1 <- getDesignANOVAContrast(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 3.5, contrast = c(1, 1, 1, -3)/3,
  allocationRatioPlanned = c(2, 2, 2, 1),
  alpha = 0.025))
```

---

getDesignEquiv	<i>Power and sample size for a generic group sequential equivalence design</i>
----------------	--

---

### Description

Obtains the maximum information and stopping boundaries for a generic group sequential equivalence design assuming a constant treatment effect, or obtains the power given the maximum information and stopping boundaries.

### Usage

```
getDesignEquiv(
  beta = NA_real_,
  IMax = NA_real_,
  thetaLower = NA_real_,
  thetaUpper = NA_real_,
  theta = 0,
  kMax = 1L,
```

```

informationRates = NA_real_,
criticalValues = NA_real_,
alpha = 0.05,
typeAlphaSpending = "sfOF",
parameterAlphaSpending = NA_real_,
userAlphaSpending = NA_real_,
spendingTime = NA_real_,
varianceRatioH10 = 1,
varianceRatioH20 = 1,
varianceRatioH12 = 1,
varianceRatioH21 = 1
)

```

### Arguments

beta	The type II error.
IMax	The maximum information. Either beta or IMax should be provided while the other one should be missing.
thetaLower	The parameter value at the lower equivalence limit.
thetaUpper	The parameter value at the upper equivalence limit.
theta	The parameter value under the alternative hypothesis.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests, e.g., 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
varianceRatioH10	The ratio of the variance under H10 to the variance under H1.
varianceRatioH20	The ratio of the variance under H20 to the variance under H1.

varianceRatioH12

The ratio of the variance under H10 to the variance under H20.

varianceRatioH21

The ratio of the variance under H20 to the variance under H10.

## Details

Consider the equivalence design with two one-sided hypotheses:

$$H_{10} : \theta \leq \theta_{10},$$

$$H_{20} : \theta \geq \theta_{20}.$$

We reject  $H_{10}$  at or before look  $k$  if

$$Z_{1j} = (\hat{\theta}_j - \theta_{10}) \sqrt{\frac{n_j}{v_{10}}} \geq b_j$$

for some  $j = 1, \dots, k$ , where  $\{b_j : j = 1, \dots, K\}$  are the critical values associated with the specified alpha-spending function, and  $v_{10}$  is the null variance of  $\hat{\theta}$  based on the restricted maximum likelihood (reml) estimate of model parameters subject to the constraint imposed by  $H_{10}$  for one sampling unit drawn from  $H_1$ . For example, for estimating the risk difference  $\theta = \pi_1 - \pi_2$ , the asymptotic limits of the reml estimates of  $\pi_1$  and  $\pi_2$  subject to the constraint imposed by  $H_{10}$  are given by

$$(\tilde{\pi}_1, \tilde{\pi}_2) = f(\theta_{10}, r, r\pi_1, 1-r, (1-r)\pi_2),$$

where  $f(\theta_0, n_1, y_1, n_2, y_2)$  is the function to obtain the reml of  $\pi_1$  and  $\pi_2$  subject to the constraint that  $\pi_1 - \pi_2 = \theta_0$  with observed data  $(n_1, y_1, n_2, y_2)$  for the number of subjects and number of responses in the active treatment and control groups,  $r$  is the randomization probability for the active treatment group, and

$$v_{10} = \frac{\tilde{\pi}_1(1-\tilde{\pi}_1)}{r} + \frac{\tilde{\pi}_2(1-\tilde{\pi}_2)}{1-r}.$$

Let  $I_j = n_j/v_1$  denote the information for  $\theta$  at the  $j$ th look, where

$$v_1 = \frac{\pi_1(1-\pi_1)}{r} + \frac{\pi_2(1-\pi_2)}{1-r}$$

denotes the variance of  $\hat{\theta}$  under  $H_1$  for one sampling unit. It follows that

$$(Z_{1j} \geq b_j) = (Z_j \geq w_{10}b_j + (\theta_{10} - \theta)\sqrt{I_j}),$$

where  $Z_j = (\hat{\theta}_j - \theta)\sqrt{I_j}$ , and  $w_{10} = \sqrt{v_{10}/v_1}$ .

Similarly, we reject  $H_{20}$  at or before look  $k$  if

$$Z_{2j} = (\hat{\theta}_j - \theta_{20}) \sqrt{\frac{n_j}{v_{20}}} \leq -b_j$$

for some  $j = 1, \dots, k$ , where  $v_{20}$  is the null variance of  $\hat{\theta}$  based on the reml estimate of model parameters subject to the constraint imposed by  $H_{20}$  for one sampling unit drawn from  $H_1$ . We have

$$(Z_{2j} \leq -b_j) = (Z_j \leq -w_{20}b_j + (\theta_{20} - \theta)\sqrt{I_j}),$$

where  $w_{20} = \sqrt{v_{20}/v_1}$ .

Let  $l_j = w_{10}b_j + (\theta_{10} - \theta)\sqrt{I_j}$ , and  $u_j = -w_{20}b_j + (\theta_{20} - \theta)\sqrt{I_j}$ . The cumulative probability to reject  $H_0 = H_{10} \cup H_{20}$  at or before look  $k$  under the alternative hypothesis  $H_1$  is given by

$$P_\theta \left( \bigcup_{j=1}^k (Z_{1j} \geq b_j) \cap \bigcup_{j=1}^k (Z_{2j} \leq -b_j) \right) = p_1 + p_2 + p_{12},$$

where

$$p_1 = P_\theta \left( \bigcup_{j=1}^k (Z_{1j} \geq b_j) \right) = P_\theta \left( \bigcup_{j=1}^k (Z_j \geq l_j) \right),$$

$$p_2 = P_\theta \left( \bigcup_{j=1}^k (Z_{2j} \leq -b_j) \right) = P_\theta \left( \bigcup_{j=1}^k (Z_j \leq u_j) \right),$$

and

$$p_{12} = P_\theta \left( \bigcup_{j=1}^k \{ (Z_j \geq l_j) \cup (Z_j \leq u_j) \} \right).$$

Of note, both  $p_1$  and  $p_2$  can be evaluated using one-sided exit probabilities for group sequential designs. If there exists  $j \leq k$  such that  $l_j \leq u_j$ , then  $p_{12} = 1$ . Otherwise,  $p_{12}$  can be evaluated using two-sided exit probabilities for group sequential designs.

To evaluate the type I error of the equivalence trial under  $H_{10}$ , we first match the information under  $H_{10}$  with the information under  $H_1$ . For example, for estimating the risk difference for two independent samples, the sample size  $n_{10}$  under  $H_{10}$  must satisfy

$$\frac{1}{n_{10}} \left( \frac{(\pi_2 + \theta_{10})(1 - \pi_2 - \theta_{10})}{r} + \frac{\pi_2(1 - \pi_2)}{1 - r} \right) = \frac{1}{n} \left( \frac{\pi_1(1 - \pi_1)}{r} + \frac{\pi_2(1 - \pi_2)}{1 - r} \right).$$

Then we obtain the reml estimates of  $\pi_1$  and  $\pi_2$  subject to the constraint imposed by  $H_{20}$  for one sampling unit drawn from  $H_{10}$ ,

$$(\tilde{\pi}_{10}, \tilde{\pi}_{20}) = f(\theta_{20}, r, r(\pi_2 + \theta_{10}), 1 - r, (1 - r)\pi_2).$$

Let  $t_j$  denote the information fraction at look  $j$ . Define

$$\tilde{v}_1 = \frac{(\pi_2 + \theta_{10})(1 - \pi_2 - \theta_{10})}{r} + \frac{\pi_2(1 - \pi_2)}{1 - r},$$

and

$$\tilde{v}_{20} = \frac{\tilde{\pi}_{10}(1 - \tilde{\pi}_{10})}{r} + \frac{\tilde{\pi}_{20}(1 - \tilde{\pi}_{20})}{1 - r}.$$

The cumulative rejection probability under  $H_{10}$  at or before look  $k$  is given by

$$P_{\theta_{10}} \left( \bigcup_{j=1}^k \{ (\hat{\theta}_j - \theta_{10})\sqrt{n_{10}t_j/\tilde{v}_1} \geq b_j \} \cap \bigcup_{j=1}^k \{ (\hat{\theta}_j - \theta_{20})\sqrt{n_{10}t_j/\tilde{v}_{20}} \leq -b_j \} \right) = q_1 + q_2 + q_{12},$$

where

$$q_1 = P_{\theta_{10}} \left( \bigcup_{j=1}^k \{ (\hat{\theta}_j - \theta_{10})\sqrt{n_{10}t_j/\tilde{v}_1} \geq b_j \} \right) = P_{\theta_{10}} \left( \bigcup_{j=1}^k (Z_j \geq b_j) \right),$$

$$q_2 = P_{\theta_{10}} \left( \bigcup_{j=1}^k \{ (\hat{\theta}_j - \theta_{20})\sqrt{n_{10}t_j/\tilde{v}_{20}} \leq -b_j \} \right) = P_{\theta_{10}} \left( \bigcup_{j=1}^k (Z_j \leq -b_j w_{21} + (\theta_{20} - \theta_{10})\sqrt{I_j}) \right),$$

and

$$q_{12} = P_{\theta_{10}} \left( \bigcup_{j=1}^k \{ (Z_j \geq b_j) \cup (Z_j \leq -w_{21}b_j + (\theta_{20} - \theta_{10})\sqrt{I_j}) \} \right).$$



Here  $Z_j = (\hat{\theta}_j - \theta_{10})\sqrt{I_j}$ , and  $w_{21} = \sqrt{\tilde{v}_{20}/\tilde{v}_1}$ . Of note,  $q_1$ ,  $q_2$ , and  $q_{12}$  can be evaluated using group sequential exit probabilities. Similarly, we can define  $\tilde{v}_2$ ,  $\tilde{v}_{10}$ , and  $w_{12} = \sqrt{\tilde{v}_{10}/\tilde{v}_2}$ , and evaluate the type I error under  $H_{20}$ .

The variance ratios correspond to

$$\text{varianceRatioH10} = v_{10}/v_1,$$

$$\text{varianceRatioH20} = v_{20}/v_1,$$

$$\text{varianceRatioH12} = \tilde{v}_{10}/\tilde{v}_2,$$

$$\text{varianceRatioH21} = \tilde{v}_{20}/\tilde{v}_1.$$

If the alternative variance is used, then the variance ratios are all equal to 1.

## Value

An S3 class `designEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlphaH10`: The attained significance level under H10.
  - `attainedAlphaH20`: The attained significance level under H20.
  - `kMax`: The number of stages.
  - `thetaLower`: The parameter value at the lower equivalence limit.
  - `thetaUpper`: The parameter value at the upper equivalence limit.
  - `theta`: The parameter value under the alternative hypothesis.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH10`: The expected information under H10.
  - `expectedInformationH20`: The expected information under H20.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha for each of the two one-sided tests.
  - `cumulativeAttainedAlphaH10`: The cumulative probability for efficacy stopping under H10.
  - `cumulativeAttainedAlphaH20`: The cumulative probability for efficacy stopping under H20.
  - `efficacyThetaLower`: The efficacy boundaries on the parameter scale for the one-sided null hypothesis at the lower equivalence limit.
  - `efficacyThetaUpper`: The efficacy boundaries on the parameter scale for the one-sided null hypothesis at the upper equivalence limit.

- efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
- information: The cumulative information.
- settings: A list containing the following components:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
# Example 1: obtain the maximum information given power
(design1 <- getDesignEquiv(
  beta = 0.2, thetaLower = log(0.8), thetaUpper = log(1.25),
  kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF"))
```

```
# Example 2: obtain power given the maximum information
(design2 <- getDesignEquiv(
  IMax = 72.5, thetaLower = log(0.7), thetaUpper = -log(0.7),
  kMax = 3, informationRates = c(0.5, 0.75, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF"))
```

---

getDesignFisherExact    *Power and sample size for Fisher's exact test for two proportions*

---

### Description

Obtains the power given sample size or obtains the sample size given power for Fisher's exact test for two proportions.

**Usage**

```
getDesignFisherExact(  
  beta = NA_real_,  
  n = NA_real_,  
  pi1 = NA_real_,  
  pi2 = NA_real_,  
  allocationRatioPlanned = 1,  
  alpha = 0.05  
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The two-sided significance level. Defaults to 0.05.

**Value**

A data frame with the following variables:

- alpha: The two-sided significance level.
- power: The power.
- n: The sample size.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignFisherExact(  
  beta = 0.2, pi1 = 0.5, pi2 = 0.2, alpha = 0.05))
```

---

getDesignLogistic      *Power and sample size for logistic regression*

---

### Description

Obtains the power given sample size or obtains the sample size given power for logistic regression of a binary response given the covariate of interest and other covariates.

### Usage

```
getDesignLogistic(
  beta = NA_real_,
  n = NA_real_,
  ncovariates = NA_integer_,
  nconfigs = NA_integer_,
  x = NA_real_,
  pconfigs = NA_real_,
  corr = 0,
  oddsratios = NA_real_,
  responseprob = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

### Arguments

beta	The type II error.
n	The total sample size.
ncovariates	The number of covariates.
nconfigs	The number of configurations of discretized covariate values.
x	The matrix of covariate values.
pconfigs	The vector of probabilities for the configurations.
corr	The multiple correlation between the predictor and other covariates. Defaults to 0.
oddsratios	The odds ratios for one unit increase in the covariates.
responseprob	The response probability in the full model when all predictor variables are equal to their means.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

### Details

We consider the logistic regression of a binary response variable  $Y$  on a set of predictor variables  $x = (x_1, \dots, x_K)^T$  with  $x_1$  being the covariate of interest:  $\log \frac{P(Y_i=1)}{1-P(Y_i=1)} = \psi_0 + x_i^T \psi$ , where  $\psi = (\psi_1, \dots, \psi_K)^T$ . Similar to Self et al (1992), we assume that all covariates are either inherently discrete or discretized from continuous distributions (e.g. using the quantiles). Let  $m$  denote the total number of configurations of the covariate values. Let

$$\pi_i = P(x = x_i), i = 1, \dots, m$$

denote the probabilities for the configurations of the covariates under independence. The likelihood ratio test statistic for testing  $H_0 : \psi_1 = 0$  can be approximated by a noncentral chi-square distribution with one degree of freedom and noncentrality parameter

$$\Delta = 2 \sum_{i=1}^m \pi_i [b'(\theta_i)(\theta_i - \theta_i^*) - \{b(\theta_i) - b(\theta_i^*)\}],$$

where

$$\theta_i = \psi_0 + \sum_{j=1}^k \psi_j x_{ij},$$

$$\theta_i^* = \psi_0^* + \sum_{j=2}^k \psi_j^* x_{ij},$$

for  $\psi_0^* = \psi_0 + \psi_1 \mu_1$ , and  $\psi_j^* = \psi_j$  for  $j = 2, \dots, K$ . Here  $\mu_1$  is the mean of  $x_1$ , e.g.,  $\mu_1 = \sum_i \pi_i x_{i1}$ . In addition, by formulating the logistic regression in the framework of generalized linear models,

$$b(\theta) = \log(1 + \exp(\theta)),$$

and

$$b'(\theta) = \frac{\exp(\theta)}{1 + \exp(\theta)}.$$

The regression coefficients  $\psi$  can be obtained by taking the log of the odds ratios for the covariates. The intercept  $\psi_0$  can be derived as

$$\psi_0 = \log(\bar{\mu}/(1 - \bar{\mu})) - \sum_{j=1}^K \psi_j \mu_j,$$

where  $\bar{\mu}$  denotes the response probability when all predictor variables are equal to their means.

Finally, let  $\rho$  denote the multiple correlation between the predictor and other covariates. The non-centrality parameter of the chi-square test is adjusted downward by multiplying by  $1 - \rho^2$ .

### Value

An S3 class `designLogistic` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The two-sided significance level.

- n: The total sample size.
- ncovariates: The number of covariates.
- nconfigs: The number of configurations of discretized covariate values.
- x: The matrix of covariate values.
- pconfigs: The vector of probabilities for the configurations.
- corr: The multiple correlation between the predictor and other covariates.
- oddsratios: The odds ratios for one unit increase in the covariates.
- responseprob: The response probability in the full model when all predictor variables are equal to their means.
- effectsize: The effect size for the chi-square test.
- rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### References

Steven G. Self, Robert H. Mauritsen and Jill Ohara. Power calculations for likelihood ratio tests in generalized linear models. *Biometrics* 1992; 48:31-39.

### Examples

```
# two ordinal covariates
x1 = c(5, 10, 15, 20)
px1 = c(0.2, 0.3, 0.3, 0.2)

x2 = c(2, 4, 6)
px2 = c(0.4, 0.4, 0.2)

# discretizing a normal distribution with mean 4 and standard deviation 2
nbins = 10
x3 = qnorm(((1:nbins) - 0.5)/nbins)*2 + 4
px3 = rep(1/nbins, nbins)

# combination of covariate values
nconfigs = length(x1)*length(x2)*length(x3)
x = expand.grid(x3 = x3, x2 = x2, x1 = x1)
x = as.matrix(x[, ncol(x):1])

# probabilities for the covariate configurations under independence
pconfigs = as.numeric(px1 %% px2 %% px3)

# convert the odds ratio for the predictor variable in 5-unit change
# to the odds ratio in 1-unit change
(design1 <- getDesignLogistic(
  beta = 0.1, ncovariates = 3,
  nconfigs = nconfigs,
```

```
x = x,
pconfigs = pconfigs,
oddsratios = c(1.2^(1/5), 1.4, 1.3),
responseprob = 0.25,
alpha = 0.1))
```

---

getDesignMeanDiff      *Group sequential design for two-sample mean difference*

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean difference.

### Usage

```
getDesignMeanDiff(
  beta = NA_real_,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
meanDiffH0	The mean difference under the null hypothesis. Defaults to 0.

<code>meanDiff</code>	The mean difference under the alternative hypothesis.
<code>stDev</code>	The standard deviation.
<code>allocationRatioPlanned</code>	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
<code>normalApproximation</code>	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
<code>futilityStopping</code>	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level. Defaults to 0.025.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.
<code>futilityBounds</code>	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
<code>typeBetaSpending</code>	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
<code>parameterBetaSpending</code>	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".



userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

### Value

An S3 class designMeanDiff object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanDiffH0: The mean difference under the null hypothesis.
  - meanDiff: The mean difference under the alternative hypothesis.
  - stDev: The standard deviation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.

- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- efficacyMeanDiff: The efficacy boundaries on the mean difference scale.
- futilityMeanDiff: The futility boundaries on the mean difference scale.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiff(
  beta = NA, n = 456, meanDiff = 9, stDev = 32,
  kMax = 5, alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))

# Example 2: sample size calculation for two-sample t-test
(design2 <- getDesignMeanDiff(
  beta = 0.1, n = NA, meanDiff = 0.3, stDev = 1,
  normalApproximation = FALSE, alpha = 0.025))
```

---

getDesignMeanDiffCarryover

*Power and sample size for direct treatment effects in crossover trials  
accounting for carryover effects*

---

**Description**

Obtains the power and sample size for direct treatment effects in crossover trials accounting for carryover effects.

**Usage**

```

getDesignMeanDiffCarryover(
  beta = NA_real_,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  stDev = 1,
  corr = 0.5,
  design = NA_real_,
  cumdrop = NA_real_,
  allocationRatioPlanned = NA_real_,
  normalApproximation = FALSE,
  rounding = TRUE,
  alpha = 0.025
)

```

**Arguments**

beta	The type II error.
n	The total sample size.
meanDiffH0	The mean difference at the last time point under the null hypothesis. Defaults to 0.
meanDiff	The mean difference at the last time point under the alternative hypothesis.
stDev	The standard deviation for within-subject random error.
corr	The intra-subject correlation due to subject random effect.
design	The crossover design represented by a matrix with rows indexing the sequences, columns indexing the periods, and matrix entries indicating the treatments.
cumdrop	The cumulative dropout rate over periods.
allocationRatioPlanned	Allocation ratio for the sequences. Defaults to equal randomization if not provided.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

**Details**

The linear mixed-effects model to assess the direct treatment effect in the presence of carryover treatment effect is given by

$$y_{ijk} = \mu + \alpha_i + b_{ij} + \gamma_k + \tau_{d(i,k)} + \lambda_{c(i,k-1)} + e_{ijk},$$

$$i = 1, \dots, n; j = 1, \dots, r_i; k = 1, \dots, p; d, c = 1, \dots, t,$$

where  $\mu$  is the general mean,  $\alpha_i$  is the effect of the  $i$ th treatment sequence,  $b_{ij}$  is the random effect with variance  $\sigma_b^2$  for the  $j$ th subject of the  $i$ th treatment sequence,  $\gamma_k$  is the period effect, and  $e_{ijk}$  is the random error with variance  $\sigma^2$  for the subject in period  $k$ . The direct effect of the treatment administered in period  $k$  of sequence  $i$  is  $\tau_{d(i,k)}$ , and  $\lambda_{c(i,k-1)}$  is the carryover effect of the treatment administered in period  $k-1$  of sequence  $i$ . The value of the carryover effect for the observed response in the first period is  $\lambda_{c(i,0)} = 0$  since there is no carryover effect in the first period. The intra-subject correlation due to the subject random effect is

$$\rho = \frac{\sigma_b^2}{\sigma_b^2 + \sigma^2}.$$

By constructing the design matrix  $X$  for the linear model with a compound symmetry covariance matrix for the response vector of a subject, we can obtain

$$\text{Var}(\hat{\beta}) = (X'V^{-1}X)^{-1}.$$

The covariance matrix for the direct treatment effects and the carryover treatment effects can be extracted from the appropriate sub-matrices. The covariance matrix for the direct treatment effects without accounting for the carryover treatment effects can be obtained by omitting the carryover effect terms from the model.

The power and relative efficiency are for the direct treatment effect comparing the first treatment to the last treatment accounting for carryover effects.

The degrees of freedom for the t-test can be calculated as the total number of observations minus the number of subjects minus  $p-1$  minus  $2(t-1)$  to account for the subject effect, period effect, and direct and carryover treatment effects.

## Value

An S3 class `designMeanDiffCarryover` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The one-sided significance level.
- `numberOfSubjects`: The maximum number of subjects.
- `meanDiffH0`: The mean difference under the null hypothesis.
- `meanDiff`: The mean difference under the alternative hypothesis.
- `stDev`: The standard deviation for within-subject random error.
- `corr`: The intra-subject correlation due to subject random effect.
- `design`: The crossover design represented by a matrix with rows indexing the sequences, columns indexing the periods, and matrix entries indicating the treatments.
- `nseq`: The number of sequences.
- `nprd`: The number of periods.
- `ntrt`: The number of treatments.
- `cumdrop`: The cumulative dropout rate over periods.
- `V_direct_only`: The covariance matrix for direct treatment effects without accounting for carryover effects.



---

```
getDesignMeanDiffEquiv
```

*Group sequential design for equivalence in two-sample mean difference*

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample mean difference.

### Usage

```
getDesignMeanDiffEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanDiffLower = NA_real_,
  meanDiffUpper = NA_real_,
  meanDiff = 0,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
meanDiffLower	The lower equivalence limit of mean difference.
meanDiffUpper	The upper equivalence limit of mean difference.
meanDiff	The mean difference under the alternative hypothesis.
stDev	The standard deviation.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class `designMeanDiffEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - `attainedAlpha`: The attained significance level.
  - `kMax`: The number of stages.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `meanDiffLower`: The lower equivalence limit of mean difference.
  - `meanDiffUpper`: The upper equivalence limit of mean difference.
  - `meanDiff`: The mean difference under the alternative hypothesis.
  - `stDev`: The standard deviation.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.

- rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyMeanDiffLower: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyMeanDiffUpper: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
    - typeAlphaSpending: The type of alpha spending.
    - parameterAlphaSpending: The parameter value for alpha spending.
    - userAlphaSpending: The user defined alpha spending.
    - spendingTime: The error spending time at each analysis.
    - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
    - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
    - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiffEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanDiffEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))
```



---

getDesignMeanDiffMMRM *Group sequential design for two-sample mean difference from the MMRM model*

---

### Description

Obtains the power and sample size for two-sample mean difference at the last time point from the mixed-model for repeated measures (MMRM) model.

### Usage

```
getDesignMeanDiffMMRM(  
  beta = NA_real_,  
  meanDiffH0 = 0,  
  meanDiff = 0.5,  
  k = 1,  
  t = NA_real_,  
  covar1 = diag(k),  
  covar2 = NA_real_,  
  accrualTime = 0,  
  accrualIntensity = NA_real_,  
  piecewiseSurvivalTime = 0,  
  gamma1 = 0,  
  gamma2 = 0,  
  accrualDuration = NA_real_,  
  allocationRatioPlanned = 1,  
  normalApproximation = TRUE,  
  rounding = TRUE,  
  kMax = 1L,  
  informationRates = NA_real_,  
  efficacyStopping = NA_integer_,  
  futilityStopping = NA_integer_,  
  criticalValues = NA_real_,  
  alpha = 0.025,  
  typeAlphaSpending = "sfOF",  
  parameterAlphaSpending = NA_real_,  
  userAlphaSpending = NA_real_,  
  futilityBounds = NA_real_,  
  typeBetaSpending = "none",  
  parameterBetaSpending = NA_real_,  
  userBetaSpending = NA_real_,  
  spendingTime = NA_real_  
)
```

### Arguments

beta            The type II error.

<code>meanDiffH0</code>	The mean difference at the last time point under the null hypothesis. Defaults to 0.
<code>meanDiff</code>	The mean difference at the last time point under the alternative hypothesis.
<code>k</code>	The number of postbaseline time points.
<code>t</code>	The postbaseline time points.
<code>covar1</code>	The covariance matrix for the repeated measures given baseline for the active treatment group.
<code>covar2</code>	The covariance matrix for the repeated measures given baseline for the control group. If missing, it will be set equal to the covariance matrix for the active treatment group.
<code>accrualTime</code>	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
<code>accrualIntensity</code>	A vector of accrual intensities. One for each accrual time interval.
<code>piecewiseSurvivalTime</code>	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
<code>gamma1</code>	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
<code>gamma2</code>	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group.
<code>accrualDuration</code>	Duration of the enrollment period.
<code>allocationRatioPlanned</code>	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
<code>normalApproximation</code>	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The degrees of freedom for the t-distribution is the total effective sample size minus 2. The exact calculation using the t distribution is only implemented for the fixed design.
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
<code>futilityStopping</code>	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class `designMeanDiffMMRM` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.

- drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
- inflationFactor: The inflation factor (relative to the fixed design).
- numberOfSubjects: The maximum number of subjects.
- studyDuration: The maximum study duration.
- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- expectedStudyDurationH1: The expected study duration under H1.
- expectedStudyDurationH0: The expected study duration under H0.
- accrualDuration: The accrual duration.
- followupTime: The follow-up time.
- fixedFollowup: Whether a fixed follow-up design is used.
- meanDiffH0: The mean difference under H0.
- meanDiff: The mean difference under H1.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyMeanDiff: The efficacy boundaries on the mean difference scale.
  - futilityMeanDiff: The futility boundaries on the mean difference scale.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.

- userBetaSpending: The user defined beta spending.
- spendingTime: The error spending time at each analysis.
- allocationRatioPlanned: The allocation ratio for the active treatment versus control.
- accrualTime: A vector that specifies the starting time of piecewise Poisson enrollment time intervals.
- accrualIntensity: A vector of accrual intensities. One for each accrual time interval.
- piecewiseSurvivalTime: A vector that specifies the starting time of piecewise exponential survival time intervals.
- gamma1: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
- gamma2: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the control group.
- k: The number of postbaseline time points.
- t: The postbaseline time points.
- covar1: The covariance matrix for the repeated measures given baseline for the active treatment group.
- covar2: The covariance matrix for the repeated measures given baseline for the control group.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
# function to generate the AR(1) correlation matrix
ar1_cor <- function(n, corr) {
  exponent <- abs(matrix((1:n) - 1, n, n, byrow = TRUE) - ((1:n) - 1))
  corr^exponent
}

(design1 = getDesignMeanDiffMMRM(
  beta = 0.2,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  k = 4,
  t = c(1,2,3,4),
  covar1 = ar1_cor(4, 0.7),
  accrualIntensity = 10,
  gamma1 = 0.02634013,
  gamma2 = 0.02634013,
  accrualDuration = NA,
  allocationRatioPlanned = 1,
  kMax = 3,
  alpha = 0.025,
```

```
typeAlphaSpending = "sfOF"))
```

---

```
getDesignMeanDiffXO    Group sequential design for mean difference in 2x2 crossover
```

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean difference in 2x2 crossover.

### Usage

```
getDesignMeanDiffXO(
  beta = NA_real_,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
meanDiffH0	The mean difference under the null hypothesis. Defaults to 0.
meanDiff	The mean difference under the alternative hypothesis.
stDev	The standard deviation for within-subject random error.

allocationRatioPlanned	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.

`spendingTime` A vector of length `kMax` for the error spending time at each analysis. Defaults to missing, in which case, it is the same as `informationRates`.

### Value

An S3 class `designMeanDiffXO` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `drift`: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `meanDiffH0`: The mean difference under the null hypothesis.
  - `meanDiff`: The mean difference under the alternative hypothesis.
  - `stDev`: The standard deviation for within-subject random error.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale.
  - `futilityBounds`: The futility boundaries on the Z-scale.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.
  - `efficacyP`: The efficacy boundaries on the p-value scale.
  - `futilityP`: The futility boundaries on the p-value scale.
  - `information`: The cumulative information.
  - `efficacyStopping`: Whether to allow efficacy stopping.
  - `futilityStopping`: Whether to allow futility stopping.
  - `rejectPerStageH0`: The probability for efficacy stopping under H0.
  - `futilityPerStageH0`: The probability for futility stopping under H0.
  - `cumulativeRejectionH0`: The cumulative probability for efficacy stopping under H0.
  - `cumulativeFutilityH0`: The cumulative probability for futility stopping under H0.



- efficacyMeanDiff: The efficacy boundaries on the mean difference scale.
- futilityMeanDiff: The futility boundaries on the mean difference scale.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignMeanDiffXO(
  beta = 0.2, n = NA, meanDiff = 75, stDev = 150,
  normalApproximation = FALSE, alpha = 0.05))
```

---

```
getDesignMeanDiffXOEquiv
```

*Group sequential design for equivalence in mean difference in 2x2 crossover*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in mean difference in 2x2 crossover.

**Usage**

```
getDesignMeanDiffXOEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanDiffLower = NA_real_,
  meanDiffUpper = NA_real_,
  meanDiff = 0,
```

```

stDev = 1,
allocationRatioPlanned = 1,
normalApproximation = TRUE,
rounding = TRUE,
kMax = 1L,
informationRates = NA_real_,
alpha = 0.05,
typeAlphaSpending = "sfOF",
parameterAlphaSpending = NA_real_,
userAlphaSpending = NA_real_,
spendingTime = NA_real_
)

```

### Arguments

<code>beta</code>	The type II error.
<code>n</code>	The total sample size.
<code>meanDiffLower</code>	The lower equivalence limit of mean difference.
<code>meanDiffUpper</code>	The upper equivalence limit of mean difference.
<code>meanDiff</code>	The mean difference under the alternative hypothesis.
<code>stDev</code>	The standard deviation for within-subject random error.
<code>allocationRatioPlanned</code>	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.
<code>normalApproximation</code>	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
<code>alpha</code>	The significance level for each of the two one-sided tests. Defaults to 0.05.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

### Value

An S3 class designMeanDiffXOEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanDiffLower: The lower equivalence limit of mean difference.
  - meanDiffUpper: The upper equivalence limit of mean difference.
  - meanDiff: The mean difference under the alternative hypothesis.
  - stDev: The standard deviation for within-subject random error.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyMeanDiffLower: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyMeanDiffUpper: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.

- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
- rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifengl@gmail.com>

**Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiffXOEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanDiffXOEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignMeanRatio      *Group sequential design for two-sample mean ratio*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean ratio.

**Usage**

```
getDesignMeanRatio(
  beta = NA_real_,
  n = NA_real_,
  meanRatioH0 = 1,
  meanRatio = 1.25,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
```

```

criticalValues = NA_real_,
alpha = 0.025,
typeAlphaSpending = "sfOF",
parameterAlphaSpending = NA_real_,
userAlphaSpending = NA_real_,
futilityBounds = NA_real_,
typeBetaSpending = "none",
parameterBetaSpending = NA_real_,
userBetaSpending = NA_real_,
spendingTime = NA_real_
)

```

### Arguments

beta	The type II error.
n	The total sample size.
meanRatioH0	The mean ratio under the null hypothesis. Defaults to 1.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation. The standard deviation on the log scale is equal to $\sqrt{\log(1 + CV^2)}$ .
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfp" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class designMeanRatio object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanRatioH0: The mean ratio under the null hypothesis.
  - meanRatio: The mean ratio under the alternative hypothesis.
  - CV: The coefficient of variation.
- byStageResults: A data frame containing the following variables:

- informationRates: The information rates.
- efficacyBounds: The efficacy boundaries on the Z-scale.
- futilityBounds: The futility boundaries on the Z-scale.
- rejectPerStage: The probability for efficacy stopping.
- futilityPerStage: The probability for futility stopping.
- cumulativeRejection: The cumulative probability for efficacy stopping.
- cumulativeFutility: The cumulative probability for futility stopping.
- cumulativeAlphaSpent: The cumulative alpha spent.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- numberOfSubjects: The number of subjects.
- efficacyMeanRatio: The efficacy boundaries on the mean ratio scale.
- futilityMeanRatio: The futility boundaries on the mean ratio scale.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
(design1 <- getDesignMeanRatio(
  beta = 0.1, n = NA, meanRatio = 1.25, CV = 0.25,
  alpha = 0.05, normalApproximation = FALSE))
```

---

```
getDesignMeanRatioEquiv
```

*Group sequential design for equivalence in two-sample mean ratio*

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample mean ratio.

### Usage

```
getDesignMeanRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanRatioLower = NA_real_,
  meanRatioUpper = NA_real_,
  meanRatio = 1,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
meanRatioLower	The lower equivalence limit of mean ratio.
meanRatioUpper	The upper equivalence limit of mean ratio.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.



rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class `designMeanRatioEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - `attainedAlpha`: The attained significance level.
  - `kMax`: The number of stages.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `meanRatioLower`: The lower equivalence limit of mean ratio.
  - `meanRatioUpper`: The upper equivalence limit of mean ratio.
  - `meanRatio`: The mean ratio under the alternative hypothesis.
  - `CV`: The coefficient of variation.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.

- rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
  - efficacyMeanRatioLower: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyMeanRatioUpper: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the upper equivalence limit.
- settings: A list containing the following input parameters:
    - typeAlphaSpending: The type of alpha spending.
    - parameterAlphaSpending: The parameter value for alpha spending.
    - userAlphaSpending: The user defined alpha spending.
    - spendingTime: The error spending time at each analysis.
    - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
    - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
    - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanRatioEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanRatioEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignMeanRatioXO *Group sequential design for mean ratio in 2x2 crossover*

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean ratio in 2x2 crossover.

### Usage

```
getDesignMeanRatioXO(
  beta = NA_real_,
  n = NA_real_,
  meanRatioH0 = 1,
  meanRatio = 1.25,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
meanRatioH0	The mean ratio under the null hypothesis. Defaults to 1.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation. The standard deviation on the log scale is equal to $\sqrt{\log(1 + CV^2)}$ .
allocationRatioPlanned	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.

<code>normalApproximation</code>	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
<code>futilityStopping</code>	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level. Defaults to 0.025.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.
<code>futilityBounds</code>	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., $kMax-1$ . Defaults to $rep(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
<code>typeBetaSpending</code>	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
<code>parameterBetaSpending</code>	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
<code>userBetaSpending</code>	The user defined beta spending. Cumulative beta spent up to each stage.
<code>spendingTime</code>	A vector of length $kMax$ for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .

**Value**

An S3 class `designMeanRatioXO` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `drift`: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `meanRatioH0`: The mean ratio under the null hypothesis.
  - `meanRatio`: The mean ratio under the alternative hypothesis.
  - `CV`: The coefficient of variation.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale.
  - `futilityBounds`: The futility boundaries on the Z-scale.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.
  - `efficacyMeanRatio`: The efficacy boundaries on the mean ratio scale.
  - `futilityMeanRatio`: The futility boundaries on the mean ratio scale.
  - `efficacyP`: The efficacy boundaries on the p-value scale.
  - `futilityP`: The futility boundaries on the p-value scale.
  - `information`: The cumulative information.
  - `efficacyStopping`: Whether to allow efficacy stopping.
  - `futilityStopping`: Whether to allow futility stopping.
  - `rejectPerStageH0`: The probability for efficacy stopping under H0.
  - `futilityPerStageH0`: The probability for futility stopping under H0.
  - `cumulativeRejectionH0`: The cumulative probability for efficacy stopping under H0.
  - `cumulativeFutilityH0`: The cumulative probability for futility stopping under H0.
  - `numberOfSubjects`: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
(design1 <- getDesignMeanRatioXO(
  beta = 0.1, n = NA, meanRatio = 1.25, CV = 0.25,
  alpha = 0.05, normalApproximation = FALSE))
```

---

getDesignMeanRatioXOEquiv

*Group sequential design for equivalence in mean ratio in 2x2 crossover*

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence mean ratio in 2x2 crossover.

### Usage

```
getDesignMeanRatioXOEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanRatioLower = NA_real_,
  meanRatioUpper = NA_real_,
  meanRatio = 1,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
```

```

rounding = TRUE,
kMax = 1L,
informationRates = NA_real_,
alpha = 0.05,
typeAlphaSpending = "sfOF",
parameterAlphaSpending = NA_real_,
userAlphaSpending = NA_real_,
spendingTime = NA_real_
)

```

### Arguments

beta	The type II error.
n	The total sample size.
meanRatioLower	The lower equivalence limit of mean ratio.
meanRatioUpper	The upper equivalence limit of mean ratio.
meanRatio	The mean ratio under the alternative hypothesis.
CV	The coefficient of variation.
allocationRatioPlanned	Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

**Value**

An S3 class `designMeanRatioEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level.
  - `kMax`: The number of stages.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `meanRatioLower`: The lower equivalence limit of mean ratio.
  - `meanRatioUpper`: The upper equivalence limit of mean ratio.
  - `meanRatio`: The mean ratio under the alternative hypothesis.
  - `CV`: The coefficient of variation.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha for each of the two one-sided tests.
  - `cumulativeAttainedAlpha`: The cumulative probability for efficacy stopping under H0.
  - `efficacyMeanRatioLower`: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the lower equivalence limit.
  - `efficacyMeanRatioUpper`: The efficacy boundaries on the mean ratio scale for the one-sided null hypothesis on the upper equivalence limit.
  - `efficacyP`: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - `information`: The cumulative information.
  - `numberOfSubjects`: The number of subjects.
- `settings`: A list containing the following input parameters:
  - `typeAlphaSpending`: The type of alpha spending.
  - `parameterAlphaSpending`: The parameter value for alpha spending.
  - `userAlphaSpending`: The user defined alpha spending.
  - `spendingTime`: The error spending time at each analysis.
  - `allocationRatioPlanned`: Allocation ratio for sequence A/B versus sequence B/A.
  - `normalApproximation`: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
  - `rounding`: Whether to round up sample size.



**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanRatioXOEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanRatioXOEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignOddsRatio      *Group sequential design for two-sample odds ratio*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample odds ratio.

**Usage**

```
getDesignOddsRatio(
  beta = NA_real_,
  n = NA_real_,
  oddsRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
```

```

    typeBetaSpending = "none",
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_
  )

```

### Arguments

<code>beta</code>	The type II error.
<code>n</code>	The total sample size.
<code>oddsRatioH0</code>	The odds ratio under the null hypothesis. Defaults to 1.
<code>pi1</code>	The assumed probability for the active treatment group.
<code>pi2</code>	The assumed probability for the control group.
<code>nullVariance</code>	Whether to use the variance under the null or the empirical variance under the alternative.
<code>allocationRatioPlanned</code>	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
<code>futilityStopping</code>	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level. Defaults to 0.025.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to $\text{rep}(-6, \text{kMax}-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class designOddsRatio object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to  $\text{theta} \times \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - oddsRatioH0: The odds ratio under the null hypothesis.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.

- *futilityPerStage*: The probability for futility stopping.
- *cumulativeRejection*: The cumulative probability for efficacy stopping.
- *cumulativeFutility*: The cumulative probability for futility stopping.
- *cumulativeAlphaSpent*: The cumulative alpha spent.
- *efficacyP*: The efficacy boundaries on the p-value scale.
- *futilityP*: The futility boundaries on the p-value scale.
- *information*: The cumulative information.
- *efficacyStopping*: Whether to allow efficacy stopping.
- *futilityStopping*: Whether to allow futility stopping.
- *rejectPerStageH0*: The probability for efficacy stopping under H0.
- *futilityPerStageH0*: The probability for futility stopping under H0.
- *cumulativeRejectionH0*: The cumulative probability for efficacy stopping under H0.
- *cumulativeFutilityH0*: The cumulative probability for futility stopping under H0.
- *efficacyOddsRatio*: The efficacy boundaries on the odds ratio scale.
- *futilityOddsRatio*: The futility boundaries on the odds ratio scale.
- *numberOfSubjects*: The number of subjects.
- *settings*: A list containing the following input parameters:
  - *typeAlphaSpending*: The type of alpha spending.
  - *parameterAlphaSpending*: The parameter value for alpha spending.
  - *userAlphaSpending*: The user defined alpha spending.
  - *typeBetaSpending*: The type of beta spending.
  - *parameterBetaSpending*: The parameter value for beta spending.
  - *userBetaSpending*: The user defined beta spending.
  - *spendingTime*: The error spending time at each analysis.
  - *varianceRatio*: The ratio of the variance under H0 to the variance under H1.
  - *nullVariance*: Whether to use the variance under the null or the empirical variance under the alternative.
  - *allocationRatioPlanned*: Allocation ratio for the active treatment versus control.
  - *rounding*: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignOddsRatio(
  beta = 0.1, n = NA, pi1 = 0.5, pi2 = 0.3,
  alpha = 0.05))
```

---

 getDesignOddsRatioEquiv

*Group sequential design for equivalence in two-sample odds ratio*


---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample odds ratio.

### Usage

```
getDesignOddsRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  oddsRatioLower = NA_real_,
  oddsRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
oddsRatioLower	The lower equivalence limit of odds ratio.
oddsRatioUpper	The upper equivalence limit of odds ratio.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level for each of the two one-sided tests. Defaults to 0.05.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.
<code>spendingTime</code>	A vector of length <code>kMax</code> for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .

## Value

An S3 class `designOddsRatioEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - `attainedAlphaH10`: The attained significance level under H10.
  - `attainedAlphaH20`: The attained significance level under H20.
  - `kMax`: The number of stages.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH10`: The expected information under H10.
  - `expectedInformationH20`: The expected information under H20.
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH10`: The expected number of subjects under H10.
  - `expectedNumberOfSubjectsH20`: The expected number of subjects under H20.
  - `oddsRatioLower`: The lower equivalence limit of odds ratio.
  - `oddsRatioUpper`: The upper equivalence limit of odds ratio.
  - `pi1`: The assumed probability for the active treatment group.
  - `pi2`: The assumed probability for the control group.
  - `oddsRatio`: The odds ratio.

- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha for each of the two one-sided tests.
  - `cumulativeAttainedAlphaH10`: The cumulative alpha attained under H10.
  - `cumulativeAttainedAlphaH20`: The cumulative alpha attained under H20.
  - `efficacyOddsRatioLower`: The efficacy boundaries on the odds ratio scale for the one-sided null hypothesis on the lower equivalence limit.
  - `efficacyOddsRatioUpper`: The efficacy boundaries on the odds ratio scale for the one-sided null hypothesis on the upper equivalence limit.
  - `efficacyP`: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - `information`: The cumulative information.
  - `numberOfSubjects`: The number of subjects.
- `settings`: A list containing the following input parameters:
  - `typeAlphaSpending`: The type of alpha spending.
  - `parameterAlphaSpending`: The parameter value for alpha spending.
  - `userAlphaSpending`: The user defined alpha spending.
  - `spendingTime`: The error spending time at each analysis.
  - `nullVariance`: Whether to use the variance under the null or the empirical variance under the alternative.
  - `varianceRatioH10`: The ratio of the variance under H10 to the variance under H1.
  - `varianceRatioH20`: The ratio of the variance under H20 to the variance under H1.
  - `varianceRatioH12`: The ratio of the variance under H10 to the variance under H20.
  - `varianceRatioH21`: The ratio of the variance under H20 to the variance under H10.
  - `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.
  - `rounding`: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
(design1 <- getDesignOddsRatioEquiv(
  beta = 0.2, n = NA, oddsRatioLower = 0.8,
  oddsRatioUpper = 1.25, pi1 = 0.12, pi2 = 0.12,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))
```

---

getDesignOneMean      *Group sequential design for one-sample mean*

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample mean.

### Usage

```
getDesignOneMean(
  beta = NA_real_,
  n = NA_real_,
  meanH0 = 0,
  mean = 0.5,
  stDev = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
meanH0	The mean under the null hypothesis. Defaults to 0.
mean	The mean under the alternative hypothesis.
stDev	The standard deviation.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.



rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to $\text{rep}(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

### Value

An S3 class `designOneMean` object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanH0: The mean under the null hypothesis.
  - mean: The mean under the alternative hypothesis.
  - stDev: The standard deviation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyMean: The efficacy boundaries on the mean scale.
  - futilityMean: The futility boundaries on the mean scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.

- parameterAlphaSpending: The parameter value for alpha spending.
- userAlphaSpending: The user defined alpha spending.
- typeBetaSpending: The type of beta spending.
- parameterBetaSpending: The parameter value for beta spending.
- userBetaSpending: The user defined beta spending.
- spendingTime: The error spending time at each analysis.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignOneMean(
  beta = 0.1, n = NA, meanH0 = 7, mean = 6, stDev = 2.5,
  kMax = 5, alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignOneMean(
  beta = 0.1, n = NA, meanH0 = 7, mean = 6, stDev = 2.5,
  normalApproximation = FALSE, alpha = 0.025))
```

---

getDesignOneMultinom *Power and sample for one-sample multinomial response*

---

### Description

Obtains the power given sample size or obtains the sample size given power for one-sample multinomial response.

### Usage

```
getDesignOneMultinom(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  piH0 = NA_real_,
  pi = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
ncats	The number of categories of the multinomial response.
piH0	The prevalence of each category under the null hypothesis. Only need to provide the values for the first $ncats-1$ categories.
pi	The prevalence of each category. Only need to provide the values for the first $ncats-1$ categories.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

**Value**

An S3 class `designOneMultinom` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The two-sided significance level.
- `n`: The maximum number of subjects.
- `ncats`: The number of categories of the multinomial response.
- `piH0`: The prevalence of each category under the null hypothesis.
- `pi`: The prevalence of each category.
- `effectsize`: The effect size for the chi-square test.
- `rounding`: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignOneMultinom(
  beta = 0.1, ncats = 3, piH0 = c(0.25, 0.25),
  pi = c(0.3, 0.4), alpha = 0.05))
```

---

```
getDesignOneProportion
```

*Group sequential design for one-sample proportion*

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample proportion.

### Usage

```
getDesignOneProportion(
  beta = NA_real_,
  n = NA_real_,
  piH0 = 0.1,
  pi = 0.2,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
piH0	The response probability under the null hypothesis.
pi	The response probability under the alternative hypothesis.
normalApproximation	The type of computation of the p-values. If TRUE, the normal approximation will be used, otherwise the calculations are performed with the binomial distribution. The exact calculation using the binomial distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
<code>futilityStopping</code>	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level. Defaults to 0.025.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.
<code>futilityBounds</code>	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., $kMax-1$ . Defaults to $rep(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
<code>typeBetaSpending</code>	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
<code>parameterBetaSpending</code>	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
<code>userBetaSpending</code>	The user defined beta spending. Cumulative beta spent up to each stage.
<code>spendingTime</code>	A vector of length $kMax$ for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .

**Value**

An S3 class `designOneProportion` object with three components:

- `overallResults`: A data frame containing the following variables:

- overallReject: The overall rejection probability.
- alpha: The overall significance level.
- attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping as well as for the binomial exact test in a fixed design.
- kMax: The number of stages.
- theta: The parameter value.
- information: The maximum information.
- expectedInformationH1: The expected information under H1.
- expectedInformationH0: The expected information under H0.
- drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
- inflationFactor: The inflation factor (relative to the fixed design).
- numberOfSubjects: The maximum number of subjects.
- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- piH0: The response probability under the null hypothesis.
- pi: The response probability under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyResponses: The efficacy boundaries on the number of responses scale.
  - futilityResponses: The futility boundaries on the number of responses scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.

- typeBetaSpending: The type of beta spending.
- parameterBetaSpending: The parameter value for beta spending.
- userBetaSpending: The user defined beta spending.
- spendingTime: The error spending time at each analysis.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the binomial distribution.
- rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignOneProportion(
  beta = 0.2, n = NA, piH0 = 0.15, pi = 0.25,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sf0F"))

# Example 2: sample size calculation for one-sample binomial exact test
(design2 <- getDesignOneProportion(
  beta = 0.2, n = NA, piH0 = 0.15, pi = 0.25,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignOneRateExact *Power and sample size for one-sample Poisson rate exact test*

---

### Description

Obtains the power given sample size or obtains the sample size given power for one-sample Poisson rate.

### Usage

```
getDesignOneRateExact(
  beta = NA_real_,
  n = NA_real_,
  lambdaH0 = NA_real_,
  lambda = NA_real_,
  D = 1,
  alpha = 0.025
)
```



**Arguments**

beta	The type II error.
n	The total sample size.
lambdaH0	The Poisson rate under the null hypothesis.
lambda	The Poisson rate under the alternative hypothesis.
D	The average exposure per subject.
alpha	The one-sided significance level. Defaults to 0.025.

**Value**

A data frame containing the following variables:

- alpha: The specified significance level.
- attainedAlpha: The attained type I error of the exact test.
- power: The actual power of the exact test.
- n: The sample size.
- lambdaH0: The Poisson rate under the null hypothesis.
- lambda: The Poisson rate under the alternative hypothesis.
- D: The average exposure per subject.
- r: The critical value of the number of events for rejecting the null hypothesis. Reject H0 if  $Y \geq r$  for upper-tailed test, and reject H0 if  $Y \leq r$  for lower-tailed test.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: power calculation
(design1 <- getDesignOneRateExact(
  n = 525, lambdaH0 = 0.049, lambda = 0.012,
  D = 0.5, alpha = 0.025))

# Example 2: sample size calculation
(design2 <- getDesignOneRateExact(
  beta = 0.2, lambdaH0 = 0.2, lambda = 0.3,
  D = 1, alpha = 0.05))
```

---

getDesignOneSlope      *Group sequential design for one-sample slope*

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample slope.

### Usage

```
getDesignOneSlope(
  beta = NA_real_,
  n = NA_real_,
  slopeH0 = 0,
  slope = 0.5,
  stDev = 1,
  stDevCovariate = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
slopeH0	The slope under the null hypothesis. Defaults to 0.
slope	The slope under the alternative hypothesis.
stDev	The standard deviation of the residual.
stDevCovariate	The standard deviation of the covariate.

normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to $\text{rep}(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

**Value**

An S3 class `designOneSlope` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `drift`: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `slopeH0`: The slope under the null hypothesis.
  - `slope`: The slope under the alternative hypothesis.
  - `stDev`: The standard deviation of the residual.
  - `stDevCovariate`: The standard deviation of the covariate.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale.
  - `futilityBounds`: The futility boundaries on the Z-scale.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.
  - `efficacyP`: The efficacy boundaries on the p-value scale.
  - `futilityP`: The futility boundaries on the p-value scale.
  - `information`: The cumulative information.
  - `efficacyStopping`: Whether to allow efficacy stopping.
  - `futilityStopping`: Whether to allow futility stopping.
  - `rejectPerStageH0`: The probability for efficacy stopping under H0.
  - `futilityPerStageH0`: The probability for futility stopping under H0.
  - `cumulativeRejectionH0`: The cumulative probability for efficacy stopping under H0.
  - `cumulativeFutilityH0`: The cumulative probability for futility stopping under H0.
  - `efficacySlope`: The efficacy boundaries on the slope scale.
  - `futilitySlope`: The futility boundaries on the slope scale.

- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignOneSlope(
  beta = 0.1, n = NA, slope = 0.5,
  stDev = 15, stDevCovariate = 9,
  normalApproximation = FALSE,
  alpha = 0.025))
```

---

getDesignOrderedBinom *Power and sample size for Cochran-Armitage trend test for ordered multi-sample binomial response*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for the Cochran-Armitage trend test for ordered multi-sample binomial response.

**Usage**

```
getDesignOrderedBinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  pi = NA_real_,
  w = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
pi	The response probabilities for the treatment groups.
w	The scores assigned to the treatment groups. This should reflect the ordinal nature of the treatment groups, e.g. dose levels. Defaults to equally spaced scores.
allocationRatioPlanned	Allocation ratio for the treatment groups.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

**Value**

An S3 class `designOrderedBinom` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The two-sided significance level.
- `n`: The maximum number of subjects.
- `ngroups`: The number of treatment groups.
- `pi`: The response probabilities for the treatment groups.
- `w`: The scores assigned to the treatment groups.
- `trendstat`: The Cochran-Armitage trend test statistic.
- `allocationRatioPlanned`: Allocation ratio for the treatment groups.
- `rounding`: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignOrderedBinom(
  beta = 0.1, ngroups = 3, pi = c(0.1, 0.25, 0.5), alpha = 0.05))
```

---

 getDesignPairedMeanDiff

*Group sequential design for paired mean difference*


---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for paired mean difference.

### Usage

```
getDesignPairedMeanDiff(
  beta = NA_real_,
  n = NA_real_,
  pairedDiffH0 = 0,
  pairedDiff = 0.5,
  stDev = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
pairedDiffH0	The paired difference under the null hypothesis. Defaults to 0.
pairedDiff	The paired difference under the alternative hypothesis.
stDev	The standard deviation for paired difference.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
<code>futilityStopping</code>	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level. Defaults to 0.025.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.
<code>futilityBounds</code>	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., $kMax-1$ . Defaults to $rep(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
<code>typeBetaSpending</code>	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
<code>parameterBetaSpending</code>	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
<code>userBetaSpending</code>	The user defined beta spending. Cumulative beta spent up to each stage.
<code>spendingTime</code>	A vector of length $kMax$ for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .

**Value**

An S3 class `designPairedMeanDiff` object with three components:



- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedDiffH0: The paired difference under the null hypothesis.
  - pairedDiff: The paired difference under the alternative hypothesis.
  - stDev: The standard deviation for paired difference.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyPairedDiff: The efficacy boundaries on the paired difference scale.
  - futilityPairedDiff: The futility boundaries on the paired difference scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.

- parameterAlphaSpending: The parameter value for alpha spending.
- userAlphaSpending: The user defined alpha spending.
- typeBetaSpending: The type of beta spending.
- parameterBetaSpending: The parameter value for beta spending.
- userBetaSpending: The user defined beta spending.
- spendingTime: The error spending time at each analysis.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanDiff(
  beta = 0.1, n = NA, pairedDiffH0 = 0, pairedDiff = -2, stDev = 5,
  kMax = 5, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignPairedMeanDiff(
  beta = 0.1, n = NA, pairedDiffH0 = 0, pairedDiff = -2, stDev = 5,
  normalApproximation = FALSE, alpha = 0.025))
```

---

`getDesignPairedMeanDiffEquiv`

*Group sequential design for equivalence in paired mean difference*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in paired mean difference.

**Usage**

```
getDesignPairedMeanDiffEquiv(
  beta = NA_real_,
  n = NA_real_,
  pairedDiffLower = NA_real_,
  pairedDiffUpper = NA_real_,
  pairedDiff = 0,
  stDev = 1,
  normalApproximation = TRUE,
```

```

    rounding = TRUE,
    kMax = 1L,
    informationRates = NA_real_,
    alpha = 0.05,
    typeAlphaSpending = "sfOF",
    parameterAlphaSpending = NA_real_,
    userAlphaSpending = NA_real_,
    spendingTime = NA_real_
  )

```

### Arguments

beta	The type II error.
n	The total sample size.
pairedDiffLower	The lower equivalence limit of paired difference.
pairedDiffUpper	The upper equivalence limit of paired difference.
pairedDiff	The paired difference under the alternative hypothesis.
stDev	The standard deviation for paired difference.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

**Value**

An S3 class `designPairedMeanDiffEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - `attainedAlpha`: The attained significance level under  $H_0$ .
  - `kMax`: The number of stages.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under  $H_1$ .
  - `expectedInformationH0`: The expected information under  $H_0$ .
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under  $H_1$ .
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under  $H_0$ .
  - `pairedDiffLower`: The lower equivalence limit of paired difference.
  - `pairedDiffUpper`: The upper equivalence limit of paired difference.
  - `pairedDiff`: The paired difference under the alternative hypothesis.
  - `stDev`: The standard deviation for paired difference.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha for each of the two one-sided tests.
  - `cumulativeAttainedAlpha`: The cumulative probability for efficacy stopping under  $H_0$ .
  - `efficacyPairedDiffLower`: The efficacy boundaries on the paired difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - `efficacyPairedDiffUpper`: The efficacy boundaries on the paired difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - `efficacyP`: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - `information`: The cumulative information.
  - `numberOfSubjects`: The number of subjects.
- `settings`: A list containing the following input parameters:
  - `typeAlphaSpending`: The type of alpha spending.
  - `parameterAlphaSpending`: The parameter value for alpha spending.
  - `userAlphaSpending`: The user defined alpha spending.
  - `spendingTime`: The error spending time at each analysis.
  - `normalApproximation`: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
  - `rounding`: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanDiffEquiv(
  beta = 0.1, n = NA, pairedDiffLower = -1.3, pairedDiffUpper = 1.3,
  pairedDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignPairedMeanDiffEquiv(
  beta = 0.1, n = NA, pairedDiffLower = -1.3, pairedDiffUpper = 1.3,
  pairedDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignPairedMeanRatio

*Group sequential design for paired mean ratio*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for paired mean ratio.

**Usage**

```
getDesignPairedMeanRatio(
  beta = NA_real_,
  n = NA_real_,
  pairedRatioH0 = 1,
  pairedRatio = 1.2,
  CV = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
```

```

    typeBetaSpending = "none",
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_
  )

```

### Arguments

<code>beta</code>	The type II error.
<code>n</code>	The total sample size.
<code>pairedRatioH0</code>	The paired ratio under the null hypothesis.
<code>pairedRatio</code>	The paired ratio under the alternative hypothesis.
<code>CV</code>	The coefficient of variation for paired ratio.
<code>normalApproximation</code>	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
<code>futilityStopping</code>	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level. Defaults to 0.025.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.
<code>futilityBounds</code>	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., $kMax-1$ . Defaults to $rep(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class designPairedMeanRatio object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedRatioH0: The paired ratio under the null hypothesis.
  - pairedRatio: The paired ratio under the alternative hypothesis.
  - CV: The coefficient of variation for paired ratio.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.

- cumulativeAlphaSpent: The cumulative alpha spent.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- numberOfSubjects: The number of subjects.
- efficacyPairedRatio: The efficacy boundaries on the paired ratio scale.
- futilityPairedRatio: The futility boundaries on the paired ratio scale.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanRatio(
  beta = 0.1, n = NA, pairedRatio = 1.2, CV = 0.35,
  kMax = 5, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignPairedMeanRatio(
  beta = 0.1, n = NA, pairedRatio = 1.2, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```



---

```
getDesignPairedMeanRatioEquiv
```

*Group sequential design for equivalence in paired mean ratio*

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in paired mean ratio.

### Usage

```
getDesignPairedMeanRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  pairedRatioLower = NA_real_,
  pairedRatioUpper = NA_real_,
  pairedRatio = 1,
  CV = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### Arguments

beta	The type II error.
n	The total sample size.
pairedRatioLower	The lower equivalence limit of paired ratio.
pairedRatioUpper	The upper equivalence limit of paired ratio.
pairedRatio	The paired ratio under the alternative hypothesis.
CV	The coefficient of variation for paired ratio.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.

<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>alpha</code>	The significance level for each of the two one-sided tests. Defaults to 0.05.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.
<code>spendingTime</code>	A vector of length <code>kMax</code> for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .

## Value

An S3 class `designPairedMeanRatioEquiv` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - `attainedAlpha`: The attained significance level under  $H_0$ .
  - `kMax`: The number of stages.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under  $H_1$ .
  - `expectedInformationH0`: The expected information under  $H_0$ .
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under  $H_1$ .
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under  $H_0$ .
  - `pairedRatioLower`: The lower equivalence limit of paired ratio.
  - `pairedRatioUpper`: The upper equivalence limit of paired ratio.
  - `pairedRatio`: The paired ratio under the alternative hypothesis.
  - `CV`: The coefficient of variation for paired ratios.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.

- cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
- cumulativeAttainedAlpha: The cumulative alpha attained under H0.
- efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
- information: The cumulative information.
- numberOfSubjects: The number of subjects.
- efficacyPairedRatioLower: The efficacy boundaries on the paired ratio scale for the one-sided null hypothesis on the lower equivalence limit.
- efficacyPairedRatioUpper: The efficacy boundaries on the paired ratio scale for the one-sided null hypothesis on the upper equivalence limit.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanRatioEquiv(
  beta = 0.1, n = NA, pairedRatioLower = 0.8, pairedRatioUpper = 1.25,
  pairedRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sf0F"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignPairedMeanRatioEquiv(
  beta = 0.1, n = NA, pairedRatioLower = 0.8, pairedRatioUpper = 1.25,
  pairedRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))
```

---

getDesignPairedPropMcNemar

*Group sequential design for McNemar's test for paired proportions*

---

### Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for McNemar's test for paired proportions.

**Usage**

```

getDesignPairedPropMcNemar(
  beta = NA_real_,
  n = NA_real_,
  pDiscordant = NA_real_,
  riskDiff = NA_real_,
  nullVariance = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)

```

**Arguments**

beta	The type II error.
n	The total sample size.
pDiscordant	The proportion of discordant pairs ( $\xi = \pi_{01} + \pi_{10}$ ).
riskDiff	The risk difference between the active and control treatments ( $\delta = \pi_{1t} - \pi_{1c} = \pi_{01} - \pi_{10}$ ).
nullVariance	Whether to use the variance under the null or the variance under the alternative.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.

typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class designPairedPropMcNemar object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.

- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- pDiscordant: The proportion of discordant pairs ( $\xi = \pi_{01} + \pi_{10}$ ).
- riskDiff: The risk difference between the active and control treatments ( $\delta = \pi_t - \pi_c = \pi_{01} - \pi_{10}$ )
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyRiskDiff: The efficacy boundaries on the risk difference scale.
  - futilityRiskDiff: The futility boundaries on the risk difference scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, &lt;kaifenglu@gmail.com&gt;

**Examples**

```
# Example 1: fixed design
(design1 <- getDesignPairedPropMcNemar(
  beta = 0.1, n = NA, pDiscordant = 0.16, riskDiff = 0.1,
  alpha = 0.025))

# Example 2: group sequential design
(design2 <- getDesignPairedPropMcNemar(
  beta = 0.1, n = NA, pDiscordant = 0.16, riskDiff = 0.1,
  alpha = 0.025, kMax = 3, typeAlphaSpending = "sfOF"))
```

---

```
getDesignRepeatedANOVA
```

*Power and sample size for repeated-measures ANOVA*

---

**Description**

Obtains the power and sample size for one-way repeated measures analysis of variance. Each subject takes all treatments in the longitudinal study.

**Usage**

```
getDesignRepeatedANOVA(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  corr = 0,
  rounding = TRUE,
  alpha = 0.05
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The total standard deviation.
corr	The correlation among the repeated measures.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

### Details

Let  $y_{ij}$  denote the measurement under treatment condition  $j$  ( $j = 1, \dots, k$ ) for subject  $i$  ( $i = 1, \dots, n$ ). Then

$$y_{ij} = \alpha + \beta_j + b_i + e_{ij},$$

where  $b_i$  denotes the subject random effect,  $b_i \sim N(0, \sigma_b^2)$ , and  $e_{ij} \sim N(0, \sigma_e^2)$  denotes the within-subject residual. If we set  $\beta_k = 0$ , then  $\alpha$  is the mean of the last treatment (control), and  $\beta_j$  is the difference in means between the  $j$ th treatment and the control for  $j = 1, \dots, k-1$ .

The repeated measures have a compound symmetry covariance structure. Let  $\sigma^2 = \sigma_b^2 + \sigma_e^2$ , and  $\rho = \frac{\sigma_b^2}{\sigma_b^2 + \sigma_e^2}$ . Then  $\text{Var}(y_i) = \sigma^2\{(1-\rho)I_k + \rho\mathbf{1}_k\mathbf{1}_k^T\}$ . Let  $X_i$  denote the design matrix for subject  $i$ . Let  $\theta = (\alpha, \beta_1, \dots, \beta_{k-1})^T$ . It follows that

$$\text{Var}(\hat{\theta}) = \left( \sum_{i=1}^n X_i^T V_i^{-1} X_i \right)^{-1}.$$

It can be shown that

$$\text{Var}(\hat{\beta}) = \frac{\sigma^2(1-\rho)}{n} (I_{k-1} + \mathbf{1}_{k-1}\mathbf{1}_{k-1}^T).$$

It follows that  $\hat{\beta}^T \hat{V}_{\hat{\beta}}^{-1} \hat{\beta} \sim F_{k-1, (n-1)(k-1), \lambda}$ , where the noncentrality parameter for the  $F$  distribution is

$$\lambda = \beta^T V_{\hat{\beta}}^{-1} \beta = \frac{n \sum_{j=1}^k (\mu_j - \bar{\mu})^2}{\sigma^2(1-\rho)}.$$

### Value

An S3 class `designRepeatedANOVA` object with the following components:

- `power`: The power to reject the null hypothesis that there is no difference among the treatment groups.
- `alpha`: The two-sided significance level.
- `n`: The number of subjects.
- `ngroups`: The number of treatment groups.
- `means`: The treatment group means.
- `stDev`: The total standard deviation.
- `corr`: The correlation among the repeated measures.
- `effectsize`: The effect size.
- `rounding`: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>



**Examples**

```
(design1 <- getDesignRepeatedANOVA(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 5, corr = 0.2, alpha = 0.05))
```

---

```
getDesignRepeatedANOVAContrast
```

*Power and sample size for one-way repeated measures ANOVA contrast*

---

**Description**

Obtains the power and sample size for a single contrast in one-way repeated measures analysis of variance.

**Usage**

```
getDesignRepeatedANOVAContrast(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  corr = 0,
  contrast = NA_real_,
  meanContrastH0 = 0,
  rounding = TRUE,
  alpha = 0.025
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The total standard deviation.
corr	The correlation among the repeated measures.
contrast	The coefficients for the single contrast.
meanContrastH0	The mean of the contrast under the null hypothesis.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

**Value**

An S3 class `designRepeatedANOVAContrast` object with the following components:

- `power`: The power to reject the null hypothesis for the treatment contrast.
- `alpha`: The one-sided significance level.
- `n`: The number of subjects.
- `ngroups`: The number of treatment groups.
- `means`: The treatment group means.
- `stDev`: The total standard deviation.
- `corr`: The correlation among the repeated measures.
- `contrast`: The coefficients for the single contrast.
- `meanContrastH0`: The mean of the contrast under the null hypothesis.
- `meanContrast`: The mean of the contrast under the alternative hypothesis.
- `effectsize`: The effect size.
- `rounding`: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignRepeatedANOVAContrast(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 5, corr = 0.2, contrast = c(1, 1, 1, -3)/3,
  alpha = 0.025))
```

---

`getDesignRiskDiff`      *Group sequential design for two-sample risk difference*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk difference.

**Usage**

```

getDesignRiskDiff(
  beta = NA_real_,
  n = NA_real_,
  riskDiffH0 = 0,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)

```

**Arguments**

beta	The type II error.
n	The total sample size.
riskDiffH0	The risk difference under the null hypothesis. Defaults to 0.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

<code>futilityStopping</code>	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level. Defaults to 0.025.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.
<code>futilityBounds</code>	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., <code>kMax-1</code> . Defaults to <code>rep(-6, kMax-1)</code> if left unspecified. The futility bounds are non-binding for the calculation of critical values.
<code>typeBetaSpending</code>	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
<code>parameterBetaSpending</code>	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
<code>userBetaSpending</code>	The user defined beta spending. Cumulative beta spent up to each stage.
<code>spendingTime</code>	A vector of length <code>kMax</code> for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .

## Value

An S3 class `designRiskDiff` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.

- expectedInformationH1: The expected information under H1.
- expectedInformationH0: The expected information under H0.
- drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
- inflationFactor: The inflation factor (relative to the fixed design).
- numberOfSubjects: The maximum number of subjects.
- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- riskDiffH0: The risk difference under the null hypothesis.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyRiskDiff: The efficacy boundaries on the risk difference scale.
  - futilityRiskDiff: The futility boundaries on the risk difference scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignRiskDiff(
  beta = 0.2, n = NA, pi1 = 0.1, pi2 = 0.15,
  kMax = 3, alpha = 0.025, typeAlphaSpending = "sfOF",
  nullVariance = 0))
```

---

```
getDesignRiskDiffEquiv
```

*Group sequential design for equivalence in two-sample risk difference*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample risk difference.

**Usage**

```
getDesignRiskDiffEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskDiffLower = NA_real_,
  riskDiffUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

**Arguments**

beta	The type II error.
n	The total sample size.

riskDiffLower	The lower equivalence limit of risk difference.
riskDiffUpper	The upper equivalence limit of risk difference.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class designRiskDiffEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH10: The expected information under H10.

- expectedInformationH20: The expected information under H20.
- numberOfSubjects: The maximum number of subjects.
- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH10: The expected number of subjects under H10.
- expectedNumberOfSubjectsH20: The expected number of subjects under H20.
- riskDiffLower: The lower equivalence limit of risk difference.
- riskDiffUpper: The upper equivalence limit of risk difference.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- riskDiff: The risk difference.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - efficacyRiskDiffLower: The efficacy boundaries on the risk difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyRiskDiffUpper: The efficacy boundaries on the risk difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifengl@gmail.com>



## Examples

```
(design1 <- getDesignRiskDiffEquiv(  
  beta = 0.2, n = NA, riskDiffLower = -0.1,  
  riskDiffUpper = 0.1, pi1 = 0.12, pi2 = 0.12,  
  nullVariance = 1,  
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sf0F"))
```

---

getDesignRiskDiffExact

*Power and sample size for exact unconditional test for risk difference*

---

## Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of risk difference.

## Usage

```
getDesignRiskDiffExact(  
  beta = NA_real_,  
  n = NA_real_,  
  riskDiffH0 = 0,  
  pi1 = NA_real_,  
  pi2 = NA_real_,  
  allocationRatioPlanned = 1,  
  alpha = 0.025  
)
```

## Arguments

beta	The type II error.
n	The total sample size.
riskDiffH0	The risk difference under the null hypothesis. Defaults to 0.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The one-sided significance level. Defaults to 0.025.

**Value**

A data frame with the following variables:

- alpha: The specified one-sided significance level.
- attainedAlpha: The attained one-sided significance level.
- power: The power.
- n: The sample size.
- riskDiffH0: The risk difference under the null hypothesis.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskDiffBound: The critical value on the scale of score test statistic for risk difference.
- pi2star: The response probability in the control group at which the critical value of the test statistic is attained.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Superiority test
getDesignRiskDiffExact(n = 50, pi1 = 0.6, pi2 = 0.25, alpha = 0.025)

# Non-inferiority test
getDesignRiskDiffExact(beta = 0.1, riskDiffH0 = -0.2,
  pi1 = 0.8, pi2 = 0.8, alpha = 0.025)
```

---

getDesignRiskDiffExactEquiv

*Power and sample size for exact unconditional test for equivalence in risk difference*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of equivalence in risk difference.

**Usage**

```
getDesignRiskDiffExactEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskDiffLower = NA_real_,
  riskDiffUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
riskDiffLower	The lower equivalence limit of risk difference.
riskDiffUpper	The upper equivalence limit of risk difference.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.

**Value**

A data frame with the following variables:

- alpha: The specified significance level for each of the two one-sided tests.
- attainedAlpha: The attained significance level.
- power: The power.
- n: The sample size.
- riskDiffLower: The lower equivalence limit of risk difference.
- riskDiffUpper: The upper equivalence limit of risk difference.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- riskDiff: The risk difference.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskDiffLower: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the lower equivalence limit.
- zstatRiskDiffUpper: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the upper equivalence limit.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
getDesignRiskDiffExactEquiv(
  n = 200, riskDiffLower = -0.2, riskDiffUpper = 0.2,
  pi1 = 0.775, pi2 = 0.775, alpha = 0.05)
```

---

getDesignRiskRatio      *Group sequential design for two-sample risk ratio*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk ratio.

**Usage**

```
getDesignRiskRatio(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to $rep(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

**Value**

An S3 class `designRiskRatio` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `drift`: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numberOfSubjects`: The maximum number of subjects.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `riskRatioH0`: The risk ratio under the null hypothesis.
  - `pi1`: The assumed probability for the active treatment group.
  - `pi2`: The assumed probability for the control group.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale.
  - `futilityBounds`: The futility boundaries on the Z-scale.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.
  - `efficacyP`: The efficacy boundaries on the p-value scale.
  - `futilityP`: The futility boundaries on the p-value scale.
  - `information`: The cumulative information.
  - `efficacyStopping`: Whether to allow efficacy stopping.
  - `futilityStopping`: Whether to allow futility stopping.

- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- efficacyRiskRatio: The efficacy boundaries on the risk ratio scale.
- futilityRiskRatio: The futility boundaries on the risk ratio scale.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignRiskRatio(
  beta = 0.1, n = NA, pi1 = 0.5, pi2 = 0.3,
  alpha = 0.05))
```

---

getDesignRiskRatioEquiv

*Group sequential design for equivalence in two-sample risk ratio*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample risk ratio.

**Usage**

```

getDesignRiskRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskRatioLower = NA_real_,
  riskRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)

```

**Arguments**

<code>beta</code>	The type II error.
<code>n</code>	The total sample size.
<code>riskRatioLower</code>	The lower equivalence limit of risk ratio.
<code>riskRatioUpper</code>	The upper equivalence limit of risk ratio.
<code>pi1</code>	The assumed probability for the active treatment group.
<code>pi2</code>	The assumed probability for the control group.
<code>nullVariance</code>	Whether to use the variance under the null or the empirical variance under the alternative.
<code>allocationRatioPlanned</code>	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level for each of the two one-sided tests. Defaults to 0.05.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries,



"sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class designRiskRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH10: The expected information under H10.
  - expectedInformationH20: The expected information under H20.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH10: The expected number of subjects under H10.
  - expectedNumberOfSubjectsH20: The expected number of subjects under H20.
  - riskRatioLower: The lower equivalence limit of risk ratio.
  - riskRatioUpper: The upper equivalence limit of risk ratio.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
  - riskRatio: The risk ratio.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.

- efficacyRiskRatioLower: The efficacy boundaries on the risk ratio scale for the one-sided null hypothesis on the lower equivalence limit.
- efficacyRiskRatioUpper: The efficacy boundaries on the risk ratio scale for the one-sided null hypothesis on the upper equivalence limit.
- efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
- information: The cumulative information.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
(design1 <- getDesignRiskRatioEquiv(
  beta = 0.2, n = NA, riskRatioLower = 0.8,
  riskRatioUpper = 1.25, pi1 = 0.12, pi2 = 0.12,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))
```

---

getDesignRiskRatioExact

*Power and sample size for exact unconditional test for risk ratio*

---

### Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of risk ratio.

**Usage**

```
getDesignRiskRatioExact(  
  beta = NA_real_,  
  n = NA_real_,  
  riskRatioH0 = 1,  
  pi1 = NA_real_,  
  pi2 = NA_real_,  
  allocationRatioPlanned = 1,  
  alpha = 0.025  
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 0.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The one-sided significance level. Defaults to 0.025.

**Value**

A data frame with the following variables:

- alpha: The specified one-sided significance level.
- attainedAlpha: The attained one-sided significance level.
- power: The power.
- n: The sample size.
- riskRatioH0: The risk ratio under the null hypothesis.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskRatioBound: The critical value on the scale of score test statistic for risk ratio.
- pi2star: The response probability in the control group at which the critical value of the test statistic is attained.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Non-inferiority test

getDesignRiskRatioExact(beta = 0.1, riskRatioH0 = 0.833,
                        pi1 = 0.9, pi2 = 0.9, alpha = 0.025)
```

---

```
getDesignRiskRatioExactEquiv
```

*Power and sample size for exact unconditional test for equivalence in risk ratio*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of equivalence in risk ratio.

**Usage**

```
getDesignRiskRatioExactEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskRatioLower = NA_real_,
  riskRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
riskRatioLower	The lower equivalence limit of risk ratio.
riskRatioUpper	The upper equivalence limit of risk ratio.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.

**Value**

A data frame with the following variables:

- alpha: The specified significance level for each of the two one-sided tests.
- attainedAlpha: The attained significance level.
- power: The power.
- n: The sample size.
- riskRatioLower: The lower equivalence limit of risk ratio.
- riskRatioUpper: The upper equivalence limit of risk ratio.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- riskRatio: The risk ratio.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskRatioLower: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the lower equivalence limit.
- zstatRiskRatioUpper: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the upper equivalence limit.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
getDesignRiskRatioExactEquiv(  
  n = 200, riskRatioLower = 0.8, riskRatioUpper = 1.25,  
  pi1 = 0.775, pi2 = 0.775, alpha = 0.05)
```

---

getDesignRiskRatioFM    *Group sequential design for two-sample risk ratio based on the  
Farrington-Manning score test*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk ratio based on the Farrington-Manning score test

**Usage**

```

getDesignRiskRatioFM(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)

```

**Arguments**

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class `designRiskRatioFM` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.

- expectedInformationH1: The expected information under H1.
- expectedInformationH0: The expected information under H0.
- drift: The drift parameter, equal to  $\theta * \sqrt{\text{information}}$ .
- inflationFactor: The inflation factor (relative to the fixed design).
- numberOfSubjects: The maximum number of subjects.
- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- riskRatioH0: The risk ratio under the null hypothesis.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyRiskRatioScore: The efficacy boundaries on the score test  $\pi_1 - \text{riskRatioH0} * \pi_2$  scale.
  - futilityRiskRatioScore: The futility boundaries on the score test  $\pi_1 - \text{riskRatioH0} * \pi_2$  scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.



- nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignRiskRatioFM(
  beta = 0.2, riskRatioH0 = 1.3, pi1 = 0.125, pi2 = 0.125,
  alpha = 0.05))
```

---

getDesignSlopeDiff      *Group sequential design for two-sample slope difference*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample slope difference.

**Usage**

```
getDesignSlopeDiff(
  beta = NA_real_,
  n = NA_real_,
  slopeDiffH0 = 0,
  slopeDiff = 0.5,
  stDev = 1,
  stDevCovariate = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
```

```

    typeBetaSpending = "none",
    parameterBetaSpending = NA_real_,
    userBetaSpending = NA_real_,
    spendingTime = NA_real_
  )

```

## Arguments

beta	The type II error.
n	The total sample size.
slopeDiffH0	The slope difference under the null hypothesis. Defaults to 0.
slopeDiff	The slope difference under the alternative hypothesis.
stDev	The standard deviation of the residual.
stDevCovariate	The standard deviation of the covariate.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
normalApproximation	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
kMax	The maximum number of stages.
informationRates	The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfp" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class designSlopeDiff object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - slopeDiffH0: The slope difference under the null hypothesis.
  - slopeDiff: The slope difference under the alternative hypothesis.
  - stDev: The standard deviation of the residual.
  - stDevCovariate: The standard deviation of the covariate.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.

- efficacyBounds: The efficacy boundaries on the Z-scale.
- futilityBounds: The futility boundaries on the Z-scale.
- rejectPerStage: The probability for efficacy stopping.
- futilityPerStage: The probability for futility stopping.
- cumulativeRejection: The cumulative probability for efficacy stopping.
- cumulativeFutility: The cumulative probability for futility stopping.
- cumulativeAlphaSpent: The cumulative alpha spent.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- efficacySlopeDiff: The efficacy boundaries on the slope difference scale.
- futilitySlopeDiff: The futility boundaries on the slope difference scale.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifengl@gmail.com>

**Examples**

```
(design1 <- getDesignSlopeDiff(
  beta = 0.1, n = NA, slopeDiff = -0.5,
  stDev = 10, stDevCovariate = 6,
  normalApproximation = FALSE, alpha = 0.025))
```

---

`getDesignSlopeDiffMMRM`

*Group sequential design for two-sample slope difference from the MMRM model*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for two-sample slope difference from the growth curve MMRM model.

**Usage**

```
getDesignSlopeDiffMMRM(  
  beta = NA_real_,  
  slopeDiffH0 = 0,  
  slopeDiff = 0.5,  
  stDev = 1,  
  stDevIntercept = 1,  
  stDevSlope = 1,  
  corrInterceptSlope = 0.5,  
  w = NA_real_,  
  N = NA_real_,  
  accrualTime = 0,  
  accrualIntensity = NA_real_,  
  piecewiseSurvivalTime = 0,  
  gamma1 = 0,  
  gamma2 = 0,  
  accrualDuration = NA_real_,  
  followupTime = NA_real_,  
  allocationRatioPlanned = 1,  
  normalApproximation = TRUE,  
  rounding = TRUE,  
  kMax = 1L,  
  informationRates = NA_real_,  
  efficacyStopping = NA_integer_,  
  futilityStopping = NA_integer_,  
  criticalValues = NA_real_,  
  alpha = 0.025,  
  typeAlphaSpending = "sfOF",  
  parameterAlphaSpending = NA_real_,  
  userAlphaSpending = NA_real_,  
  futilityBounds = NA_real_,  
  typeBetaSpending = "none",  
  parameterBetaSpending = NA_real_,  
  userBetaSpending = NA_real_,  
  spendingTime = NA_real_  
)
```

**Arguments**

<code>beta</code>	The type II error.
<code>slopeDiffH0</code>	The slope difference under the null hypothesis. Defaults to 0.
<code>slopeDiff</code>	The slope difference under the alternative hypothesis.
<code>stDev</code>	The standard deviation of the residual.
<code>stDevIntercept</code>	The standard deviation of the random intercept.
<code>stDevSlope</code>	The standard deviation of the random slope.
<code>corrInterceptSlope</code>	The correlation between the random intercept and random slope.
<code>w</code>	The number of time units per measurement visit in a period.
<code>N</code>	The number of measurement visits in a period.
<code>accrualTime</code>	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
<code>accrualIntensity</code>	A vector of accrual intensities. One for each accrual time interval.
<code>piecewiseSurvivalTime</code>	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
<code>gamma1</code>	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
<code>gamma2</code>	The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group.
<code>accrualDuration</code>	Duration of the enrollment period.
<code>followupTime</code>	Follow-up time for the last enrolled subject.
<code>allocationRatioPlanned</code>	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
<code>normalApproximation</code>	The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The degrees of freedom for the t-distribution for testing the slope difference is calculated using the containment method, and is equal to the total number of observations minus two times the total number of subjects. The exact calculation using the t distribution is only implemented for the fixed design.
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Details

We use the following random-effects model to compare two slopes:

$$y_{ij} = \alpha + (\beta + \gamma x_i)t_j + a_i + b_i t_j + e_{ij},$$

where

- $\alpha$ : overall intercept common across treatment groups due to randomization
- $\beta$ : slope for the control group
- $\gamma$ : difference in slopes between the active treatment and control groups
- $x_i$ : treatment indicator for subject  $i$ , 1 for the active treatment and 0 for the control

- $t_j$ : time point  $j$  for repeated measurements,  $t_1 = 0 < t_2 < \dots < t_k$
- $(a_i, b_i)$ : random intercept and random slope for subject  $i$ ,  $Var(a_i) = \sigma_a^2$ ,  $Var(b_i) = \sigma_b^2$ ,  $Corr(a_i, b_i) = \rho$
- $e_{ij}$ : within-subject residual with variance  $\sigma_e^2$

By accounting for randomization, we improve the efficiency for estimating the difference in slopes. We also allow for non-equal spacing of the time points and missing data due to dropouts.

### Value

An S3 class `designSlopeDiffMMRM` object with three components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlpha`: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - `kMax`: The number of stages.
  - `theta`: The parameter value.
  - `information`: The maximum information.
  - `expectedInformationH1`: The expected information under H1.
  - `expectedInformationH0`: The expected information under H0.
  - `drift`: The drift parameter, equal to `theta*sqrt(information)`.
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numberOfSubjects`: The maximum number of subjects.
  - `studyDuration`: The maximum study duration.
  - `expectedNumberOfSubjectsH1`: The expected number of subjects under H1.
  - `expectedNumberOfSubjectsH0`: The expected number of subjects under H0.
  - `expectedStudyDurationH1`: The expected study duration under H1.
  - `expectedStudyDurationH0`: The expected study duration under H0.
  - `accrualDuration`: The accrual duration.
  - `followupTime`: The follow-up time.
  - `fixedFollowup`: Whether a fixed follow-up design is used.
  - `slopeDiffH0`: The slope difference under H0.
  - `slopeDiff`: The slope difference under H1.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale.
  - `futilityBounds`: The futility boundaries on the Z-scale.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.



- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- efficacySlopeDiff: The efficacy boundaries on the slope difference scale.
- futilitySlopeDiff: The futility boundaries on the slope difference scale.
- numberOfSubjects: The number of subjects.
- analysisTime: The average time since trial start.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: The allocation ratio for the active treatment versus control.
  - accrualTime: A vector that specifies the starting time of piecewise Poisson enrollment time intervals.
  - accrualIntensity: A vector of accrual intensities. One for each accrual time interval.
  - piecewiseSurvivalTime: A vector that specifies the starting time of piecewise exponential survival time intervals.
  - gamma1: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
  - gamma2: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the control group.
  - w: The number of time units per measurement visit in a period.
  - N: The number of measurement visits in a period.
  - stdDev: The standard deviation of the residual.
  - G: The covariance matrix for the random intercept and random slope.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

## References

Daniel O. Scharfstein, Anastasios A. Tsiatis, and James M. Robins. Semiparametric efficiency and its implication on the design and analysis of group-sequential studies. *Journal of the American Statistical Association* 1997; 92:1342-1350.

## Examples

```
(design1 <- getDesignSlopeDiffMRRM(
  beta = 0.2, slopeDiff = log(1.15)/52,
  stDev = sqrt(.182),
  stDevIntercept = sqrt(.238960),
  stDevSlope = sqrt(.000057),
  corrInterceptSlope = .003688/sqrt(.238960*.000057),
  w = 8,
  N = 10000,
  accrualIntensity = 15,
  gamma1 = 1/(4.48*52),
  gamma2 = 1/(4.48*52),
  accrualDuration = NA,
  followupTime = 8,
  alpha = 0.025))
```

---

getDesignTwoMultinom *Power and sample for difference in two-sample multinomial responses*

---

## Description

Obtains the power given sample size or obtains the sample size given power for difference in two-sample multinomial responses.

## Usage

```
getDesignTwoMultinom(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
ncats	The number of categories of the multinomial response.
pi1	The prevalence of each category for the treatment group. Only need to specify the valued for the first $ncats-1$ categories.
pi2	The prevalence of each category for the control group. Only need to specify the valued for the first $ncats-1$ categories.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

**Value**

An S3 class `designTwoMultinom` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The two-sided significance level.
- `n`: The maximum number of subjects.
- `ncats`: The number of categories of the multinomial response.
- `pi1`: The prevalence of each category for the treatment group.
- `pi2`: The prevalence of each category for the control group.
- `effectsize`: The effect size for the chi-square test.
- `allocationRatioPlanned`: Allocation ratio for the active treatment versus control.
- `rounding`: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignTwoMultinom(
  beta = 0.1, ncats = 3, pi1 = c(0.3, 0.35),
  pi2 = c(0.2, 0.3), alpha = 0.05))
```

---

getDesignTwoOrdinal     *Power and sample size for the Wilcoxon test for two-sample ordinal response*

---

### Description

Obtains the power given sample size or obtains the sample size given power for the Wilcoxon test for two-sample ordinal response.

### Usage

```
getDesignTwoOrdinal(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

### Arguments

beta	The type II error.
n	The total sample size.
ncats	The number of categories of the ordinal response.
pi1	The prevalence of each category for the treatment group. Only need to specify the valued for the first ncats-1 categories.
pi2	The prevalence of each category for the control group. Only need to specify the valued for the first ncats-1 categories.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The significance level. Defaults to 0.025.

### Value

An S3 class `designTwoOrdinal` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The two-sided significance level.
- `n`: The maximum number of subjects.

- ncats: The number of categories of the ordinal response.
- pi1: The prevalence of each category for the treatment group.
- pi2: The prevalence of each category for the control group.
- meanscore1: The mean midrank score for the treatment group.
- meanscore2: The mean midrank score for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignTwoOrdinal(  
  beta = 0.1, ncats = 4, pi1 = c(0.55, 0.3, 0.1),  
  pi2 = c(0.214, 0.344, 0.251), alpha = 0.025))
```

---

getDesignTwoWayANOVA *Power and sample size for two-way ANOVA*

---

**Description**

Obtains the power and sample size for two-way analysis of variance.

**Usage**

```
getDesignTwoWayANOVA(  
  beta = NA_real_,  
  n = NA_real_,  
  nlevelsA = 2,  
  nlevelsB = 2,  
  means = NA_real_,  
  stDev = 1,  
  rounding = TRUE,  
  alpha = 0.05  
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
nlevelsA	The number of groups for Factor A.
nlevelsB	The number of levels for Factor B.
means	The matrix of treatment means for Factors A and B combination.
stDev	The common standard deviation.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

**Value**

An S3 class `designTwoWayANOVA` object with the following components:

- alpha: The two-sided significance level.
- nlevelsA: The number of levels for Factor A.
- nlevelsB: The number of levels for Factor B.
- means: The matrix of treatment group means.
- stDev: The common standard deviation.
- effectsizeA: The effect size for Factor A.
- effectsizeB: The effect size for Factor B.
- effectsizeAB: The effect size for Factor A and Factor B interaction.
- rounding: Whether to round up sample size.
- powerdf: The data frame containing the power and sample size results. It has the following variables:
  - n: The sample size.
  - powerA: The power to reject the null hypothesis that there is no difference among Factor A levels.
  - powerB: The power to reject the null hypothesis that there is no difference among Factor B levels.
  - powerAB: The power to reject the null hypothesis that there is no interaction between Factor A and Factor B.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignTwoWayANOVA(
  beta = 0.1, nlevelsA = 2, nlevelsB = 2,
  means = matrix(c(0.5, 4.7, 0.4, 6.9), 2, 2, byrow = TRUE),
  stDev = 2, alpha = 0.05))
```

---

`getDesignUnorderedBinom`*Power and sample size for unordered multi-sample binomial response*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for the chi-square test for unordered multi-sample binomial response.

**Usage**

```
getDesignUnorderedBinom(  
  beta = NA_real_,  
  n = NA_real_,  
  ngroups = NA_integer_,  
  pi = NA_real_,  
  allocationRatioPlanned = NA_integer_,  
  rounding = TRUE,  
  alpha = 0.05  
)
```

**Arguments**

<code>beta</code>	The type II error.
<code>n</code>	The total sample size.
<code>ngroups</code>	The number of treatment groups.
<code>pi</code>	The response probabilities for the treatment groups.
<code>allocationRatioPlanned</code>	Allocation ratio for the treatment groups.
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>alpha</code>	The two-sided significance level. Defaults to 0.05.

**Value**

An S3 class `designUnorderedBinom` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The two-sided significance level.
- `n`: The maximum number of subjects.
- `ngroups`: The number of treatment groups.
- `pi`: The response probabilities for the treatment groups.
- `effectsize`: The effect size for the chi-square test.
- `allocationRatioPlanned`: Allocation ratio for the treatment groups.
- `rounding`: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignUnorderedBinom(
  beta = 0.1, ngroups = 3, pi = c(0.1, 0.25, 0.5), alpha = 0.05))
```

---

```
getDesignUnorderedMultinom
```

*Power and sample size for unordered multi-sample multinomial response*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for the chi-square test for unordered multi-sample multinomial response.

**Usage**

```
getDesignUnorderedMultinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  ncats = NA_integer_,
  pi = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

**Arguments**

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
ncats	The number of categories of the multinomial response.
pi	The matrix of response probabilities for the treatment groups. It should have ngroups rows and ncats-1 or ncats columns.
allocationRatioPlanned	Allocation ratio for the treatment groups.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.



**Value**

An S3 class `designUnorderedMultinom` object with the following components:

- `power`: The power to reject the null hypothesis.
- `alpha`: The two-sided significance level.
- `n`: The maximum number of subjects.
- `ngroups`: The number of treatment groups.
- `ncats`: The number of categories of the multinomial response.
- `pi`: The response probabilities for the treatment groups.
- `effectsize`: The effect size for the chi-square test.
- `allocationRatioPlanned`: Allocation ratio for the treatment groups.
- `rounding`: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
(design1 <- getDesignUnorderedMultinom(
  beta = 0.1, ngroups = 3, ncats = 4,
  pi = matrix(c(0.230, 0.320, 0.272,
               0.358, 0.442, 0.154,
               0.142, 0.036, 0.039),
             3, 3, byrow = TRUE),
  allocationRatioPlanned = c(2, 2, 1),
  alpha = 0.05))
```

---

`getDesignWilcoxon`      *Group sequential design for two-sample Wilcoxon test*

---

**Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample Wilcoxon test.

**Usage**

```
getDesignWilcoxon(
  beta = NA_real_,
  n = NA_real_,
  pLarger = 0.6,
  allocationRatioPlanned = 1,
  rounding = TRUE,
```

```

kMax = 1L,
informationRates = NA_real_,
efficacyStopping = NA_integer_,
futilityStopping = NA_integer_,
criticalValues = NA_real_,
alpha = 0.025,
typeAlphaSpending = "sfOF",
parameterAlphaSpending = NA_real_,
userAlphaSpending = NA_real_,
futilityBounds = NA_real_,
typeBetaSpending = "none",
parameterBetaSpending = NA_real_,
userBetaSpending = NA_real_,
spendingTime = NA_real_
)

```

### Arguments

<code>beta</code>	The type II error.
<code>n</code>	The total sample size.
<code>pLarger</code>	The probability that a randomly chosen sample from the treatment group is larger than a randomly chosen sample from the control group under the alternative hypothesis.
<code>allocationRatioPlanned</code>	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
<code>futilityStopping</code>	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level. Defaults to 0.025.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class designWilcoxon object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping..
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to  $\theta \cdot \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pLarger: The probability that a randomly chosen sample from the treatment group is larger than a randomly chosen sample from the control group under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:

- informationRates: The information rates.
- efficacyBounds: The efficacy boundaries on the Z-scale.
- futilityBounds: The futility boundaries on the Z-scale.
- rejectPerStage: The probability for efficacy stopping.
- futilityPerStage: The probability for futility stopping.
- cumulativeRejection: The cumulative probability for efficacy stopping.
- cumulativeFutility: The cumulative probability for futility stopping.
- cumulativeAlphaSpent: The cumulative alpha spent.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- efficacyPLarger: The efficacy boundaries on the proportion of pairs of samples from the two treatment groups with the sample from the treatment group greater than that from the control group.
- futilityPLarger: The futility boundaries on the proportion of pairs of samples from the two treatment groups with the sample from the treatment group greater than that from the control group.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: fixed design
(design1 <- getDesignWilcoxon(
```

```

beta = 0.1, n = NA,
pLarger = pnorm((8 - 2)/sqrt(2*25^2)), alpha = 0.025)

# Example 2: group sequential design
(design2 <- getDesignWilcoxon(
  beta = 0.1, n = NA,
  pLarger = pnorm((8 - 2)/sqrt(2*25^2)), alpha = 0.025,
  kMax = 3, typeAlphaSpending = "sf0F"))

```

---

```
getDurationFromNevents
```

*Range of accrual duration for target number of events*

---

### Description

Obtains a range of accrual duration to reach the target number of events.

### Usage

```

getDurationFromNevents(
  nevents = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  npoints = 23L,
  interval = as.numeric(c(0.001, 240))
)

```

### Arguments

nevents	The target number of events.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., <code>c(0, 3)</code> breaks the time axis into 2 accrual intervals: <code>[0, 3)</code> and <code>[3, Inf)</code> .

<code>accrualIntensity</code>	A vector of accrual intensities. One for each accrual time interval.
<code>piecewiseSurvivalTime</code>	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
<code>stratumFraction</code>	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
<code>lambda1</code>	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
<code>lambda2</code>	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
<code>gamma1</code>	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
<code>gamma2</code>	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
<code>followupTime</code>	Follow-up time for the last enrolled subjects. Must be provided for fixed follow-up design.
<code>fixedFollowup</code>	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
<code>npoints</code>	The number of accrual duration time points. Defaults to 23.
<code>interval</code>	The interval to search for the solution of <code>accrualDuration</code> . Defaults to $c(0.001, 240)$ .

**Value**

A data frame of the following variables:

- `nevents`: The target number of events.
- `fixedFollowup`: Whether a fixed follow-up design is used.
- `accrualDuration`: The accrual duration.
- `subjects`: The total number of subjects.
- `followupTime`: The follow-up time for the last enrolled subject.
- `studyDuration`: The study duration.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.
```

```
getDurationFromNevents(
  nevents = 80, allocationRatioPlanned = 1,
  accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
  lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  gamma1 = -log(1-0.05)/12,
  gamma2 = -log(1-0.05)/12,
  fixedFollowup = FALSE)
```

---

```
getNeventsFromHazardRatio
```

*Get the required number of events given hazard ratio*

---

**Description**

Obtains the required number of events given the hazard ratios under the null and alternative hypotheses for a group sequential design.

**Usage**

```
getNeventsFromHazardRatio(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_,
  hazardRatioH0 = 1,
  hazardRatio = NA_real_,
  allocationRatioPlanned = 1,
  rounding = 1L
)
```

**Arguments**

<code>beta</code>	Type II error. Defaults to 0.2.
<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates in terms of number of events. Fixed prior to the trial. Defaults to $(1:kMax) / kMax$ if left unspecified.
<code>efficacyStopping</code>	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
<code>futilityStopping</code>	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>alpha</code>	The significance level. Defaults to 0.025.
<code>typeAlphaSpending</code>	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
<code>parameterAlphaSpending</code>	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
<code>userAlphaSpending</code>	The user defined alpha spending. Cumulative alpha spent up to each stage.
<code>futilityBounds</code>	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., $kMax-1$ . Defaults to $rep(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
<code>typeBetaSpending</code>	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
<code>parameterBetaSpending</code>	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
<code>userBetaSpending</code>	The user defined beta spending. Cumulative beta spent up to each stage.
<code>spendingTime</code>	A vector of length $kMax$ for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .
<code>hazardRatioH0</code>	Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.



hazardRatio	Hazard ratio under the alternative hypothesis for the active treatment versus control. Defaults to 0.5.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
rounding	Whether to round up the number of events. Defaults to 1 for rounding.

**Value**

The required number of events.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
getNeventsFromHazardRatio(
  beta = 0.2, kMax = 2,
  informationRates = c(0.5,1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP",
  hazardRatio = 0.673)
```

---

getRCI

*Repeated confidence interval for group sequential design*


---

**Description**

Obtains the repeated confidence interval for a group sequential trial.

**Usage**

```
getRCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

**Arguments**

L	The look of interest.
zL	The z-test statistic at the look.
IMax	The maximum information of the trial.
informationRates	The information rates up to look L.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage up to look L. Defaults to true if left unspecified.
criticalValues	The upper boundaries on the z-test statistic scale for efficacy stopping up to look L.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value of alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
spendingTime	The error spending time up to look L. Defaults to missing, in which case, it is the same as informationRates.

**Value**

A data frame with the following components:

- pvalue: Repeated p-value for rejecting the null hypothesis.
- thetihat: Point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of repeated confidence interval.
- upper: Upper bound of repeated confidence interval.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**References**

Christopher Jennison and Bruce W. Turnbull. Interim analyses: the repeated confidence interval approach (with discussion). *J R Stat Soc Series B*. 1989;51:305-361.

**Examples**

```
# group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4))

# results at the second look
L = 2
n1 = n*2/3
delta1 = 7
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)

# repeated confidence interval
getRCI(L = L, zL = zL, IMax = n/(4*sigma1^2),
  informationRates = c(1/3, 2/3), alpha = 0.05,
  typeAlphaSpending = "sfHSD", parameterAlphaSpending = -4)
```

---

hedgesg

*Hedges' g effect size*


---

**Description**

Obtains Hedges'  $g$  estimate and confidence interval of effect size.

**Usage**

```
hedgesg(tstat, m, ntilde, cilevel = 0.95)
```

**Arguments**

tstat	The value of the t-test statistic for comparing two treatment conditions.
m	The degrees of freedom for the t-test.
ntilde	The normalizing sample size to convert the standardized treatment difference to the t-test statistic, i.e., $tstat = \sqrt{ntilde} * \text{meanDiff} / \text{stDev}$ .
cilevel	The confidence interval level. Defaults to 0.95.

**Details**

Hedges'  $g$  is an effect size measure commonly used in meta-analysis to quantify the difference between two groups. It's an improvement over Cohen's  $d$ , particularly when dealing with small sample sizes.

The formula for Hedges'  $g$  is

$$g = c(m)d,$$

where  $d$  is Cohen's  $d$  effect size estimate, and  $c(m)$  is the bias correction factor,

$$d = (\hat{\mu}_1 - \hat{\mu}_2)/\hat{\sigma},$$

$$c(m) = 1 - \frac{3}{4m - 1}.$$

Since  $c(m) < 1$ , Cohen's  $d$  overestimates the true effect size.  $\delta = (\mu_1 - \mu_2)/\sigma$ . Since

$$t = \sqrt{\tilde{n}}d,$$

we have

$$g = \frac{c(m)}{\sqrt{\tilde{n}}}t,$$

where  $t$  has a noncentral  $t$  distribution with  $m$  degrees of freedom and noncentrality parameter  $\sqrt{\tilde{n}}\delta$ .

The asymptotic variance of  $g$  can be approximated by

$$Var(g) = \frac{1}{\tilde{n}} + \frac{g^2}{2m}.$$

The confidence interval for  $\delta$  can be constructed using normal approximation.

For two-sample mean difference with sample size  $n_1$  for the treatment group and  $n_2$  for the control group, we have  $\tilde{n} = \frac{n_1 n_2}{n_1 + n_2}$  and  $m = n_1 + n_2 - 2$  for pooled variance estimate.

### Value

A data frame with the following variables:

- `tstat`: The value of the t test statistic.
- `m`: The degrees of freedom for the t-test.
- `ntilde`: The normalizing sample size to convert the standardized treatment difference to the t-test statistic.
- `g`: Hedges'  $g$  effect size estimate.
- `varg`: Variance of  $g$ .
- `lower`: The lower confidence limit for effect size.
- `upper`: The upper confidence limit for effect size.
- `cilevel`: The confidence interval level.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### References

Larry V. Hedges. Distribution theory for Glass's estimator of effect size and related estimators. *Journal of Educational Statistics* 1981; 6:107-128.

**Examples**

```

n1 = 7
n2 = 8
meanDiff = 0.444
stDev = 1.201
m = n1+n2-2
ntilde = n1*n2/(n1+n2)
tstat = sqrt(ntilde)*meanDiff/stDev

hedgesg(tstat, m, ntilde)

```

kmdiff

*Estimate of milestone survival difference***Description**

Obtains the estimate of milestone survival difference between two treatment groups.

**Usage**

```

kmdiff(
  data,
  rep = "rep",
  stratum = "stratum",
  treat = "treat",
  time = "time",
  event = "event",
  milestone = NA_real_,
  survDiffH0 = 0,
  confint = 0.95
)

```

**Arguments**

data	The input data frame that contains the following variables: <ul style="list-style-type: none"> <li>• rep: The replication for by-group processing.</li> <li>• stratum: The stratum.</li> <li>• treat: The treatment.</li> <li>• time: The possibly right-censored survival time.</li> <li>• event: The event indicator.</li> </ul>
rep	The name of the replication variable in the input data.
stratum	The name of the stratum variable in the input data.
treat	The name of the treatment variable in the input data.

time	The name of the time variable in the input data.
event	The name of the event variable in the input data.
milestone	The milestone time at which to calculate the survival probability.
survDiffH0	The difference in milestone survival probabilities under the null hypothesis. Defaults to 0 for superiority test.
confint	The level of the two-sided confidence interval for the difference in milestone survival probabilities. Defaults to 0.95.

### Value

A data frame with the following variables:

- rep: The replication.
- milestone: The milestone time relative to randomization.
- survDiffH0: The difference in milestone survival probabilities under the null hypothesis.
- surv1: The estimated milestone survival probability for the treatment group.
- surv2: The estimated milestone survival probability for the control group.
- survDiff: The estimated difference in milestone survival probabilities.
- vsurv1: The variance for surv1.
- vsurv2: The variance for surv2.
- vsurvDiff: The variance for survDiff.
- survDiffZ: The Z-statistic value.
- survDiffPValue: The one-sided p-value.
- lower: The lower bound of confidence interval.
- upper: The upper bound of confidence interval.
- confint: The level of confidence interval.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
df <- kmdiff(data = rawdata, rep = "iterationNumber",
             stratum = "stratum", treat = "treatmentGroup",
             time = "timeUnderObservation", event = "event",
             milestone = 12)
head(df)
```

---

kmest *Kaplan-Meier estimates of the survival curve*

---

### Description

Obtains the Kaplan-Meier estimates of the survival curve.

### Usage

```
kmest(  
  data,  
  rep = "rep",  
  stratum = "stratum",  
  time = "time",  
  event = "event",  
  conftype = "log-log",  
  confint = 0.95  
)
```

### Arguments

data	The input data frame that contains the following variables: <ul style="list-style-type: none"><li>• rep: The replication for by-group processing.</li><li>• stratum: The stratum.</li><li>• time: The possibly right-censored survival time.</li><li>• event: The event indicator.</li></ul>
rep	The name of the replication variable in the input data.
stratum	The name of the stratum variable in the input data.
time	The name of the time variable in the input data.
event	The name of the event variable in the input data.
conftype	The type of confidence interval. One of "none", "plain", "log", "log-log" (the default), or "arcsin". The arcsin option bases the intervals on $\text{asin}(\sqrt{\text{survival}})$ .
confint	The level of the two-sided confidence interval for the survival probabilities. Defaults to 0.95.

### Value

A data frame with the following variables:

- rep: The replication.
- stratum: The stratum.
- size: The number of subjects in the stratum.
- time: The event time.
- nrisk: The number of subjects at risk.

- `nevent`: The number of subjects having the event.
- `survival`: The Kaplan-Meier estimate of the survival probability.
- `stderr`: The standard error of the estimated survival probability based on the Greendwood formula.
- `lower`: The lower bound of confidence interval if requested.
- `upper`: The upper bound of confidence interval if requested.
- `confint`: The level of confidence interval if requested.
- `conftype`: The type of confidence interval if requested.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
kcest(data = survival::aml, stratum = "x",
      time = "time", event = "status")
```

---

kmpower

*Power for difference in milestone survival probabilities*

---

### Description

Estimates the power for testing the difference in milestone survival probabilities in a two-sample survival design.

### Usage

```
kmpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  milestone = NA_real_,
  survDiffH0 = 0,
  allocationRatioPlanned = 1,
```



```

accrualTime = 0L,
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
lambda1 = NA_real_,
lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
spendingTime = NA_real_,
studyDuration = NA_real_
)

```

### Arguments

**kMax** The maximum number of stages.

**informationRates** The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**efficacyStopping** Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

**futilityStopping** Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha** The significance level. Defaults to 0.025.

**typeAlphaSpending** The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending** The user defined alpha spending. Cumulative alpha spent up to each stage.

**futilityBounds** Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to  $\text{rep}(-6, kMax-1)$  if left unspecified. The futility bounds are non-binding for the calculation of critical values.

**typeBetaSpending** The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for

	Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
milestone	The milestone time at which to calculate the survival probability.
survDiffH0	The difference in milestone survival probabilities under the null hypothesis. Defaults to 0 for superiority test.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
spendingTime	A vector of length <code>kMax</code> for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of <code>accrualDuration</code> and <code>followupTime</code> . If provided, the value is allowed to be less than the sum of <code>accrualDuration</code> and <code>followupTime</code> .

**Value**

An S3 class `kmpower` object with 3 components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `drift`: The drift parameter, equal to  $(\text{survDiff} - \text{survDiffH0}) * \sqrt{\text{information}}$ .
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numbeOfSubjects`: The total number of subjects.
  - `studyDuration`: The total study duration.
  - `information`: The maximum information.
  - `expectedNumberOfSubjects`: The expected number of subjects.
  - `expectedStudyDuration`: The expected study duration.
  - `expectedInformation`: The expected information.
  - `accrualDuration`: The accrual duration.
  - `followupTime`: The follow-up duration.
  - `fixedFollowup`: Whether a fixed follow-up design is used.
  - `kMax`: The number of stages.
  - `milestone`: The milestone time relative to randomization.
  - `survDiffH0`: The difference in milestone survival probabilities under the null hypothesis.
  - `surv1`: The milestone survival probability for the treatment group.
  - `surv2`: The milestone survival probability for the control group.
  - `survDiff`: The difference in milestone survival probabilities, equal to  $\text{surv1} - \text{surv2}$ .
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.
  - `efficacyBounds`: The efficacy boundaries on the Z-scale.
  - `futilityBounds`: The futility boundaries on the Z-scale.
  - `rejectPerStage`: The probability for efficacy stopping.
  - `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.
  - `numberOfSubjects`: The number of subjects.
  - `analysisTime`: The average time since trial start.
  - `efficacySurvDiff`: The efficacy boundaries on the survival difference scale.
  - `futilitySurvDiff`: The futility boundaries on the survival difference scale.
  - `efficacyP`: The efficacy boundaries on the p-value scale.
  - `futilityP`: The futility boundaries on the p-value scale.
  - `information`: The cumulative information.
  - `efficacyStopping`: Whether to allow efficacy stopping.
  - `futilityStopping`: Whether to allow futility stopping.
- `settings`: A list containing the following input parameters: `typeAlphaSpending`, `parameterAlphaSpending`, `userAlphaSpending`, `typeBetaSpending`, `parameterBetaSpending`, `allocationRatioPlanned`, `accrualTime`, `accrualIntensity`, `piecewiseSurvivalTime`, `stratumFraction`, `lambda1`, `lambda2`, `gamma1`, `gamma2`, and `spendingTime`.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.
```

```
kmpower(kMax = 2, informationRates = c(0.8, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        milestone = 18,
        allocationRatioPlanned = 1, accrualTime = seq(0, 8),
        accrualIntensity = 26/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        stratumFraction = c(0.2, 0.8),
        lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
        lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12, accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

---

kmpower1s

*Power for one-sample milestone survival probability*

---

**Description**

Estimates the power, stopping probabilities, and expected sample size in a one-group survival design.

**Usage**

```
kmpower1s(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  milestone = NA_real_,
  survH0 = NA_real_,
  accrualTime = 0L,
```

```

    accrualIntensity = NA_real_,
    piecewiseSurvivalTime = 0L,
    stratumFraction = 1L,
    lambda = NA_real_,
    gamma = 0L,
    accrualDuration = NA_real_,
    followupTime = NA_real_,
    fixedFollowup = 0L,
    spendingTime = NA_real_,
    studyDuration = NA_real_
  )

```

### Arguments

**kMax** The maximum number of stages.

**informationRates** The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**efficacyStopping** Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

**futilityStopping** Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha** The significance level. Defaults to 0.025.

**typeAlphaSpending** The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending** The user defined alpha spending. Cumulative alpha spent up to each stage.

**futilityBounds** Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to  $\text{rep}(-6, kMax-1)$  if left unspecified. The futility bounds are non-binding for the calculation of critical values.

**typeBetaSpending** The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
milestone	The milestone time at which to calculate the survival probability.
survH0	The milestone survival probability under the null hypothesis.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda	A vector of hazard rates for the event in each analysis time interval by stratum under the alternative hypothesis.
gamma	The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout. Defaults to 0 for no dropout.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

## Value

An S3 class `kmpower1s` object with 3 components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `drift`: The drift parameter, equal to  $(\text{surv} - \text{survH0}) * \sqrt{\text{information}}$ .
  - `inflationFactor`: The inflation factor (relative to the fixed design).
  - `numbeOfSubjects`: The total number of subjects.
  - `studyDuration`: The total study duration.
  - `information`: The maximum information.
  - `expectedNumberOfSubjects`: The expected number of subjects.

- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- accrualDuration: The accrual duration.
- followupTime: The follow-up duration.
- fixedFollowup: Whether a fixed follow-up design is used.
- kMax: The number of stages.
- milestone: The milestone time to calculate the survival probability.
- survH0: The milestone survival probability under the null hypothesis.
- surv: The milestone survival probability under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - efficacySurv: The efficacy boundaries on the milestone survival probability scale.
  - futilitySurv: The futility boundaries on the milestone survival probability scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, accrualTime, accrualIntensity, piecewiseSurvivalTime, stratumFraction, lambda, gamma, and spendingTime.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[kmstat](#)

**Examples**

```
kmpower1s(kMax = 2, informationRates = c(0.8, 1),
          alpha = 0.025, typeAlphaSpending = "sfOF",
          milestone = 18, survH0 = 0.30,
```

```

accrualTime = seq(0, 8),
accrualIntensity = 26/9*seq(1, 9),
piecewiseSurvivalTime = c(0, 6),
stratumFraction = c(0.2, 0.8),
lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
gamma = -log(1-0.05)/12, accrualDuration = 22,
followupTime = 18, fixedFollowup = FALSE)

```

---

kmpowerequiv

*Power for equivalence in milestone survival probability difference*


---

### Description

Obtains the power for equivalence in milestone survival probability difference.

### Usage

```

kmpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  milestone = NA_real_,
  survDiffLower = NA_real_,
  survDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)

```



**Arguments**

kMax	The maximum number of stages.
informationRates	The information rates. Defaults to $(1:kMax) / kMax$ if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
milestone	The milestone time at which to calculate the survival probability.
survDiffLower	The lower equivalence limit of milestone survival probability difference.
survDiffUpper	The upper equivalence limit of milestone survival probability difference.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, Inf)$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, Inf)$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

<code>gamma2</code>	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
<code>accrualDuration</code>	Duration of the enrollment period.
<code>followupTime</code>	Follow-up time for the last enrolled subject.
<code>fixedFollowup</code>	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
<code>spendingTime</code>	A vector of length <code>kMax</code> for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .
<code>studyDuration</code>	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of <code>accrualDuration</code> and <code>followupTime</code> . If provided, the value is allowed to be less than the sum of <code>accrualDuration</code> and <code>followupTime</code> .

### Value

An S3 class `kmpowerequiv` object with 3 components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlphaH10`: The attained significance level under H10.
  - `attainedAlphaH20`: The attained significance level under H20.
  - `numbeOfSubjects`: The total number of subjects.
  - `studyDuration`: The total study duration.
  - `information`: The maximum information.
  - `expectedNumberOfSubjects`: The expected number of subjects.
  - `expectedStudyDuration`: The expected study duration.
  - `expectedInformation`: The expected information.
  - `kMax`: The number of stages.
  - `milestone`: The milestone time relative to randomization.
  - `survDiffLower`: The lower equivalence limit of milestone survival probability difference.
  - `survDiffUpper`: The upper equivalence limit of milestone survival probability difference.
  - `surv1`: The milestone survival probability for the treatment group.
  - `surv2`: The milestone survival probability for the control group.
  - `survDiff`: The milestone survival probability difference.
  - `accrualDuration`: The accrual duration.
  - `followupTime`: The follow-up duration.
  - `fixedFollowup`: Whether a fixed follow-up design is used.
- `byStageResults`: A data frame containing the following variables:
  - `informationRates`: The information rates.

- efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - efficacySurvDiffLower: The efficacy boundaries on the milestone survival probability difference scale for the one-sided null hypothesis at the lower equivalence limit.
  - efficacySurvDiffUpper: The efficacy boundaries on the milestone survival probability difference scale for the one-sided null hypothesis at the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accrualIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, and spendingTime.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[kmstat](#)

**Examples**

```
kmpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             milestone = 18,
             survDiffLower = -0.13, survDiffUpper = 0.13,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12, accrualDuration = 22,
             followupTime = 18, fixedFollowup = FALSE)
```

---

kmsamplesize

*Sample size for difference in milestone survival probabilities*


---

### Description

Obtains the needed accrual duration given power, accrual intensity, and follow-up time, the needed follow-up time given power, accrual intensity, and accrual duration, or the needed absolute accrual intensity given power, relative accrual intensity, accrual duration, and follow-up time in a two-group survival design.

### Usage

```
kmsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  milestone = NA_real_,
  survDiffH0 = 0,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

**Arguments**

beta	Type II error. Defaults to 0.2.
kMax	The maximum number of stages.
informationRates	The information rates. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to $\text{rep}(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
milestone	The milestone time at which to calculate the survival probability.
survDiffH0	The difference in milestone survival probabilities under the null hypothesis. Defaults to 0 for superiority test.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
interval	The interval to search for the solution of accrualDuration, followupTime, or the proportionality constant of accrualIntensity. Defaults to $c(0.001, 240)$ .
spendingTime	A vector of length <code>kMax</code> for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

**Value**

A list of two components:

- `resultsUnderH1`: An S3 class `kmpower` object under the alternative hypothesis.
- `resultsUnderH0`: An S3 class `kmpower` object under the null hypothesis.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[kmpower](#)

**Examples**

```
# Example 1: Obtains follow-up time given power, accrual intensity,
# and accrual duration for variable follow-up. Of note, the power
# reaches the maximum when the follow-up time equals milestone.
```

```
kmsamplesize(beta = 0.25, kMax = 2, informationRates = c(0.8, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  milestone = 18,
  allocationRatioPlanned = 1, accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
  lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  gamma1 = -log(1-0.05)/12,
  gamma2 = -log(1-0.05)/12, accrualDuration = 22,
  followupTime = NA, fixedFollowup = FALSE)
```

```
# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up time for variable follow-up
```

```
kmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  milestone = 18,
  allocationRatioPlanned = 1, accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
  lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  gamma1 = -log(1-0.05)/12,
  gamma2 = -log(1-0.05)/12, accrualDuration = 22,
  followupTime = 18, fixedFollowup = FALSE)
```

```
# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up time for fixed follow-up
```

```
kmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  milestone = 18,
  allocationRatioPlanned = 1, accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
  lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  gamma1 = -log(1-0.05)/12,
  gamma2 = -log(1-0.05)/12, accrualDuration = NA,
  followupTime = 18, fixedFollowup = TRUE)
```

---

kmsamplesize1s      *Sample size for one-sample milestone survival probability*

---

### Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a one-group survival design.

### Usage

```
kmsamplesize1s(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  milestone = NA_real_,
  survH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

### Arguments

beta	Type II error. Defaults to 0.2.
kMax	The maximum number of stages.



informationRates	The information rates. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., $kMax-1$ . Defaults to $rep(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
milestone	The milestone time at which to calculate the survival probability.
survH0	The milestone survival probability under the null hypothesis.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, Inf)$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, Inf)$ . Defaults to 0 for exponential distribution.

<code>stratumFraction</code>	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
<code>lambda</code>	A vector of hazard rates for the event in each analysis time interval by stratum under the alternative hypothesis.
<code>gamma</code>	The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout. Defaults to 0 for no dropout.
<code>accrualDuration</code>	Duration of the enrollment period.
<code>followupTime</code>	Follow-up time for the last enrolled subject.
<code>fixedFollowup</code>	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
<code>interval</code>	The interval to search for the solution of <code>accrualDuration</code> , <code>followupDuration</code> , or the proportionality constant of <code>accrualIntensity</code> . Defaults to <code>c(0.001, 240)</code> .
<code>spendingTime</code>	A vector of length <code>kMax</code> for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.

**Value**

A list of two components:

- `resultsUnderH1`: An S3 class `kmpower1s` object under the alternative hypothesis.
- `resultsUnderH0`: An S3 class `kmpower1s` object under the null hypothesis.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[kmpower1s](#)

**Examples**

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up
```

```
kmsamplesize1s(beta = 0.2, kMax = 2,
  informationRates = c(0.8, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  milestone = 18, survH0 = 0.30,
  accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
  gamma = -log(1-0.05)/12, accrualDuration = 22,
  followupTime = NA, fixedFollowup = FALSE)
```

```
# Example 2: Obtains accrual intensity given power, accrual duration, and
```

```

# follow-up duration for variable follow-up

kmsamplesize1s(beta = 0.2, kMax = 2,
  informationRates = c(0.8, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  milestone = 18, survH0 = 0.30,
  accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
  gamma = -log(1-0.05)/12, accrualDuration = 22,
  followupTime = 18, fixedFollowup = FALSE)

# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up

kmsamplesize1s(beta = 0.2, kMax = 2,
  informationRates = c(0.8, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  milestone = 18, survH0 = 0.30,
  accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
  gamma = -log(1-0.05)/12, accrualDuration = NA,
  followupTime = 18, fixedFollowup = TRUE)

```

---

kmsamplesizeequiv	<i>Sample size for equivalence in milestone survival probability difference</i>
-------------------	---

---

### Description

Obtains the sample size for equivalence in milestone survival probability difference.

### Usage

```

kmsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,

```

```

milestone = NA_real_,
survDiffLower = NA_real_,
survDiffUpper = NA_real_,
allocationRatioPlanned = 1,
accrualTime = 0L,
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
lambda1 = NA_real_,
lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
interval = as.numeric(c(0.001, 240)),
spendingTime = NA_real_,
rounding = 1L
)

```

### Arguments

**beta**                    The type II error.

**kMax**                    The maximum number of stages.

**informationRates**  
The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**criticalValues**        Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha**                    The significance level for each of the two one-sided tests. Defaults to 0.05.

**typeAlphaSpending**  
The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending**  
The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending**  
The user defined alpha spending. Cumulative alpha spent up to each stage.

**milestone**                The milestone time at which to calculate the survival probability.

**survDiffLower**        The lower equivalence limit of milestone survival probability difference.

**survDiffUpper**        The upper equivalence limit of milestone survival probability difference.

**allocationRatioPlanned**  
Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
interval	The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to $c(0.001, 240)$ .
spendingTime	A vector of length $k\text{Max}$ for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

**Value**

An S3 class `kmpowerequiv` object

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[kmpowerequiv](#)

## Examples

```
kmsamplesizeequiv(beta = 0.1, kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF",
  milestone = 18,
  survDiffLower = -0.13, survDiffUpper = 0.13,
  allocationRatioPlanned = 1, accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  gamma1 = -log(1-0.05)/12,
  gamma2 = -log(1-0.05)/12, accrualDuration = NA,
  followupTime = 18, fixedFollowup = FALSE)
```

---

 kmstat

*Stratified difference in milestone survival probabilities*


---

## Description

Obtains the stratified milestone survival probabilities and difference in milestone survival probabilities at given calendar times.

## Usage

```
kmstat(
  time = NA_real_,
  milestone = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L
)
```

## Arguments

time	A vector of calendar times for data cut.
milestone	The milestone time at which to calculate the survival probability.

allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

**Value**

A data frame containing the following variables:

- time: The calendar time since trial start.
- subjects: The number of enrolled subjects.
- milestone: The milestone time relative to randomization.
- surv1: The milestone survival probability for the treatment group.
- surv2: The milestone survival probability for the control group.
- survDiff: The difference in milestone survival probabilities, i.e.,  $\text{surv1} - \text{surv2}$ .
- vsurv1: The variance for surv1.
- vsurv2: The variance for surv2.
- vsurvDiff: The variance for survDiff.
- information: The information for survDiff, equal to  $1/\text{vsurvDiff}$ .
- survDiffZ: The Z-statistic value, i.e.,  $\text{survDiff}/\sqrt{\text{vsurvDiff}}$ .

**Author(s)**

Kaifeng Lu, <kaifengl@gmail.com>

**Examples**

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.
```

```
kmstat(time = c(22, 40),
        milestone = 18,
        allocationRatioPlanned = 1,
        accrualTime = seq(0, 8),
        accrualIntensity = 26/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        stratumFraction = c(0.2, 0.8),
        lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
        lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12,
        accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

---

 lrpower

*Log-rank test power*


---

**Description**

Estimates the power, stopping probabilities, and expected sample size in a two-group survival design.

**Usage**

```
lrpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
```



```

accrualTime = 0L,
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
lambda1 = NA_real_,
lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
rho1 = 0,
rho2 = 0,
numSubintervals = 300L,
estimateHazardRatio = 1L,
typeOfComputation = "direct",
spendingTime = NA_real_,
studyDuration = NA_real_
)

```

### Arguments

**kMax** The maximum number of stages.

**informationRates** The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**efficacyStopping** Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

**futilityStopping** Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha** The significance level. Defaults to 0.025.

**typeAlphaSpending** The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending** The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to $\text{rep}(-6, \text{kMax}-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
hazardRatioH0	Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

rho2	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
numSubintervals	Number of sub-intervals to approximate the mean and variance of the weighted log-rank test score statistic. Defaults to 300. Specify a larger number for better approximation.
estimateHazardRatio	Whether to estimate the hazard ratio from weighted Cox regression model and report the stopping boundaries on the hazard ratio scale.
typeOfComputation	The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

## Value

An S3 class Irpower object with 4 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - numberOfEvents: The total number of events.
  - numberOfDropouts: The total number of dropouts.
  - numbeOfSubjects: The total number of subjects.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfEvents: The expected number of events.
  - expectedNumberOfDropouts: The expected number of dropouts.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - accrualDuration: The accrual duration.
  - followupTime: The follow-up time.
  - fixedFollowup: Whether a fixed follow-up design is used.
  - rho1: The first parameter of the Fleming-Harrington family of weighted log-rank test.
  - rho2: The second parameter of the Fleming-Harrington family of weighted log-rank test.
  - kMax: The number of stages.
  - hazardRatioH0: The hazard ratio under the null hypothesis.

- typeOfComputation: The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - efficacyHR: The efficacy boundaries on the hazard ratio scale if estimateHazardRatio.
  - futilityHR: The futility boundaries on the hazard ratio scale if estimateHazardRatio.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - HR: The average hazard ratio.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accrualIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, estimateHazardRatio, and spendingTime.
- byTreatmentCounts: A list containing the following counts by treatment group:
  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - numberOfEvents2: The number of events by stage for the control group.
  - numberOfDropouts2: The number of dropouts by stage for the control group.
  - numberOfSubjects2: The number of subjects by stage for the control group.
  - expectedNumberOfEvents1: The expected number of events for the treatment group.
  - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
  - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
  - expectedNumberOfEvents2: The expected number of events for control group.
  - expectedNumberOfDropouts2: The expected number of dropouts for the control group.
  - expectedNumberOfSubjects2: The expected number of subjects for the control group.

**Author(s)**

Kaifeng Lu, <kaifengl@gmail.com>

**Examples**

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.
```

```
lrpower(kMax = 2, informationRates = c(0.8, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        allocationRatioPlanned = 1, accrualTime = seq(0, 8),
        accrualIntensity = 26/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        stratumFraction = c(0.2, 0.8),
        lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
        lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12, accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

---

Irpowerequiv

*Power for equivalence in hazard ratio*


---

**Description**

Obtains the power for equivalence in hazard ratio.

**Usage**

```
lrpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  hazardRatioLower = NA_real_,
  hazardRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
```

```

    typeOfComputation = "direct",
    spendingTime = NA_real_,
    studyDuration = NA_real_
)

```

## Arguments

kMax	The maximum number of stages.
informationRates	The information rates. Defaults to $(1:kMax) / kMax$ if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
hazardRatioLower	The lower equivalence limit of hazard ratio.
hazardRatioUpper	The upper equivalence limit of hazard ratio.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, Inf)$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, Inf)$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
typeOfComputation	The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

## Value

An S3 class `Irpowerequiv` object with 4 components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlphaH10`: The attained significance level under H10.
  - `attainedAlphaH20`: The attained significance level under H20.
  - `numberOfEvents`: The total number of events.
  - `numberOfDropouts`: The total number of dropouts.
  - `numbeOfSubjects`: The total number of subjects.
  - `studyDuration`: The total study duration.
  - `information`: The maximum information.
  - `expectedNumberOfEvents`: The expected number of events.
  - `expectedNumberOfDropouts`: The expected number of dropouts.
  - `expectedNumberOfSubjects`: The expected number of subjects.
  - `expectedStudyDuration`: The expected study duration.
  - `expectedInformation`: The expected information.
  - `kMax`: The number of stages.
  - `hazardRatioLower`: The lower equivalence limit of hazard ratio.
  - `hazardRatioUpper`: The upper equivalence limit of hazard ratio.

- accrualDuration: The accrual duration.
- followupTime: The follow-up time.
- fixedFollowup: Whether a fixed follow-up design is used.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - efficacyHRLower: The efficacy boundaries on the hazard ratio scale for the one-sided null hypothesis at the lower equivalence limit.
  - efficacyHRUpper: The efficacy boundaries on the hazard ratio scale for the one-sided null hypothesis at the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - HR: The average hazard ratio.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accrualIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, typeOfComputation, and spendingTime.
- byTreatmentCounts: A list containing the following counts by treatment group:
  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - numberOfEvents2: The number of events by stage for the control group.
  - numberOfDropouts2: The number of dropouts by stage for the control group.
  - numberOfSubjects2: The number of subjects by stage for the control group.
  - expectedNumberOfEvents1: The expected number of events for the treatment group.
  - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
  - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
  - expectedNumberOfEvents2: The expected number of events for control group.
  - expectedNumberOfDropouts2: The expected number of dropouts for the control group.
  - expectedNumberOfSubjects2: The expected number of subjects for the control group.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>



**See Also**[rmstat](#)**Examples**

```
lrsamplesize(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             hazardRatioLower = 0.71, hazardRatioUpper = 1.4,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 100/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12, accrualDuration = 22,
             followupTime = 18, fixedFollowup = FALSE)
```

Irsamplesize

*Log-rank test sample size***Description**

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up time, and relative accrual rates in a two-group survival design.

**Usage**

```
lrsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
```

```

accrualTime = 0L,
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
lambda1 = NA_real_,
lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
rho1 = 0,
rho2 = 0,
numSubintervals = 300L,
estimateHazardRatio = 1L,
typeOfComputation = "direct",
interval = as.numeric(c(0.001, 240)),
spendingTime = NA_real_,
rounding = 1L
)

```

### Arguments

**beta** Type II error. Defaults to 0.2.

**kMax** The maximum number of stages.

**informationRates** The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Defaults to (1:kMax) / kMax if left unspecified.

**efficacyStopping** Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

**futilityStopping** Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha** The significance level. Defaults to 0.025.

**typeAlphaSpending** The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., $k_{\text{Max}}-1$ . Defaults to $\text{rep}(-6, k_{\text{Max}}-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
hazardRatioH0	Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.

followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
rho2	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
numSubintervals	Number of sub-intervals to approximate the mean and variance of the weighted log-rank test score statistic. Defaults to 300. Specify a larger number for better approximation.
estimateHazardRatio	Whether to estimate the hazard ratio from weighted Cox regression model and report the stopping boundaries on the hazard ratio scale.
typeOfComputation	The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.
interval	The interval to search for the solution of accrualDuration, followupTime, or the proportionality constant of accrualIntensity. Defaults to c(0.001, 240). Adjustment may be needed for non-monotone relationship with study power.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
rounding	Whether to round up sample size and events. Defaults to 1 for sample size rounding.

**Value**

A list of two components:

- resultsUnderH1: An S3 class lrpower object under the alternative hypothesis.
- resultsUnderH0: An S3 class lrpower object under the null hypothesis.

**Author(s)**

Kaifeng Lu, <kweifenglu@gmail.com>

**See Also**

[lrpower](#)

**Examples**

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.

# Example 1: Obtains accrual duration given power and follow-up time
```

```

Irsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualTime = seq(0, 8),
             accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12,
             accrualDuration = NA,
             followupTime = 18, fixedFollowup = FALSE)

# Example 2: Obtains follow-up time given power and accrual duration

Irsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualTime = seq(0, 8),
             accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12,
             accrualDuration = 22,
             followupTime = NA, fixedFollowup = FALSE)

# Example 3: Obtains absolute accrual intensity given power,
# accrual duration, follow-up time, and relative accrual intensity

Irsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualTime = seq(0, 8),
             accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12,
             accrualDuration = 22,
             followupTime = 18, fixedFollowup = FALSE)

```

**Description**

Obtains the sample size for equivalence in hazard ratio.

**Usage**

```
lrsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  hazardRatioLower = NA_real_,
  hazardRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  typeOfComputation = "direct",
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

**Arguments**

beta	The type II error.
kMax	The maximum number of stages.
informationRates	The information rates. Defaults to $(1:kMax) / kMax$ if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang,

	Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
hazardRatioLower	The lower equivalence limit of hazard ratio.
hazardRatioUpper	The upper equivalence limit of hazard ratio.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
typeOfComputation	The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.

interval	The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to $c(0.001, 240)$ .
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

**Value**

An S3 class lrpowerequiv object

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[lrpowerequiv](#)

**Examples**

```
lrsamplesizeequiv(kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF",
  hazardRatioLower = 0.71, hazardRatioUpper = 1.4,
  allocationRatioPlanned = 1, accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  gamma1 = -log(1-0.05)/12,
  gamma2 = -log(1-0.05)/12, accrualDuration = NA,
  followupTime = 18, fixedFollowup = FALSE)
```

---

lrsim

*Log-rank test simulation*

---

**Description**

Performs simulation for two-arm group sequential trials based on weighted log-rank test.



**Usage**

```

Irsim(
  kMax = NA_integer_,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  futilityBounds = NA_real_,
  hazardRatioH0 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  plannedEvents = NA_integer_,
  plannedTime = NA_real_,
  maxNumberOfIterations = 1000L,
  maxNumberOfRawDatasetsPerStage = 0L,
  seed = NA_integer_
)

```

**Arguments**

<code>kMax</code>	The maximum number of stages.
<code>informationRates</code>	The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Fixed prior to the trial. If left unspecified, it defaults to <code>plannedEvents / plannedEvents[kMax]</code> when <code>plannedEvents</code> is provided and to <code>plannedTime / plannedTime[kMax]</code> otherwise.
<code>criticalValues</code>	Upper boundaries on the z-test statistic scale for stopping for efficacy.
<code>futilityBounds</code>	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., <code>kMax-1</code> . Defaults to <code>rep(-6, kMax-1)</code> if left unspecified. The futility bounds are non-binding for the calculation of critical values.
<code>hazardRatioH0</code>	Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.
<code>allocation1</code>	Number of subjects in the active treatment group in a randomization block. Defaults to 1 for equal randomization.

allocation2	Number of subjects in the control group in a randomization block. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
rho2	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
plannedEvents	The planned cumulative total number of events at each stage.
plannedTime	The calendar times for the analyses. To use calendar time to plan the analyses, plannedEvents should be missing.
maxNumberOfIterations	The number of simulation iterations. Defaults to 1000.
maxNumberOfRawDatasetsPerStage	The number of raw datasets per stage to extract. Defaults to 1.
seed	The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified,

**Value**

An S3 class `Irsim` object with 3 components:

- overview: A list containing the following information:
  - `rejectPerStage`: The efficacy stopping probability by stage.
  - `futilityPerStage`: The futility stopping probability by stage.
  - `cumulativeRejection`: Cumulative efficacy stopping probability by stage.
  - `cumulativeFutility`: The cumulative futility stopping probability by stage.
  - `numberOfEvents`: The average number of events by stage.
  - `numberOfDropouts`: The average number of dropouts by stage.
  - `numberOfSubjects`: The average number of subjects by stage.
  - `analysisTime`: The average analysis time by stage.
  - `overallReject`: The overall rejection probability.
  - `expectedNumberOfEvents`: The expected number of events for the overall study.
  - `expectedNumberOfDropouts`: The expected number of dropouts for the overall study.
  - `expectedNumberOfSubjects`: The expected number of subjects for the overall study.
  - `expectedStudyDuration`: The expected study duration.
  - `hazardRatioH0`: Hazard ratio under the null hypothesis for the active treatment versus control.
  - `useEvents`: whether the analyses are planned based on the number of events or calendar time.
  - `accrualDuration`: Duration of the enrollment period.
  - `fixedFollowup`: Whether a fixed follow-up design is used.
  - `rho1`: The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
  - `rho2`: The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
  - `kMax`: The maximum number of stages.
- `sumdata`: A data frame of summary data by iteration and stage:
  - `iterationNumber`: The iteration number.
  - `stopStage`: The stage at which the trial stops.
  - `eventsNotAchieved`: Whether the target number of events is not achieved for the iteration.
  - `stageNumber`: The stage number, covering all stages even if the trial stops at an interim look.
  - `analysisTime`: The time for the stage since trial start.
  - `accruals1`: The number of subjects enrolled at the stage for the treatment group.
  - `accruals2`: The number of subjects enrolled at the stage for the control group.
  - `totalAccruals`: The total number of subjects enrolled at the stage.
  - `events1`: The number of events at the stage for the treatment group.
  - `events2`: The number of events at the stage for the control group.
  - `totalEvents`: The total number of events at the stage.
  - `dropouts1`: The number of dropouts at the stage for the treatment group.

- dropouts2: The number of dropouts at the stage for the control group.
- totalDropouts: The total number of dropouts at the stage.
- uscore: The numerator of the log-rank test statistic.
- vscore: The variance of the log-rank test statistic.
- logRankStatistic: The log-rank test Z-statistic.
- rejectPerStage: Whether to reject the null hypothesis at the stage.
- futilityPerStage: Whether to stop the trial for futility at the stage.
- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
  - iterationNumber: The iteration number.
  - stopStage: The stage at which the trial stops.
  - analysisTime: The time for the stage since trial start.
  - subjectId: The subject ID.
  - arrivalTime: The enrollment time for the subject.
  - stratum: The stratum for the subject.
  - treatmentGroup: The treatment group (1 or 2) for the subject.
  - survivalTime: The underlying survival time for the subject.
  - dropoutTime: The underlying dropout time for the subject.
  - timeUnderObservation: The time under observation since randomization.
  - event: Whether the subject experienced the event.
  - dropoutEvent: Whether the subject dropped out.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
# Example 1: analyses based on number of events

sim1 = lrsim(kMax = 2, informationRates = c(0.5, 1),
            criticalValues = c(2.797, 1.977),
            accrualIntensity = 11,
            lambda1 = 0.018, lambda2 = 0.030,
            accrualDuration = 12,
            plannedEvents = c(60, 120),
            maxNumberOfIterations = 1000,
            maxNumberOfRawDatasetsPerStage = 1,
            seed = 314159)

# summary statistics
sim1

# summary for each simulated data set
head(sim1$sumdata)

# raw data for selected replication
```

```

head(sim1$rawdata)

# Example 2: analyses based on calendar time have similar power

sim2 = lrslim(kMax = 2, informationRates = c(0.5, 1),
             criticalValues = c(2.797, 1.977),
             accrualIntensity = 11,
             lambda1 = 0.018, lambda2 = 0.030,
             accrualDuration = 12,
             plannedTime = c(31.9, 113.2),
             maxNumberOfIterations = 1000,
             maxNumberOfRawDatasetsPerStage = 1,
             seed = 314159)

# summary statistics
sim2

# summary for each simulated data set
head(sim2$sumdata)

```

---

Irsim2e

*Log-rank test simulation for two endpoints*


---

## Description

Performs simulation for two-endpoint two-arm group sequential trials based on weighted log-rank test. The first  $k_{\text{Max}1}$  looks are driven by the total number of PFS events in two arms combined, and the subsequent looks are driven by the total number of OS events in two arms combined. Alternatively, the analyses can be planned to occur at specified calendar times.

## Usage

```

lrslim2e(
  kMax = NA_integer_,
  kMaxe1 = NA_integer_,
  hazardRatioH0e1 = 1,
  hazardRatioH0e2 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  rho = 0,
  lambda1e1 = NA_real_,
  lambda2e1 = NA_real_,
  lambda1e2 = NA_real_,

```

```

lambda2e2 = NA_real_,
gamma1e1 = 0L,
gamma2e1 = 0L,
gamma1e2 = 0L,
gamma2e2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
rho1 = 0,
rho2 = 0,
plannedEvents = NA_integer_,
plannedTime = NA_real_,
maxNumberOfIterations = 1000L,
maxNumberOfRawDatasetsPerStage = 0L,
seed = NA_integer_
)

```

### Arguments

kMax	The maximum number of stages.
kMaxe1	Number of stages with timing determined by PFS events. Ranges from 0 (none) to kMax.
hazardRatioH0e1	Hazard ratio under the null hypothesis for the active treatment vs control for endpoint 1 (PFS). Defaults to 1 for superiority test.
hazardRatioH0e2	Hazard ratio under the null hypothesis for the active treatment vs control for endpoint 2 (OS). Defaults to 1 for superiority test.
allocation1	Number of subjects in the treatment group in a randomization block. Defaults to 1 for equal randomization.
allocation2	Number of subjects in the control group in a randomization block. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
rho	The correlation coefficient for the standard bivariate normal random variables used to generate time to disease progression and time to death using the inverse CDF method.

lambda1e1	A vector of hazard rates for the event in each analysis time interval by stratum for the treatment group and endpoint 1 (PFS).
lambda2e1	A vector of hazard rates for the event in each analysis time interval by stratum for the control group and endpoint 1 (PFS).
lambda1e2	A vector of hazard rates for the event in each analysis time interval by stratum for the treatment group and endpoint 2 (OS).
lambda2e2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group and endpoint 2 (OS).
gamma1e1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the treatment group and endpoint 1 (PFS).
gamma2e1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group and endpoint 1 (PFS).
gamma1e2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the treatment group and endpoint 2 (OS).
gamma2e2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group and endpoint 2 (OS).
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
rho2	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
plannedEvents	The planned cumulative total number of PFS events at Look 1 to Look kMaxe1 and the planned cumulative total number of OS events at Look kMaxe1+1 to Look kMax.
plannedTime	The calendar times for the analyses. To use calendar time to plan the analyses, plannedEvents should be missing.
maxNumberOfIterations	The number of simulation iterations. Defaults to 1000.
maxNumberOfRawDatasetsPerStage	The number of raw datasets per stage to extract. Defaults to 1.
seed	The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified,

**Value**

A list with 2 components:

- **sumdata**: A data frame of summary data by iteration and stage:
  - **iterationNumber**: The iteration number.
  - **eventsNotAchieved**: Whether the target number of events is not achieved for the iteration.
  - **stageNumber**: The stage number, covering all stages even if the trial stops at an interim look.
  - **analysisTime**: The time for the stage since trial start.
  - **accruals1**: The number of subjects enrolled at the stage for the treatment group.
  - **accruals2**: The number of subjects enrolled at the stage for the control group.
  - **totalAccruals**: The total number of subjects enrolled at the stage.
  - **endpoint**: The endpoint (1 or 2) under consideration.
  - **events1**: The number of events at the stage for the treatment group.
  - **events2**: The number of events at the stage for the control group.
  - **totalEvents**: The total number of events at the stage.
  - **dropouts1**: The number of dropouts at the stage for the treatment group.
  - **dropouts2**: The number of dropouts at the stage for the control group.
  - **totalDropouts**: The total number of dropouts at the stage.
  - **logRankStatistic**: The log-rank test Z-statistic for the endpoint.
- **rawdata** (exists if **maxNumberOfRawDatasetsPerStage** is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
  - **iterationNumber**: The iteration number.
  - **stageNumber**: The stage under consideration.
  - **analysisTime**: The time for the stage since trial start.
  - **subjectId**: The subject ID.
  - **arrivalTime**: The enrollment time for the subject.
  - **stratum**: The stratum for the subject.
  - **treatmentGroup**: The treatment group (1 or 2) for the subject.
  - **survivalTime1**: The underlying survival time for event endpoint 1 for the subject.
  - **dropoutTime1**: The underlying dropout time for event endpoint 1 for the subject.
  - **timeUnderObservation1**: The time under observation since randomization for event endpoint 1 for the subject.
  - **event1**: Whether the subject experienced event endpoint 1.
  - **dropoutEvent1**: Whether the subject dropped out for endpoint 1.
  - **survivalTime2**: The underlying survival time for event endpoint 2 for the subject.
  - **dropoutTime2**: The underlying dropout time for event endpoint 2 for the subject.
  - **timeUnderObservation2**: The time under observation since randomization for event endpoint 2 for the subject.
  - **event2**: Whether the subject experienced event endpoint 2.
  - **dropoutEvent2**: Whether the subject dropped out for endpoint 2.



**Author(s)**

Kaifeng Lu, &lt;kaifenglu@gmail.com&gt;

**Examples**

```

sim1 = lrsim2e(
  kMax = 3,
  kMaxe1 = 2,
  allocation1 = 2,
  allocation2 = 1,
  accrualTime = c(0, 8),
  accrualIntensity = c(10, 28),
  piecewiseSurvivalTime = 0,
  rho = 0,
  lambda1e1 = log(2)/12*0.60,
  lambda2e1 = log(2)/12,
  lambda1e2 = log(2)/30*0.65,
  lambda2e2 = log(2)/30,
  accrualDuration = 20.143,
  plannedEvents = c(186, 259, 183),
  maxNumberOfIterations = 1000,
  maxNumberOfRawDatasetsPerStage = 1,
  seed = 314159)

head(sim1$sumdata)
head(sim1$rawdata)

```

---

Irsim2e3a

---

*Log-rank test simulation for two endpoints and three arms*


---

**Description**

Performs simulation for two-endpoint three-arm group sequential trials based on weighted log-rank test. The first kMaxe1 looks are driven by the total number of PFS events in Arm A and Arm C combined, and the subsequent looks are driven by the total number of OS events in Arm A and Arm C combined. Alternatively, the analyses can be planned to occur at specified calendar times.

**Usage**

```

lrsim2e3a(
  kMax = NA_integer_,
  kMaxe1 = NA_integer_,
  hazardRatioH013e1 = 1,
  hazardRatioH023e1 = 1,
  hazardRatioH012e1 = 1,
  hazardRatioH013e2 = 1,
  hazardRatioH023e2 = 1,

```

```

hazardRatioH012e2 = 1,
allocation1 = 1L,
allocation2 = 1L,
allocation3 = 1L,
accrualTime = 0L,
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
rho = 0,
lambda1e1 = NA_real_,
lambda2e1 = NA_real_,
lambda3e1 = NA_real_,
lambda1e2 = NA_real_,
lambda2e2 = NA_real_,
lambda3e2 = NA_real_,
gamma1e1 = 0L,
gamma2e1 = 0L,
gamma3e1 = 0L,
gamma1e2 = 0L,
gamma2e2 = 0L,
gamma3e2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
rho1 = 0,
rho2 = 0,
plannedEvents = NA_integer_,
plannedTime = NA_real_,
maxNumberOfIterations = 1000L,
maxNumberOfRawDatasetsPerStage = 0L,
seed = NA_integer_
)

```

### Arguments

kMax	The maximum number of stages.
kMaxe1	Number of stages with timing determined by PFS events. Ranges from 0 (none) to kMax.
hazardRatioH013e1	Hazard ratio under the null hypothesis for arm 1 vs arm 3 for endpoint 1 (PFS). Defaults to 1 for superiority test.
hazardRatioH023e1	Hazard ratio under the null hypothesis for arm 2 vs arm 3 for endpoint 1 (PFS). Defaults to 1 for superiority test.
hazardRatioH012e1	Hazard ratio under the null hypothesis for arm 1 vs arm 2 for endpoint 1 (PFS). Defaults to 1 for superiority test.

hazardRatioH013e2	Hazard ratio under the null hypothesis for arm 1 vs arm 3 for endpoint 2 (OS). Defaults to 1 for superiority test.
hazardRatioH023e2	Hazard ratio under the null hypothesis for arm 2 vs arm 3 for endpoint 2 (OS). Defaults to 1 for superiority test.
hazardRatioH012e2	Hazard ratio under the null hypothesis for arm 1 vs arm 2 for endpoint 2 (OS). Defaults to 1 for superiority test.
allocation1	Number of subjects in Arm A in a randomization block. Defaults to 1 for equal randomization.
allocation2	Number of subjects in Arm B in a randomization block. Defaults to 1 for equal randomization.
allocation3	Number of subjects in Arm C in a randomization block. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
rho	The correlation coefficient for the standard bivariate normal random variables used to generate time to disease progression and time to death using the inverse CDF method.
lambda1e1	A vector of hazard rates for the event in each analysis time interval by stratum for arm 1 and endpoint 1 (PFS).
lambda2e1	A vector of hazard rates for the event in each analysis time interval by stratum for arm 2 and endpoint 1 (PFS).
lambda3e1	A vector of hazard rates for the event in each analysis time interval by stratum for arm 3 and endpoint 1 (PFS).
lambda1e2	A vector of hazard rates for the event in each analysis time interval by stratum for arm 1 and endpoint 2 (OS).
lambda2e2	A vector of hazard rates for the event in each analysis time interval by stratum for arm 2 and endpoint 2 (OS).
lambda3e2	A vector of hazard rates for the event in each analysis time interval by stratum for arm 3 and endpoint 2 (OS).
gamma1e1	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1 and endpoint 1 (PFS).

gamma2e1	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2 and endpoint 1 (PFS).
gamma3e1	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3 and endpoint 1 (PFS).
gamma1e2	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1 and endpoint 2 (OS).
gamma2e2	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2 and endpoint 2 (OS).
gamma3e2	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3 and endpoint 2 (OS).
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
rho2	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
plannedEvents	The planned cumulative total number of PFS events at Look 1 to Look kMaxe1 for Arms A and C combined and the planned cumulative total number of OS events at Look kMaxe1+1 to Look kMax for Arms A and C combined.
plannedTime	The calendar times for the analyses. To use calendar time to plan the analyses, plannedEvents should be missing.
maxNumberOfIterations	The number of simulation iterations. Defaults to 1000.
maxNumberOfRawDatasetsPerStage	The number of raw datasets per stage to extract. Defaults to 1.
seed	The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified,

### Value

A list with 2 components:

- sumdata: A data frame of summary data by iteration and stage:
  - iterationNumber: The iteration number.
  - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.

- stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
  - analysisTime: The time for the stage since trial start.
  - accruals1: The number of subjects enrolled at the stage for the active treatment 1 group.
  - accruals2: The number of subjects enrolled at the stage for the active treatment 2 group.
  - accruals3: The number of subjects enrolled at the stage for the control group.
  - totalAccruals: The total number of subjects enrolled at the stage.
  - endpoint: The endpoint (1 or 2) under consideration.
  - events1: The number of events at the stage for the active treatment 1 group.
  - events2: The number of events at the stage for the active treatment 2 group.
  - events3: The number of events at the stage for the control group.
  - totalEvents: The total number of events at the stage.
  - dropouts1: The number of dropouts at the stage for the active treatment 1 group.
  - dropouts2: The number of dropouts at the stage for the active treatment 2 group.
  - dropouts3: The number of dropouts at the stage for the control group.
  - totalDropouts: The total number of dropouts at the stage.
  - logRankStatistic13: The log-rank test Z-statistic comparing the active treatment 1 to the control for the endpoint.
  - logRankStatistic23: The log-rank test Z-statistic comparing the active treatment 2 to the control for the endpoint.
  - logRankStatistic12: The log-rank test Z-statistic comparing the active treatment 1 to the active treatment 2 for the endpoint.
- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
    - iterationNumber: The iteration number.
    - stageNumber: The stage under consideration.
    - analysisTime: The time for the stage since trial start.
    - subjectId: The subject ID.
    - arrivalTime: The enrollment time for the subject.
    - stratum: The stratum for the subject.
    - treatmentGroup: The treatment group (1, 2, or 3) for the subject.
    - survivalTime1: The underlying survival time for event endpoint 1 for the subject.
    - dropoutTime1: The underlying dropout time for event endpoint 1 for the subject.
    - timeUnderObservation1: The time under observation since randomization for event endpoint 1 for the subject.
    - event1: Whether the subject experienced event endpoint 1.
    - dropoutEvent1: Whether the subject dropped out for endpoint 1.
    - survivalTime2: The underlying survival time for event endpoint 2 for the subject.
    - dropoutTime2: The underlying dropout time for event endpoint 2 for the subject.
    - timeUnderObservation2: The time under observation since randomization for event endpoint 2 for the subject.
    - event2: Whether the subject experienced event endpoint 2.
    - dropoutEvent2: Whether the subject dropped out for endpoint 2.

**Author(s)**

Kaifeng Lu, <kaifengl@gmail.com>

**Examples**

```
sim1 = lrsim2e3a(
  kMax = 3,
  kMaxe1 = 2,
  allocation1 = 2,
  allocation2 = 2,
  allocation3 = 1,
  accrualTime = c(0, 8),
  accrualIntensity = c(10, 28),
  piecewiseSurvivalTime = 0,
  rho = 0,
  lambda1e1 = log(2)/12*0.60,
  lambda2e1 = log(2)/12*0.70,
  lambda3e1 = log(2)/12,
  lambda1e2 = log(2)/30*0.65,
  lambda2e2 = log(2)/30*0.75,
  lambda3e2 = log(2)/30,
  accrualDuration = 30.143,
  plannedEvents = c(186, 259, 183),
  maxNumberOfIterations = 1000,
  maxNumberOfRawDatasetsPerStage = 1,
  seed = 314159)

head(sim1$sumdata)
head(sim1$rawdata)
```

---

 lrsim3a

---

*Log-rank test simulation for three arms*


---

**Description**

Performs simulation for three-arm group sequential trials based on weighted log-rank test. The looks are driven by the total number of events in Arm A and Arm C combined. Alternatively, the analyses can be planned to occur at specified calendar times.

**Usage**

```
lrsim3a(
  kMax = NA_integer_,
  hazardRatioH013 = 1,
  hazardRatioH023 = 1,
  hazardRatioH012 = 1,
  allocation1 = 1L,
```

```

allocation2 = 1L,
allocation3 = 1L,
accrualTime = 0L,
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
lambda1 = NA_real_,
lambda2 = NA_real_,
lambda3 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
gamma3 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
rho1 = 0,
rho2 = 0,
plannedEvents = NA_integer_,
plannedTime = NA_real_,
maxNumberOfIterations = 1000L,
maxNumberOfRawDatasetsPerStage = 0L,
seed = NA_integer_
)

```

### Arguments

kMax	The maximum number of stages.
hazardRatioH013	Hazard ratio under the null hypothesis for arm 1 versus arm 3. Defaults to 1 for superiority test.
hazardRatioH023	Hazard ratio under the null hypothesis for arm 2 versus arm 3. Defaults to 1 for superiority test.
hazardRatioH012	Hazard ratio under the null hypothesis for arm 1 versus arm 2. Defaults to 1 for superiority test.
allocation1	Number of subjects in Arm A in a randomization block. Defaults to 1 for equal randomization.
allocation2	Number of subjects in Arm B in a randomization block. Defaults to 1 for equal randomization.
allocation3	Number of subjects in Arm C in a randomization block. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.

<code>piecewiseSurvivalTime</code>	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
<code>stratumFraction</code>	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
<code>lambda1</code>	A vector of hazard rates for the event in each analysis time interval by stratum for arm 1.
<code>lambda2</code>	A vector of hazard rates for the event in each analysis time interval by stratum for arm 2.
<code>lambda3</code>	A vector of hazard rates for the event in each analysis time interval by stratum for arm 3.
<code>gamma1</code>	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1.
<code>gamma2</code>	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2.
<code>gamma3</code>	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3.
<code>accrualDuration</code>	Duration of the enrollment period.
<code>followupTime</code>	Follow-up time for the last enrolled subject.
<code>fixedFollowup</code>	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
<code>rho1</code>	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
<code>rho2</code>	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
<code>plannedEvents</code>	The planned cumulative total number of events at Look 1 to Look kMax for Arms A and C combined.
<code>plannedTime</code>	The calendar times for the analyses. To use calendar time to plan the analyses, <code>plannedEvents</code> should be missing.
<code>maxNumberOfIterations</code>	The number of simulation iterations. Defaults to 1000.
<code>maxNumberOfRawDatasetsPerStage</code>	The number of raw datasets per stage to extract. Defaults to 1.
<code>seed</code>	The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified,

**Value**

A list with 2 components:

- `sumdata`: A data frame of summary data by iteration and stage:



- iterationNumber: The iteration number.
  - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.
  - stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
  - analysisTime: The time for the stage since trial start.
  - accruals1: The number of subjects enrolled at the stage for the active treatment 1 group.
  - accruals2: The number of subjects enrolled at the stage for the active treatment 2 group.
  - accruals3: The number of subjects enrolled at the stage for the control group.
  - totalAccruals: The total number of subjects enrolled at the stage.
  - events1: The number of events at the stage for the active treatment 1 group.
  - events2: The number of events at the stage for the active treatment 2 group.
  - events3: The number of events at the stage for the control group.
  - totalEvents: The total number of events at the stage.
  - dropouts1: The number of dropouts at the stage for the active treatment 1 group.
  - dropouts2: The number of dropouts at the stage for the active treatment 2 group.
  - dropouts3: The number of dropouts at the stage for the control group.
  - totalDropouts: The total number of dropouts at the stage.
  - logRankStatistic13: The log-rank test Z-statistic comparing the active treatment 1 to the control.
  - logRankStatistic23: The log-rank test Z-statistic comparing the active treatment 2 to the control.
  - logRankStatistic12: The log-rank test Z-statistic comparing the active treatment 1 to the active treatment 2.
- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
    - iterationNumber: The iteration number.
    - stageNumber: The stage under consideration.
    - analysisTime: The time for the stage since trial start.
    - subjectId: The subject ID.
    - arrivalTime: The enrollment time for the subject.
    - stratum: The stratum for the subject.
    - treatmentGroup: The treatment group (1, 2, or 3) for the subject.
    - survivalTime: The underlying survival time for the subject.
    - dropoutTime: The underlying dropout time for the subject.
    - timeUnderObservation: The time under observation since randomization for the subject.
    - event: Whether the subject experienced the event.
    - dropoutEvent: Whether the subject dropped out.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

## Examples

```
sim1 = lrsm3a(
  kMax = 3,
  allocation1 = 2,
  allocation2 = 2,
  allocation3 = 1,
  accrualTime = c(0, 8),
  accrualIntensity = c(10, 28),
  piecewiseSurvivalTime = 0,
  lambda1 = log(2)/12*0.60,
  lambda2 = log(2)/12*0.70,
  lambda3 = log(2)/12,
  accrualDuration = 30.143,
  plannedEvents = c(186, 259, 295),
  maxNumberOfIterations = 1000,
  maxNumberOfRawDatasetsPerStage = 1,
  seed = 314159)

head(sim1$sumdata)
head(sim1$rawdata)
```

---

 Irstat

*Number of subjects having an event and log-rank statistics*


---

## Description

Obtains the number of subjects accrued, number of events, number of dropouts, and number of subjects reaching the maximum follow-up in each group, mean and variance of weighted log-rank score statistic, estimated hazard ratio from weighted Cox regression and variance of log hazard ratio estimate at given calendar times.

## Usage

```
lrstat(
  time = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
```

```

followupTime = NA_real_,
fixedFollowup = 0L,
rho1 = 0,
rho2 = 0,
numSubintervals = 300L,
predictTarget = 2L
)

```

## Arguments

<code>time</code>	A vector of calendar times at which to calculate the number of events and the mean and variance of log-rank test score statistic.
<code>hazardRatioH0</code>	Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.
<code>allocationRatioPlanned</code>	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
<code>accrualTime</code>	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
<code>accrualIntensity</code>	A vector of accrual intensities. One for each accrual time interval.
<code>piecewiseSurvivalTime</code>	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
<code>stratumFraction</code>	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
<code>lambda1</code>	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
<code>lambda2</code>	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
<code>gamma1</code>	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
<code>gamma2</code>	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
<code>accrualDuration</code>	Duration of the enrollment period.
<code>followupTime</code>	Follow-up time for the last enrolled subject.
<code>fixedFollowup</code>	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
<code>rho1</code>	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

<code>rho2</code>	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
<code>numSubintervals</code>	Number of sub-intervals to approximate the mean and variance of the weighted log-rank test score statistic. Defaults to 300. Specify a larger number for better approximation.
<code>predictTarget</code>	The target of prediction. Set <code>predictTarget = 1</code> to predict the number of events only. Set <code>predictTarget = 2</code> (default) to predict the number of events and log-rank score statistic mean and variance. Set <code>predictTarget = 3</code> to predict the number of events, log-rank score statistic mean and variance, and hazard ratio and variance of log hazard ratio.

### Value

A data frame containing the following variables if `predictTarget = 1`:

- `time`: The analysis time since trial start.
- `subjects`: The number of enrolled subjects.
- `nevents`: The total number of events.
- `nevents1`: The number of events in the active treatment group.
- `nevents2`: The number of events in the control group.
- `ndropouts`: The total number of dropouts.
- `ndropouts1`: The number of dropouts in the active treatment group.
- `ndropouts2`: The number of dropouts in the control group.
- `nfmax`: The total number of subjects reaching maximum follow-up.
- `nfmax1`: The number of subjects reaching maximum follow-up in the active treatment group.
- `nfmax2`: The number of subjects reaching maximum follow-up in the control group.

If `predictTarget = 2`, the following variables will also be included:

- `uscore`: The numerator of the log-rank test statistic.
- `vscore`: The variance of the log-rank score test statistic.
- `logRankZ`: The log-rank test statistic on the Z-scale.
- `hazardRatioH0`: The hazard ratio under the null hypothesis.

Furthermore, if `predictTarget = 3`, the following additional variables will also be included:

- `HR`: The average hazard ratio from weighted Cox regression.
- `vlogHR`: The variance of log hazard ratio.
- `zlogHR`: The Z-statistic for log hazard ratio.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.
```

```
lrstat(time = c(22, 40), allocationRatioPlanned = 1,
        accrualTime = seq(0, 8),
        accrualIntensity = 26/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        stratumFraction = c(0.2, 0.8),
        lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
        lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12,
        accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```

---

lrtest	<i>Log-rank test of survival curve difference</i>
--------	---

---

**Description**

Obtains the log-rank test using the Fleming-Harrington family of weights.

**Usage**

```
lrtest(
  data,
  rep = "rep",
  stratum = "stratum",
  treat = "treat",
  time = "time",
  event = "event",
  rho1 = 0,
  rho2 = 0
)
```

**Arguments**

data	<p>The input data frame that contains the following variables:</p> <ul style="list-style-type: none"> <li>• rep: The replication for by-group processing.</li> <li>• stratum: The stratum.</li> <li>• treat: The treatment.</li> <li>• time: The possibly right-censored survival time.</li> <li>• event: The event indicator.</li> </ul>
rep	<p>The name of the replication variable in the input data.</p>

stratum	The name of the stratum variable in the input data.
treat	The name of the treatment variable in the input data.
time	The name of the time variable in the input data.
event	The name of the event variable in the input data.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
rho2	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.

**Value**

A data frame with the following variables:

- rep: The replication.
- uscore: The numerator of the log-rank test statistic.
- vscore: The variance of the log-rank score test statistic.
- logRankZ: The Z-statistic value.
- logRankPValue: The one-sided p-value.
- rho1: The first parameter of the Fleming-Harrington weights.
- rho2: The second parameter of the Fleming-Harrington weights.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
df <- lrtest(data = rawdata, rep = "iterationNumber",
             stratum = "stratum", treat = "treatmentGroup",
             time = "timeUnderObservation", event = "event",
             rho1 = 0.5, rho2 = 0)
head(df)
```

---

mnOddsRatioCI	<i>Miettinen-Nurminen score confidence interval for two-sample odds ratio</i>
---------------	---

---

**Description**

Obtains the Miettinen-Nurminen score confidence interval for two-sample odds ratio possibly with stratification.

**Usage**

```
mnOddsRatioCI(  
  n1 = NA_real_,  
  y1 = NA_real_,  
  n2 = NA_real_,  
  y2 = NA_real_,  
  cilevel = 0.95  
)
```

**Arguments**

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

**Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

**Value**

A list with two components:

- data: A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:
  - n1: The sample size for the active treatment group.
  - y1: The number of responses for the active treatment group.
  - n2: The sample size for the control group.
  - y2: The number of responses for the control group.
- estimates: A data frame containing the point estimate and confidence interval for odds ratio. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
mnOddsRatioCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

---

mnRateDiffCI	<i>Miettinen-Nurminen score confidence interval for two-sample rate difference</i>
--------------	--

---

### Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample rate difference possibly with stratification.

### Usage

```
mnRateDiffCI(
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

### Arguments

t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.
cilevel	The confidence interval level.

### Details

The Mantel-Haenszel weights are used for stratified samples.

### Value

A list with two components:

- **data** A data frame containing the input exposure and number of events for each treatment group. It has the following variables:
  - t1: The exposure for the active treatment group.
  - y1: The number of events for the active treatment group.
  - t2: The exposure for the control group.
  - y2: The number of events for the control group.
- **estimates**: A data frame containing the point estimate and confidence interval for rate difference. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.



- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
mnRateDiffCI(t1 = c(10,10), y1 = c(4,3), t2 = c(20,10), y2 = c(2,0))
```

---

mnRateRatioCI	<i>Miettinen-Nurminen score confidence interval for two-sample rate ratio</i>
---------------	---

---

**Description**

Obtains the Miettinen-Nurminen score confidence interval for two-sample rate ratio possibly with stratification.

**Usage**

```
mnRateRatioCI(t1, y1, t2, y2, cilevel = 0.95)
```

**Arguments**

t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.
cilevel	The confidence interval level.

**Details**

The Mantel-Haenszel weights are used for stratified samples.

**Value**

A list with two components:

- data A data frame containing the input exposure and number of events for each treatment group. It has the following variables:
  - t1: The exposure for the active treatment group.
  - y1: The number of events for the active treatment group.

- t2: The exposure for the control group.
- y2: The number of events for the control group.
- estimates: A data frame containing the point estimate and confidence interval for rate ratio. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
mnRateRatioCI(t1 = c(10,10), y1 = c(4,3), t2 = c(20,10), y2 = c(2,0))
```

---

mnRiskDiffCI

*Miettinen-Nurminen score confidence interval for two-sample risk difference*

---

**Description**

Obtains the Miettinen-Nurminen score confidence interval for two-sample risk difference possibly with stratification.

**Usage**

```
mnRiskDiffCI(
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

**Arguments**

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

**Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

**Value**

A list with two components:

- **data** A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:
  - **n1**: The sample size for the active treatment group.
  - **y1**: The number of responses for the active treatment group.
  - **n2**: The sample size for the control group.
  - **y2**: The number of responses for the control group.
- **estimates**: A data frame containing the point estimate and confidence interval for risk difference. It has the following variables:
  - **scale**: The scale of treatment effect.
  - **estimate**: The point estimate.
  - **lower**: The lower limit of the confidence interval.
  - **upper**: The upper limit of the confidence interval.
  - **cilevel**: The confidence interval level.

**Author(s)**

Kaifeng Lu, <kweifenglu@gmail.com>

**Examples**

```
mnRiskDiffCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

---

mnRiskRatioCI

*Miettinen-Nurminen score confidence interval for two-sample risk ratio*

---

**Description**

Obtains the Miettinen-Nurminen score confidence interval for two-sample risk ratio possibly with stratification.

**Usage**

```
mnRiskRatioCI(  
  n1 = NA_real_,  
  y1 = NA_real_,  
  n2 = NA_real_,  
  y2 = NA_real_,  
  cilevel = 0.95  
)
```

**Arguments**

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

**Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

**Value**

A list with two components:

- data: A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:
  - n1: The sample size for the active treatment group.
  - y1: The number of responses for the active treatment group.
  - n2: The sample size for the control group.
  - y2: The number of responses for the control group.
- estimates: A data frame containing the point estimate and confidence interval for risk ratio. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
mnRiskRatioCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

---

mTPI2Table	<i>mTPI-2 decision table</i>
------------	------------------------------

---

**Description**

Obtains the decision table for the modified toxicity probability interval-2 (mTPI-2) design.

**Usage**

```
mTPI2Table(
  nMax = NA_integer_,
  pT = 0.3,
  epsilon1 = 0.05,
  epsilon2 = 0.05,
  a = 1,
  b = 1,
  pExcessTox = 0.95
)
```

**Arguments**

nMax	The maximum number of subjects in a dose cohort.
pT	The target toxicity probability. Defaults to 0.3.
epsilon1	The lower equivalence margin from the target. Defaults to 0.05.
epsilon2	The upper equivalence margin from the target. Defaults to 0.05.
a	The prior toxicity parameter for the beta prior.
b	The prior non-toxicity parameter for the beta prior.
pExcessTox	The threshold for excessive toxicity, i.e., if $\text{Prob}(p > pT \mid \text{Data}) > p\text{ExcessTox}$ , then the current and all higher doses will be excluded and never be used again in the remainder of the trial to avoid any other subjects receiving treatment at those doses. Defaults to 0.95.

**Value**

An S3 class mTPI2Table object with the following components:

- settings: The input settings data frame with the following variables:
  - nMax: The maximum number of subjects in a dose cohort.
  - pT: The target toxicity probability.
  - epsilon1: The lower equivalence margin from the target.
  - epsilon2: The upper equivalence margin from the target.
  - a: The prior toxicity parameter for the beta prior.
  - b: The prior non-toxicity parameter for the beta prior.
  - pExcessTox: The threshold for excessive toxicity.

- `subintervals`: The subintervals of equal length in the mTPI-2 design. It includes the following variables:
  - `lower`: The lower bound of the subinterval.
  - `upper`: The upper bound of the subinterval.
  - `decision`: The dosing decision for the subinterval.
- `decisionDataFrame`: The decision data frame for the mTPI-2 design. It includes the following variables:
  - `n`: The sample size.
  - `y`: The number of toxicities.
  - `decision`: The dosing decision.
- `decisionMatrix`: The decision matrix corresponding to the decision data frame.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
mTPI2Table(nMax = 18, pT = 0.3, epsilon1 = 0.05, epsilon2 = 0.05)
```

---

nbpower

*Power for negative binomial rate ratio*

---

### Description

Estimates the power for negative binomial rate ratio test.

### Usage

```
nbpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
```

```

accrualTime = 0L,
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
kappa1 = NA_real_,
kappa2 = NA_real_,
lambda1 = NA_real_,
lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
spendingTime = NA_real_,
studyDuration = NA_real_,
nullVariance = 0L
)

```

### Arguments

**kMax** The maximum number of stages.

**informationRates** The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**efficacyStopping** Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

**futilityStopping** Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha** The significance level. Defaults to 0.025.

**typeAlphaSpending** The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending** The user defined alpha spending. Cumulative alpha spent up to each stage.

**futilityBounds** Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to  $\text{rep}(-6, kMax-1)$  if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
rateRatioH0	Rate ratio under the null hypothesis.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
kappa1	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.
kappa2	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.
lambda1	The rate parameter of the negative binomial distribution for the active treatment group by stratum.
lambda2	The rate parameter of the negative binomial distribution for the control group by stratum.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
spendingTime	A vector of length $k\text{Max}$ for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .



studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.
nullVariance	Whether to calculate the variance for log rate ratio under the null hypothesis.

## Value

An S3 class nbpower object with 4 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - numberOfEvents: The total number of events.
  - numberOfDropouts: The total number of dropouts.
  - numbeOfSubjects: The total number of subjects.
  - exposure: The total exposure.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfEvents: The expected number of events.
  - expectedNumberOfDropouts: The expected number of dropouts.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedExposure: The expected exposure.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - accrualDuration: The accrual duration.
  - followupTime: The follow-up duration.
  - fixedFollowup: Whether a fixed follow-up design is used.
  - kMax: The number of stages.
  - rateRatioH0: The rate ratio under the null hypothesis.
  - rateRatio: The rate ratio.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.

- exposure: The exposure.
- analysisTime: The average time since trial start.
- efficacyRateRatio: The efficacy boundaries on the rate ratio scale.
- futilityRateRatio: The futility boundaries on the rate ratio scale.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accrualIntensity, piecewiseSurvivalTime, kappa1, kappa2, lambda1, lambda2, gamma1, gamma2, spendingTime, and nullVariance.
- byTreatmentCounts: A list containing the following counts by treatment group:
  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - exposure1: The exposure by stage for the treatment group.
  - numberOfEvents2: The number of events by stage for the control group.
  - numberOfDropouts2: The number of dropouts by stage for the control group.
  - numberOfSubjects2: The number of subjects by stage for the control group.
  - exposure2: The exposure by stage for the control group.
  - expectedNumberOfEvents1: The expected number of events for the treatment group.
  - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
  - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
  - expectedExposure1: The expected exposure for the treatment group.
  - expectedNumberOfEvents2: The expected number of events for control group.
  - expectedNumberOfDropouts2: The expected number of dropouts for the control group.
  - expectedNumberOfSubjects2: The expected number of subjects for the control group.
  - expectedExposure2: The expected exposure for the control group.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[nbstat](#)

**Examples**

```
# Example 1: Variable follow-up design

nbpower(kMax = 2, informationRates = c(0.5, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
```

```

    accrualIntensity = 1956/1.25,
    stratumFraction = c(0.2, 0.8),
    kappa1 = 5, kappa2 = 5,
    lambda1 = c(0.7*0.125, 0.75*0.25),
    lambda2 = c(0.125, 0.25),
    gamma1 = 0, gamma2 = 0,
    accrualDuration = 1.25,
    followupTime = 2.75, fixedFollowup = FALSE,
    nullVariance = 1)

# Example 2: Fixed follow-up design

nbpower(kMax = 2, informationRates = c(0.5, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        accrualIntensity = 220/1.5,
        kappa1 = 3, kappa2 = 3,
        lambda1 = 0.5*8.4, lambda2 = 8.4,
        gamma1 = 0, gamma2 = 0,
        accrualDuration = 1.5,
        followupTime = 0.5, fixedFollowup = TRUE)

```

---

nbpower1s

*Power for one-sample negative binomial rate*


---

### Description

Estimates the power, stopping probabilities, and expected sample size in a one-group negative binomial design.

### Usage

```

nbpower1s(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  lambdaH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,

```

```

stratumFraction = 1L,
kappa = NA_real_,
lambda = NA_real_,
gamma = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
spendingTime = NA_real_,
studyDuration = NA_real_
)

```

## Arguments

**kMax** The maximum number of stages.

**informationRates** The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**efficacyStopping** Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

**futilityStopping** Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha** The significance level. Defaults to 0.025.

**typeAlphaSpending** The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending** The user defined alpha spending. Cumulative alpha spent up to each stage.

**futilityBounds** Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to  $\text{rep}(-6, kMax-1)$  if left unspecified. The futility bounds are non-binding for the calculation of critical values.

**typeBetaSpending** The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

**parameterBetaSpending** The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

lambdaH0	The rate parameter of the negative binomial distribution under the null hypothesis.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
kappa	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) of the negative binomial distribution by stratum.
lambda	The rate parameter of the negative binomial distribution under the alternative hypothesis by stratum.
gamma	The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout by stratum. Defaults to 0 for no dropout.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
spendingTime	A vector of length <code>kMax</code> for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of <code>accrualDuration</code> and <code>followupTime</code> . If provided, the value is allowed to be less than the sum of <code>accrualDuration</code> and <code>followupTime</code> .

## Value

An S3 class `nbpower1s` object with 3 components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `numberOfEvents`: The total number of events.
  - `numberOfDropouts`: The total number of dropouts.
  - `numbeOfSubjects`: The total number of subjects.
  - `exposure`: The total exposure.
  - `studyDuration`: The total study duration.
  - `information`: The maximum information.
  - `expectedNumberOfEvents`: The expected number of events.

- expectedNumberOfDropouts: The expected number of dropouts.
- expectedNumberOfSubjects: The expected number of subjects.
- expectedExposure: The expected exposure.
- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- accrualDuration: The accrual duration.
- followupTime: The follow-up duration.
- fixedFollowup: Whether a fixed follow-up design is used.
- kMax: The number of stages.
- lambdaH0: The rate parameter of the negative binomial distribution under the null hypothesis.
- lambda: The overall rate parameter of the negative binomial distribution under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - exposure: The exposure.
  - analysisTime: The average time since trial start.
  - efficacyRate: The efficacy boundaries on the rate scale.
  - futilityRate: The futility boundaries on the rate scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, accrualTime, accrualIntensity, piecewiseSurvivalTime, stratumFraction, kappa, lambda, gamma, and spendingTime.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[nbstat](#)

**Examples**

```
# Example 1: Variable follow-up design

nbpower1s(kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  lambdaH0 = 0.125, accrualIntensity = 500,
  stratumFraction = c(0.2, 0.8),
  kappa = c(3, 5), lambda = c(0.0875, 0.085),
  gamma = 0, accrualDuration = 1.25,
  followupTime = 2.75, fixedFollowup = FALSE)

# Example 2: Fixed follow-up design

nbpower1s(kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  lambdaH0 = 8.4, accrualIntensity = 40,
  kappa = 3, lambda = 0.5*8.4,
  gamma = 0, accrualDuration = 1.5,
  followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbpowerequiv

*Power for equivalence in negative binomial rate ratio*


---

**Description**

Obtains the power for equivalence in negative binomial rate ratio.

**Usage**

```
nbpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  rateRatioLower = NA_real_,
  rateRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_real_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
```

```

lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
spendingTime = NA_real_,
studyDuration = NA_real_,
nullVariance = 0L
)

```

### Arguments

**kMax** The maximum number of stages.

**informationRates** The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha** The significance level for each of the two one-sided tests. Defaults to 0.05.

**typeAlphaSpending** The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending** The user defined alpha spending. Cumulative alpha spent up to each stage.

**rateRatioLower** The lower equivalence limit of rate ratio.

**rateRatioUpper** The upper equivalence limit of rate ratio.

**allocationRatioPlanned** Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

**accrualTime** A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g.,  $c(0, 3)$  breaks the time axis into 2 accrual intervals:  $[0, 3)$  and  $[3, \text{Inf})$ .

**accrualIntensity** A vector of accrual intensities. One for each accrual time interval.

**piecewiseSurvivalTime** A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g.,  $c(0, 6)$  breaks the time axis into 2 event intervals:  $[0, 6)$  and  $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.

**stratumFraction** A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.



kappa1	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.
kappa2	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.
lambda1	The rate parameter of the negative binomial distribution for the active treatment group by stratum.
lambda2	The rate parameter of the negative binomial distribution for the control group by stratum.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.
nullVariance	Whether to calculate the variance for log rate ratio under the null hypothesis.

## Value

An S3 class `nbpowerequiv` object with 4 components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.
  - `alpha`: The overall significance level.
  - `attainedAlphaH10`: The attained significance level under H10.
  - `attainedAlphaH20`: The attained significance level under H20.
  - `numberOfEvents`: The total number of events.
  - `numberOfDropouts`: The total number of dropouts.
  - `numbeOfSubjects`: The total number of subjects.
  - `exposure`: The total exposure.
  - `studyDuration`: The total study duration.
  - `information`: The maximum information.
  - `expectedNumberOfEvents`: The expected number of events.
  - `expectedNumberOfDropouts`: The expected number of dropouts.

- expectedNumberOfSubjects: The expected number of subjects.
- expectedExposure: The expected exposure.
- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- kMax: The number of stages.
- rateRatioLower: The lower equivalence limit of rate ratio.
- rateRatioUpper: The upper equivalence limit of rate ratio.
- rateRatio: The rate ratio.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - exposure: The exposure.
  - analysisTime: The average time since trial start.
  - efficacyRateRatioLower: The efficacy boundaries on the rate ratio scale for the one-sided null hypothesis at the lower equivalence limit.
  - efficacyRateRatioUpper: The efficacy boundaries on the rate ratio scale for the one-sided null hypothesis at the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accrualIntensity, piecewiseSurvivalTime, stratumFraction, kappa1, kappa2, lambda1, lambda2, gamma1, gamma2, accrualDuration, followupTime, fixedFollowup, spendingTime, nullVariance, and varianceRatios. The varianceRatios is a data frame with the following variables:
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.
- byTreatmentCounts: A list containing the following counts by treatment group:
  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - exposure1: The exposure by stage for the treatment group.

- numberOfEvents2: The number of events by stage for the control group.
- numberOfDropouts2: The number of dropouts by stage for the control group.
- numberOfSubjects2: The number of subjects by stage for the control group.
- exposure2: The exposure by stage for the control group.
- expectedNumberOfEvents1: The expected number of events for the treatment group.
- expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
- expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
- expectedExposure1: The expected exposure for the treatment group.
- expectedNumberOfEvents2: The expected number of events for control group.
- expectedNumberOfDropouts2: The expected number of dropouts for the control group.
- expectedNumberOfSubjects2: The expected number of subjects for the control group.
- expectedExposure2: The expected exposure for the control group.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### See Also

[nbstat](#)

### Examples

```
# Example 1: Variable follow-up design
nbpowerequiv(kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF",
  rateRatioLower = 2/3, rateRatioUpper = 3/2,
  accrualIntensity = 1956/1.25,
  kappa1 = 5, kappa2 = 5,
  lambda1 = 0.125, lambda2 = 0.125,
  gamma1 = 0, gamma2 = 0,
  accrualDuration = 1.25,
  followupTime = 2.75, fixedFollowup = FALSE,
  nullVariance = 1)

# Example 2: Fixed follow-up design
nbpowerequiv(kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF",
  rateRatioLower = 0.5, rateRatioUpper = 2,
  accrualIntensity = 220/1.5,
  stratumFraction = c(0.2, 0.8),
  kappa1 = 3, kappa2 = 3,
  lambda1 = c(8.4, 10.2),
  lambda2 = c(8.0, 11.5),
  gamma1 = 0, gamma2 = 0,
  accrualDuration = 1.5,
  followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbsamplesize

*Sample size for negative binomial rate ratio*


---

### Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a two-group negative binomial design.

### Usage

```
nbsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_real_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L,
  nullVariance = 0L
)
```

**Arguments**

beta	Type II error. Defaults to 0.2.
kMax	The maximum number of stages.
informationRates	The information rates. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to $\text{rep}(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
rateRatioH0	Rate ratio under the null hypothesis.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
kappa1	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.
kappa2	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.
lambda1	The rate parameter of the negative binomial distribution for the active treatment group by stratum.
lambda2	The rate parameter of the negative binomial distribution for the control group by stratum.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowupInterval	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
interval	The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to $c(0.001, 240)$ .
spendingTime	A vector of length <code>kMax</code> for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
nullVariance	Whether to calculate the variance for log rate ratio under the null hypothesis.

### Value

A list of two components:

- `resultsUnderH1`: An S3 class `nbpower` object under the alternative hypothesis.
- `resultsUnderH0`: An S3 class `nbpower` object under the null hypothesis.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[nbpower](#)

**Examples**

```
# Example 1: Obtains follow-up duration given power, accrual intensity,  
# and accrual duration for variable follow-up
```

```
nbsamplesize(beta = 0.2, kMax = 2,  
             informationRates = c(0.5, 1),  
             alpha = 0.025, typeAlphaSpending = "sfOF",  
             accrualIntensity = 1956/1.25,  
             kappa1 = 5, kappa2 = 5,  
             lambda1 = 0.0875, lambda2 = 0.125,  
             gamma1 = 0, gamma2 = 0,  
             accrualDuration = 1.25,  
             followupTime = NA, fixedFollowup = FALSE)
```

```
# Example 2: Obtains accrual intensity given power, accrual duration, and  
# follow-up duration for variable follow-up
```

```
nbsamplesize(beta = 0.2, kMax = 2,  
             informationRates = c(0.5, 1),  
             alpha = 0.025, typeAlphaSpending = "sfOF",  
             accrualIntensity = 100,  
             kappa1 = 5, kappa2 = 5,  
             lambda1 = 0.0875, lambda2 = 0.125,  
             gamma1 = 0, gamma2 = 0,  
             accrualDuration = 1.25,  
             followupTime = 2.25, fixedFollowup = FALSE)
```

```
# Example 3: Obtains accrual duration given power, accrual intensity, and  
# follow-up duration for fixed follow-up
```

```
nbsamplesize(beta = 0.2, kMax = 2,  
             informationRates = c(0.5, 1),  
             alpha = 0.025, typeAlphaSpending = "sfOF",  
             accrualIntensity = 1667,  
             stratumFraction = c(0.2, 0.8),  
             kappa1 = 5, kappa2 = 5,  
             lambda1 = c(0.7*0.125, 0.75*0.25),  
             lambda2 = c(0.125, 0.25),  
             gamma1 = 0, gamma2 = 0,  
             accrualDuration = NA,  
             followupTime = 0.5, fixedFollowup = TRUE)
```

---

nbsamplesize1s      *Sample size for one-sample negative binomial rate*

---

### Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a one-group negative binomial design.

### Usage

```
nbsamplesize1s(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  lambdaH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa = NA_real_,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

### Arguments

beta	Type II error. Defaults to 0.2.
kMax	The maximum number of stages.



informationRates	The information rates. Defaults to $(1:kMax) / kMax$ if left unspecified.
efficacyStopping	Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.
futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., $kMax-1$ . Defaults to $rep(-6, kMax-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
lambdaH0	The rate parameter of the negative binomial distribution under the null hypothesis.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, Inf)$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, Inf)$ . Defaults to 0 for exponential distribution.

stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
kappa	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) of the negative binomial distribution by stratum.
lambda	The rate parameter of the negative binomial distribution under the alternative hypothesis by stratum.
gamma	The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout by stratum. Defaults to 0 for no dropout.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
interval	The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to $c(0.001, 240)$ .
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

**Value**

A list of two components:

- resultsUnderH1: An S3 class nbpower1s object under the alternative hypothesis.
- resultsUnderH0: An S3 class nbpower1s object under the null hypothesis.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[nbpower1s](#)

**Examples**

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up
```

```
nbsamplesize1s(beta = 0.2, kMax = 2,
  informationRates = c(0.5, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  lambdaH0 = 0.125, accrualIntensity = 500,
  stratumFraction = c(0.2, 0.8),
  kappa = c(3, 5), lambda = c(0.0875, 0.085),
  gamma = 0, accrualDuration = 1.25,
  followupTime = NA, fixedFollowup = FALSE)
```

```
# Example 2: Obtains accrual intensity given power, accrual duration, and
```

```

# follow-up duration for variable follow-up

nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               lambdaH0 = 0.125, accrualIntensity = 100,
               kappa = 5, lambda = 0.0875,
               gamma = 0, accrualDuration = 1.25,
               followupTime = 2.25, fixedFollowup = FALSE)

# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up

nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               lambdaH0 = 8.4, accrualIntensity = 40,
               kappa = 3, lambda = 4.2,
               gamma = 0, accrualDuration = NA,
               followupTime = 0.5, fixedFollowup = TRUE)

```

---

nbsamplesizeequiv      *Sample size for equivalence in negative binomial rate ratio*

---

## Description

Obtains the sample size for equivalence in negative binomial rate ratio.

## Usage

```

nbsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  rateRatioLower = NA_real_,
  rateRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_real_,

```

```

kappa2 = NA_real_,
lambda1 = NA_real_,
lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
interval = as.numeric(c(0.001, 240)),
spendingTime = NA_real_,
rounding = 1L,
nullVariance = 0L
)

```

### Arguments

**beta**            The type II error.

**kMax**            The maximum number of stages.

**informationRates**  
                  The information rates. Defaults to (1:kMax) / kMax if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha**            The significance level for each of the two one-sided tests. Defaults to 0.05.

**typeAlphaSpending**  
                  The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending**  
                  The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending**  
                  The user defined alpha spending. Cumulative alpha spent up to each stage.

**rateRatioLower** The lower equivalence limit of rate ratio.

**rateRatioUpper** The upper equivalence limit of rate ratio.

**allocationRatioPlanned**  
                  Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

**accrualTime**     A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

**accrualIntensity**  
                  A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
kappa1	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.
kappa2	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.
lambda1	The rate parameter of the negative binomial distribution for the active treatment group by stratum.
lambda2	The rate parameter of the negative binomial distribution for the control group by stratum.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowupInterval	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
interval	The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to $c(0.001, 240)$ .
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
nullVariance	Whether to calculate the variance for log rate ratio under the null hypothesis.

**Value**

An S3 class `nbpowerequiv` object

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[nbpowerequiv](#)

## Examples

```
# Example 1: Variable follow-up design and solve for follow-up time
nbsamplesizeequiv(beta = 0.1, kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF",
  rateRatioLower = 2/3, rateRatioUpper = 3/2,
  accrualIntensity = 1956/1.25,
  stratumFraction = c(0.2, 0.8),
  kappa1 = c(3, 5),
  kappa2 = c(2, 3),
  lambda1 = c(0.125, 0.165),
  lambda2 = c(0.135, 0.175),
  gamma1 = -log(1-0.05),
  gamma2 = -log(1-0.10),
  accrualDuration = 1.25,
  followupTime = NA, fixedFollowup = FALSE,
  nullVariance = 1)
```

```
# Example 2: Fixed follow-up design and solve for accrual duration
nbsamplesizeequiv(beta = 0.2, kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF",
  rateRatioLower = 0.5, rateRatioUpper = 2,
  accrualIntensity = 220/1.5,
  kappa1 = 3, kappa2 = 3,
  lambda1 = 8.4, lambda2 = 8.4,
  gamma1 = 0, gamma2 = 0,
  accrualDuration = NA,
  followupTime = 0.5, fixedFollowup = TRUE)
```

---

 nbstat

*Negative binomial rate ratio*


---

## Description

Obtains the number of subjects accrued, number of events, number of dropouts, number of subjects reaching the maximum follow-up, total exposure, and variance for log rate in each group, rate ratio, variance, and Wald test statistic of log rate ratio at given calendar times.

## Usage

```
nbstat(
  time = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
```

```

kappa1 = NA_real_,
kappa2 = NA_real_,
lambda1 = NA_real_,
lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
nullVariance = 0L
)

```

### Arguments

time	A vector of calendar times for data cut.
rateRatioH0	Rate ratio under the null hypothesis.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
kappa1	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.
kappa2	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.
lambda1	The rate parameter of the negative binomial distribution for the active treatment group by stratum.
lambda2	The rate parameter of the negative binomial distribution for the control group by stratum.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
nullVariance	Whether to calculate the variance for log rate ratio under the null hypothesis.

### Details

The probability mass function for a negative binomial distribution with dispersion parameter  $\kappa_i$  and rate parameter  $\lambda_i$  is given by

$$P(Y_{ij} = y) = \frac{\Gamma(y + 1/\kappa_i)}{\Gamma(1/\kappa_i)y!} \left( \frac{1}{1 + \kappa_i \lambda_i t_{ij}} \right)^{1/\kappa_i} \left( \frac{\kappa_i \lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}} \right)^y,$$

where  $Y_{ij}$  is the event count for subject  $j$  in treatment group  $i$ , and  $t_{ij}$  is the exposure time for the subject. If  $\kappa_i = 0$ , the negative binomial distribution reduces to the Poisson distribution.

For treatment group  $i$ , let  $\beta_i = \log(\lambda_i)$ . The likelihood for  $\{(\kappa_i, \beta_i) : i = 1, 2\}$  can be written as

$$l = \sum_{i=1}^2 \sum_{j=1}^{n_i} \{ \log \Gamma(y_{ij} + 1/\kappa_i) - \log \Gamma(1/\kappa_i) + y_{ij}(\log(\kappa_i) + \beta_i) - (y_{ij} + 1/\kappa_i) \log(1 + \kappa_i \exp(\beta_i) t_{ij}) \}.$$

It follows that

$$\frac{\partial l}{\partial \beta_i} = \sum_{j=1}^{n_i} \left\{ y_{ij} - (y_{ij} + 1/\kappa_i) \frac{\kappa_i \exp(\beta_i) t_{ij}}{1 + \kappa_i \exp(\beta_i) t_{ij}} \right\},$$

and

$$-\frac{\partial^2 l}{\partial \beta_i^2} = \sum_{j=1}^{n_i} (y_{ij} + 1/\kappa_i) \frac{\kappa_i \lambda_i t_{ij}}{(1 + \kappa_i \lambda_i t_{ij})^2}.$$

The Fisher information for  $\beta_i$  is

$$E \left( -\frac{\partial^2 l}{\partial \beta_i^2} \right) = n_i E \left( \frac{\lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}} \right).$$

In addition, we can show that

$$E \left( -\frac{\partial^2 l}{\partial \beta_i \partial \kappa_i} \right) = 0.$$

Therefore, the variance of  $\hat{\beta}_i$  is

$$\text{Var}(\hat{\beta}_i) = \frac{1}{n_i} \left\{ E \left( \frac{\lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}} \right) \right\}^{-1}.$$

To evaluate the integral, we need to obtain the distribution of the exposure time,

$$t_{ij} = \min(\tau - W_{ij}, C_{ij}, T_{fmax}),$$

where  $\tau$  denotes the calendar time since trial start,  $W_{ij}$  denotes the enrollment time for subject  $j$  in treatment group  $i$ ,  $C_{ij}$  denotes the time to dropout after enrollment for subject  $j$  in treatment group  $i$ , and  $T_{fmax}$  denotes the maximum follow-up time for all subjects. Therefore,

$$P(t_{ij} \geq t) = P(W_{ij} \leq \tau - t)P(C_{ij} \geq t)I(t \leq T_{fmax}).$$



Let  $H$  denote the distribution function of the enrollment time, and  $G_i$  denote the survival function of the dropout time for treatment group  $i$ . By the change of variables, we have

$$E\left(\frac{\lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}}\right) = \int_0^{\tau \wedge T_{fmax}} \frac{\lambda_i}{(1 + \kappa_i \lambda_i t)^2} H(\tau - t) G_i(t) dt.$$

A numerical integration algorithm for a univariate function can be used to evaluate the above integral.

For the restricted maximum likelihood (reml) estimate of  $(\beta_1, \beta_2)$  subject to the constraint that  $\beta_1 - \beta_2 = \Delta$ , we express the log-likelihood in terms of  $(\beta_2, \Delta, \kappa_1, \kappa_2)$ , and takes the derivative of the log-likelihood function with respect to  $\beta_2$ . The resulting score equation has asymptotic limit

$$E\left(\frac{\partial l}{\partial \beta_2}\right) = s_1 + s_2,$$

where

$$s_1 = nrE\left\{\lambda_1 t_{1j} - \left(\lambda_1 t_{1j} + \frac{1}{\kappa_1}\right) \frac{\kappa_1 e^{\tilde{\beta}_2 + \Delta t_{1j}}}{1 + \kappa_1 e^{\tilde{\beta}_2 + \Delta t_{1j}}}\right\},$$

and

$$s_2 = n(1 - r)E\left\{\lambda_2 t_{2j} - \left(\lambda_2 t_{2j} + \frac{1}{\kappa_2}\right) \frac{\kappa_2 e^{\tilde{\beta}_2 t_{2j}}}{1 + \kappa_2 e^{\tilde{\beta}_2 t_{2j}}}\right\}.$$

Here  $r$  is the randomization probability for the active treatment group. The asymptotic limit of the reml of  $\beta_2$  is the solution  $\tilde{\beta}_2$  to  $E\left(\frac{\partial l}{\partial \beta_2}\right) = 0$ .

## Value

A list with two components:

- resultsUnderH1: A data frame containing the following variables:
  - time: The analysis time since trial start.
  - subjects: The number of enrolled subjects.
  - nevents: The total number of events.
  - nevents1: The number of events in the active treatment group.
  - nevents2: The number of events in the control group.
  - ndropouts: The total number of dropouts.
  - ndropouts1: The number of dropouts in the active treatment group.
  - ndropouts2: The number of dropouts in the control group.
  - nfmax: The total number of subjects reaching maximum follow-up.
  - nfmax1: The number of subjects reaching maximum follow-up in the active treatment group.
  - nfmax2: The number of subjects reaching maximum follow-up in the control group.
  - exposure: The total exposure time.
  - exposure1: The exposure time for the active treatment group.
  - exposure2: The exposure time for the control group.
  - rateRatio: The rate ratio of the active treatment group versus the control group.

- vlogRate1: The variance for the log rate parameter for the active treatment group.
- vlogRate2: The variance for the log rate parameter for the control group.
- vlogRR: The variance of log rate ratio.
- information: The information of log rate ratio.
- zlogRR: The Z-statistic for log rate ratio.
- resultsUnderH0 when nullVariance = TRUE: A data frame with the following variables:
  - time: The analysis time since trial start.
  - lambda1H0: The restricted maximum likelihood estimate of the event rate for the active treatment group.
  - lambda2H0: The restricted maximum likelihood estimate of the event rate for the control group.
  - rateRatioH0: The rate ratio under H0.
  - vlogRate1H0: The variance for the log rate parameter for the active treatment group under H0.
  - vlogRate2H0: The variance for the log rate parameter for the control group under H0.
  - vlogRRH0: The variance of log rate ratio under H0.
  - informationH0: The information of log rate ratio under H0.
  - zlogRRH0: The Z-statistic for log rate ratio with variance evaluated under H0.
  - varianceRatio: The ratio of the variance under H0 versus the variance under H1.
  - lambda1: The true event rate for the active treatment group.
  - lambda2: The true event rate for the control group.
  - rateRatio: The true rate ratio.
- resultsUnderH0 when nullVariance = FALSE: A data frame with the following variables:
  - time: The analysis time since trial start.
  - rateRatioH0: The rate ratio under H0.
  - varianceRatio: Equal to 1.
  - lambda1: The true event rate for the active treatment group.
  - lambda2: The true event rate for the control group.
  - rateRatio: The true rate ratio.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
# Example 1: Variable follow-up design
```

```
nbstat(time = c(1, 1.25, 2, 3, 4),
        accrualIntensity = 1956/1.25,
        kappa1 = 5,
        kappa2 = 5,
        lambda1 = 0.7*0.125,
        lambda2 = 0.125,
        gamma1 = 0,
```

```

    gamma2 = 0,
    accrualDuration = 1.25,
    followupTime = 2.75)

# Example 2: Fixed follow-up design

nbstat(time = c(0.5, 1, 1.5, 2),
        accrualIntensity = 220/1.5,
        stratumFraction = c(0.2, 0.8),
        kappa1 = 3,
        kappa2 = 3,
        lambda1 = c(0.5*8.4, 0.6*10.5),
        lambda2 = c(8.4, 10.5),
        gamma1 = 0,
        gamma2 = 0,
        accrualDuration = 1.5,
        followupTime = 0.5,
        fixedFollowup = 1,
        nullVariance = 1)

```

---

ptpwerp

*Distribution function of truncated piecewise exponential distribution*


---

## Description

Obtains the probability of a truncated piecewise exponential distribution.

## Usage

```

ptpwerp(
  q,
  piecewiseSurvivalTime = 0,
  lambda = 0.0578,
  lowerBound = 0,
  lower.tail = TRUE,
  log.p = FALSE
)

```

## Arguments

<code>q</code>	The vector of quantiles.
<code>piecewiseSurvivalTime</code>	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., <code>c(0, 6)</code> breaks the time axis into 2 event intervals: <code>[0, 6)</code> and <code>[6, Inf)</code> . Defaults to 0 for exponential distribution.
<code>lambda</code>	A vector of hazard rates for the event. One for each analysis time interval.

lowerBound	The left truncation time point for the survival time. Defaults to 0 for no truncation.
lower.tail	Logical; if TRUE (default), probabilities are $P(X \leq x)$ , otherwise, $P(X > x)$ .
log.p	Logical; if TRUE, probabilities p are given as $\log(p)$ .

**Value**

The probability p such that  $P(X > q \mid X > \text{lowerBound}) = 1 - p$ .

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
ptpwexp(q = c(8, 18), piecewiseSurvivalTime = c(0, 6, 9, 15),
        lambda = c(0.025, 0.04, 0.015, 0.007))
```

---

pwexpcuts

*Piecewise exponential approximation to a survival distribution*

---

**Description**

Obtains the piecewise exponential distribution that approximates a survival distribution.

**Usage**

```
pwexpcuts(S, ...)
```

**Arguments**

S	The survival function of a univariate survival time.
...	Additional arguments to be passed to S.

**Value**

A list with three components:

- `piecewiseSurvivalTime`: A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: `[0, 6)` and `[6, Inf)`.
- `lambda`: A vector of hazard rates for the event. One for each analysis time interval.
- `loglik`: The sequence of the asymptotic limit of the piecewise exponential log-likelihood for an increasing number of change points.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Example 1: Piecewise exponential
pwexpcuts(ptpwexp, piecewiseSurvivalTime = c(0, 3.4, 5.5),
          lambda = c(0.0168, 0.0833, 0.0431), lowerBound = 0,
          lower.tail = FALSE)

# Example 2: Weibull
pwexpcuts(pweibull, shape = 1.37, scale = 1/0.818, lower.tail = FALSE)
```

---

pwexploglik

*Profile log-likelihood function for the change points in piecewise exponential approximation*

---

**Description**

Obtains the profile log-likelihood function for the change points in the piecewise exponential approximation to a survival function.

**Usage**

```
pwexploglik(tau, S, ...)
```

**Arguments**

tau	The numeric vector of change points.
S	The survival function of a univariate survival time.
...	Additional arguments to be passed to S.

**Value**

A list with the following three components:

- `piecewiseSurvivalTime`: A vector that specifies the starting time of piecewise exponential survival time intervals.
- `lambda`: A vector of hazard rates for the event. One for each analysis time interval.
- `loglik`: The value of the profile log-likelihood.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
pwexploglik(tau = c(0.5, 1.2, 2.8), pweibull,
            shape = 1.37, scale = 1/0.818, lower.tail = FALSE)
```

qtpwexp

*Quantile function of truncated piecewise exponential distribution***Description**

Obtains the quantile of a truncated piecewise exponential distribution.

**Usage**

```
qtpwexp(
  p,
  piecewiseSurvivalTime = 0,
  lambda = 0.0578,
  lowerBound = 0,
  lower.tail = TRUE,
  log.p = FALSE
)
```

**Arguments**

p	The vector of probabilities.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
lambda	A vector of hazard rates for the event. One for each analysis time interval.
lowerBound	The left truncation time point for the survival time. Defaults to 0 for no truncation.
lower.tail	Logical; if TRUE (default), probabilities are $P(X \leq x)$ , otherwise, $P(X > x)$ .
log.p	Logical; if TRUE, probabilities p are given as log(p).

**Value**

The quantile q such that  $P(X > q \mid X > \text{lowerBound}) = 1 - p$ .

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
qtpwexp(p = c(0.205, 0.317), piecewiseSurvivalTime = c(0, 6, 9, 15),
        lambda = c(0.025, 0.04, 0.015, 0.007))
```

---

rawdata	<i>A simulated time-to-event data set with 10 replications</i>
---------	--

---

**Description**

A simulated data set with stratification and delayed treatment effect:

iterationNumber The iteration number  
 arrivalTime The enrollment time for the subject  
 stratum The stratum for the subject  
 treatmentGroup The treatment group for the subject  
 timeUnderObservation The time under observation since randomization  
 event Whether the subject experienced the event  
 dropoutEvent Whether the subject dropped out

**Usage**

```
rawdata
```

**Format**

An object of class `data.frame` with 4910 rows and 7 columns.

---

remlOddsRatio	<i>REML estimates of individual proportions with specified odds ratio</i>
---------------	---

---

**Description**

Obtains the restricted maximum likelihood estimates of individual proportions with specified odds ratio.

**Usage**

```
remlOddsRatio(
  oddsRatioH0 = 1,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
)
```

**Arguments**

oddsRatioH0	The specified odds ratio.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

**Value**

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
remlOddsRatio(oddsRatioH0 = 1.25, n1 = 10, y1 = 4, n2 = 20, y2 = 2)
```

---

remlRateDiff

*REML estimates of individual rates with specified rate difference*

---

**Description**

Obtains the restricted maximum likelihood estimates of individual proportions with specified rate difference.

**Usage**

```
remlRateDiff(  
  rateDiffH0 = 0,  
  t1 = NA_real_,  
  y1 = NA_real_,  
  t2 = NA_real_,  
  y2 = NA_real_  
)
```

**Arguments**

rateDiffH0	The specified rate difference.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.



**Value**

A vector of the restricted maximum likelihood estimates of the incidence rates for the two treatment groups.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
remlRateDiff(rateDiffH0 = 0.1, t1 = 10, y1 = 4, t2 = 20, y2 = 2)
```

---

remlRateRatio

*REML estimates of individual rates with specified rate ratio*

---

**Description**

Obtains the restricted maximum likelihood estimates of individual proportions with specified rate ratio.

**Usage**

```
remlRateRatio(  
  rateRatioH0 = 1,  
  t1 = NA_real_,  
  y1 = NA_real_,  
  t2 = NA_real_,  
  y2 = NA_real_  
)
```

**Arguments**

rateRatioH0	The specified rate ratio.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

**Value**

A vector of the restricted maximum likelihood estimates of the incidence rates for the two treatment groups.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
remlRateRatio(rateRatioH0 = 1.1, t1 = 10, y1 = 4, t2 = 20, y2 = 2)
```

---

remlRiskDiff	<i>REML estimates of individual proportions with specified risk difference</i>
--------------	--

---

**Description**

Obtains the restricted maximum likelihood estimates of individual proportions with specified risk difference.

**Usage**

```
remlRiskDiff(  
  riskDiffH0 = 0,  
  n1 = NA_real_,  
  y1 = NA_real_,  
  n2 = NA_real_,  
  y2 = NA_real_  
)
```

**Arguments**

riskDiffH0	The specified risk difference.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

**Value**

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
remlRiskDiff(riskDiffH0 = 0.1, n1 = 10, y1 = 4, n2 = 20, y2 = 0)
```

---

`remlRiskRatio`*REML estimates of individual proportions with specified risk ratio*

---

**Description**

Obtains the restricted maximum likelihood estimates of individual proportions with specified risk ratio.

**Usage**

```
remlRiskRatio(  
  riskRatioH0 = 1,  
  n1 = NA_real_,  
  y1 = NA_real_,  
  n2 = NA_real_,  
  y2 = NA_real_  
)
```

**Arguments**

<code>riskRatioH0</code>	The specified risk ratio.
<code>n1</code>	The sample size for the active treatment group.
<code>y1</code>	The number of responses for the active treatment group.
<code>n2</code>	The sample size for the control group.
<code>y2</code>	The number of responses for the control group.

**Value**

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
remlRiskRatio(riskRatioH0 = 1.2, n1 = 10, y1 = 4, n2 = 20, y2 = 2)
```

---

repeatedPValue      *Repeated p-values for group sequential design*

---

### Description

Obtains the repeated p-values for a group sequential design.

### Usage

```
repeatedPValue(
  kMax,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA,
  maxInformation = 1,
  p,
  information,
  spendingTime = NULL
)
```

### Arguments

kMax	The maximum number of stages.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
maxInformation	The target maximum information. Defaults to 1, in which case, information represents informationRates.
p	The raw p-values at look 1 to look k. It can be a matrix with k columns for k <= kMax.
information	The observed information by look. It can be a matrix with k columns.
spendingTime	The error spending time at each analysis, must be increasing and less than or equal to 1. Defaults to NULL, in which case, it is the same as informationRates derived from information and maxInformation. It can be a matrix with k columns.

### Value

The repeated p-values at look 1 to look k.

**Author(s)**

Kaifeng Lu, <kaifengl@gmail.com>

**Examples**

```
# Example 1: informationRates different from spendingTime
repeatedPValue(kMax = 3, typeAlphaSpending = "sfOF",
               maxInformation = 800,
               p = c(0.2, 0.15, 0.1),
               information = c(529, 700, 800),
               spendingTime = c(0.6271186, 0.8305085, 1))

# Example 2: Maurer & Bretz (2013), current look is not the last look
repeatedPValue(kMax = 3, typeAlphaSpending = "sfOF",
               p = matrix(c(0.0062, 0.017,
                           0.009, 0.13,
                           0.0002, 0.0035,
                           0.002, 0.06),
                          nrow=4, ncol=2),
               information = c(1/3, 2/3))
```

---

riskDiffExactCI

*Exact unconditional confidence interval for risk difference*

---

**Description**

Obtains the exact unconditional confidence interval for risk difference based on the standardized score statistic.

**Usage**

```
riskDiffExactCI(
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

**Arguments**

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

**Value**

A data frame containing the following variables:

- scale: The scale of treatment effect.
- estimate: The point estimate.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
riskDiffExactCI(n1 = 68, y1 = 2, n2 = 65, y2 = 1, cilevel = 0.95)
```

---

riskDiffExactPValue     *P-value for exact unconditional test of risk difference*

---

**Description**

Obtains the p-value for exact unconditional test of risk difference.

**Usage**

```
riskDiffExactPValue(  
  riskDiffH0 = 0,  
  directionUpper = 1L,  
  n1 = NA_real_,  
  y1 = NA_real_,  
  n2 = NA_real_,  
  y2 = NA_real_  
)
```

**Arguments**

riskDiffH0	The risk difference under the null hypothesis. Defaults to 0.
directionUpper	Whether larger values represent better responses.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

**Value**

A data frame containing the following variables:

- riskDiffH0: The risk difference under the null hypothesis.
- directionUpper: Whether larger values represent better responses.
- riskDiff: The observed risk difference.
- zstat: The observed value of the Z test statistic.
- pvalue: The one-sided p-value for the unconditional exact test.
- pi2star: The value of pi2 that yields the p-value.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
riskDiffExactPValue(riskDiffH0 = 0, directionUpper = 1,
                    n1 = 68, y1 = 2, n2 = 65, y2 = 1)
```

---

riskRatioExactCI	<i>Exact unconditional confidence interval for risk ratio</i>
------------------	---

---

**Description**

Obtains the exact unconditional confidence interval for risk ratio based on the standardized score statistic.

**Usage**

```
riskRatioExactCI(
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

**Arguments**

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

**Value**

A data frame containing the following variables:

- scale: The scale of treatment effect.
- estimate: The point estimate.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
riskRatioExactCI(n1 = 68, y1 = 2, n2 = 65, y2 = 1, cilevel = 0.95)
```

---

riskRatioExactPValue *P-value for exact unconditional test of risk ratio*

---

**Description**

Obtains the p-value for exact unconditional test of risk ratio.

**Usage**

```
riskRatioExactPValue(
  riskRatioH0 = 1,
  directionUpper = 1L,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
)
```

**Arguments**

riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
directionUpper	Whether larger values represent better responses.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.



**Value**

A data frame containing the following variables:

- riskRatioH0: The risk ratio under the null hypothesis.
- directionUpper: Whether larger values represent better responses.
- riskRatio: The observed risk ratio.
- zstat: The observed value of the Z test statistic.
- pvalue: The one-sided p-value for the unconditional exact test.
- pi2star: The value of  $\pi^2$  that yields the p-value.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
riskRatioExactPValue(riskRatioH0 = 1, directionUpper = 1,  
                     n1 = 68, y1 = 2, n2 = 65, y2 = 1)
```

---

rmdiff

*Estimate of restricted mean survival time difference*

---

**Description**

Obtains the estimate of restricted mean survival time difference between two treatment groups.

**Usage**

```
rmdiff(  
  data,  
  rep = "rep",  
  stratum = "stratum",  
  treat = "treat",  
  time = "time",  
  event = "event",  
  milestone = NA_real_,  
  rmstDiffH0 = 0,  
  confint = 0.95,  
  biascorrection = 0L  
)
```

**Arguments**

<code>data</code>	The input data frame that contains the following variables: <ul style="list-style-type: none"> <li>• <code>rep</code>: The replication for by-group processing.</li> <li>• <code>stratum</code>: The stratum.</li> <li>• <code>treat</code>: The treatment.</li> <li>• <code>time</code>: The possibly right-censored survival time.</li> <li>• <code>event</code>: The event indicator.</li> </ul>
<code>rep</code>	The name of the replication variable in the input data.
<code>stratum</code>	The name of the stratum variable in the input data.
<code>treat</code>	The name of the treatment variable in the input data.
<code>time</code>	The name of the time variable in the input data.
<code>event</code>	The name of the event variable in the input data.
<code>milestone</code>	The milestone time at which to calculate the restricted mean survival time.
<code>rmstDiffH0</code>	The difference in restricted mean survival times under the null hypothesis. Defaults to 0 for superiority test.
<code>confint</code>	The level of the two-sided confidence interval for the difference in restricted mean survival times. Defaults to 0.95.
<code>biascorrection</code>	Whether to apply bias correction for the variance estimate of individual restricted mean survival times. Defaults to no bias correction.

**Value**

A data frame with the following variables:

- `rep`: The replication number.
- `milestone`: The milestone time relative to randomization.
- `rmstDiffH0`: The difference in restricted mean survival times under the null hypothesis.
- `rmst1`: The estimated restricted mean survival time for the treatment group.
- `rmst2`: The estimated restricted mean survival time for the control group.
- `rmstDiff`: The estimated difference in restricted mean survival times.
- `vrms1`: The variance for `rmst1`.
- `vrms2`: The variance for `rmst2`.
- `vrmsDiff`: The variance for `rmstDiff`.
- `rmstDiffZ`: The Z-statistic value.
- `rmstDiffPValue`: The one-sided p-value.
- `lower`: The lower bound of confidence interval.
- `upper`: The upper bound of confidence interval.
- `confint`: The level of confidence interval.
- `biascorrection`: Whether to apply bias correction for the variance estimate of individual restricted mean survival times.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
df <- rmdiff(data = rawdata, rep = "iterationNumber",
             stratum = "stratum", treat = "treatmentGroup",
             time = "timeUnderObservation", event = "event",
             milestone = 12)
head(df)
```

---

 rmest

*Estimate of restricted mean survival time*


---

**Description**

Obtains the estimate of restricted means survival time for each stratum.

**Usage**

```
rmest(
  data,
  rep = "rep",
  stratum = "stratum",
  time = "time",
  event = "event",
  milestone = NA_real_,
  confint = 0.95,
  biascorrection = 0L
)
```

**Arguments**

data	The input data frame that contains the following variables: <ul style="list-style-type: none"> <li>• rep: The replication for by-group processing.</li> <li>• stratum: The stratum.</li> <li>• time: The possibly right-censored survival time.</li> <li>• event: The event indicator.</li> </ul>
rep	The name of the replication variable in the input data.
stratum	The name of the stratum variable in the input data.
time	The name of the time variable in the input data.
event	The name of the event variable in the input data.
milestone	The milestone time at which to calculate the restricted mean survival time.

confint	The level of the two-sided confidence interval for the survival probabilities. Defaults to 0.95.
biascorrection	Whether to apply bias correction for the variance estimate. Defaults to no bias correction.

### Value

A data frame with the following variables:

- rep: The replication.
- stratum: The stratum variable.
- size: The number of subjects in the stratum.
- milestone: The milestone time relative to randomization.
- rmst: The estimate of restricted mean survival time.
- stderr: The standard error of the estimated rmst.
- lower: The lower bound of confidence interval if requested.
- upper: The upper bound of confidence interval if requested.
- confint: The level of confidence interval if requested.
- biascorrection: Whether to apply bias correction for the variance estimate.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
rmmest(data = survival::aml, stratum = "x",
       time = "time", event = "status", milestone = 24)
```

---

rmpower

*Power for difference in restricted mean survival times*

---

### Description

Estimates the power for testing the difference in restricted mean survival times in a two-sample survival design.

**Usage**

```

rmpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  milestone = NA_real_,
  rmstDiffH0 = 0,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)

```

**Arguments**

**kMax**                    The maximum number of stages.

**informationRates**                    The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**efficacyStopping**                    Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

**futilityStopping**                    Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

**criticalValues**                    Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha**                    The significance level. Defaults to 0.025.

**typeAlphaSpending**                    The type of alpha spending. One of the following: "OF" for O'Brien-Fleming

boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending** The user defined alpha spending. Cumulative alpha spent up to each stage.

**futilityBounds** Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

**typeBetaSpending** The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

**parameterBetaSpending** The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

**milestone** The milestone time at which to calculate the restricted mean survival time.

**rmstDiffH0** The difference in restricted mean survival times under the null hypothesis. Defaults to 0 for superiority test.

**allocationRatioPlanned** Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

**accrualTime** A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

**accrualIntensity** A vector of accrual intensities. One for each accrual time interval.

**piecewiseSurvivalTime** A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

**stratumFraction** A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

**lambda1** A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

**lambda2** A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

**gamma1** The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

## Value

An S3 class rmpower object with 3 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - drift: The drift parameter, equal to  $(\text{rmstDiff} - \text{rmstDiffH0}) * \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numbeOfSubjects: The total number of subjects.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - accrualDuration: The accrual duration.
  - followupTime: The follow-up duration.
  - fixedFollowup: Whether a fixed follow-up design is used.
  - kMax: The number of stages.
  - milestone: The milestone time relative to randomization.
  - rmstDiffH0: The difference in restricted mean survival times under the null hypothesis.
  - rmst1: The restricted mean survival time for the treatment group.
  - rmst2: The restricted mean survival time for the control group.
  - rmstDiff: The difference in restricted mean survival times, equal to  $\text{rmst1} - \text{rmst2}$ .
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.

- `futilityPerStage`: The probability for futility stopping.
  - `cumulativeRejection`: The cumulative probability for efficacy stopping.
  - `cumulativeFutility`: The cumulative probability for futility stopping.
  - `cumulativeAlphaSpent`: The cumulative alpha spent.
  - `numberOfSubjects`: The number of subjects.
  - `analysisTime`: The average time since trial start.
  - `efficacyRmstDiff`: The efficacy boundaries on the restricted mean survival time difference scale.
  - `futilityRmstDiff`: The futility boundaries on the restricted mean survival time difference scale.
  - `efficacyP`: The efficacy boundaries on the p-value scale.
  - `futilityP`: The futility boundaries on the p-value scale.
  - `information`: The cumulative information.
  - `efficacyStopping`: Whether to allow efficacy stopping.
  - `futilityStopping`: Whether to allow futility stopping.
- `settings`: A list containing the following input parameters: `typeAlphaSpending`, `parameterAlphaSpending`, `userAlphaSpending`, `typeBetaSpending`, `parameterBetaSpending`, `allocationRatioPlanned`, `accrualTime`, `accrualIntensity`, `piecewiseSurvivalTime`, `stratumFraction`, `lambda1`, `lambda2`, `gamma1`, `gamma2`, and `spendingTime`.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.
```

```
rmpower(kMax = 2, informationRates = c(0.8, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        milestone = 18,
        allocationRatioPlanned = 1, accrualTime = seq(0, 8),
        accrualIntensity = 100/9*seq(1, 9),
        piecewiseSurvivalTime = c(0, 6),
        stratumFraction = c(0.2, 0.8),
        lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
        lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
        gamma1 = -log(1-0.05)/12,
        gamma2 = -log(1-0.05)/12, accrualDuration = 22,
        followupTime = 18, fixedFollowup = FALSE)
```



rmpower1s

*Power for one-sample restricted mean survival time***Description**

Estimates the power, stopping probabilities, and expected sample size in a one-group survival design.

**Usage**

```
rmpower1s(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  milestone = NA_real_,
  rmstH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

**Arguments**

**kMax**                    The maximum number of stages.

**informationRates**        The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**efficacyStopping**        Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping	Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level. Defaults to 0.025.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
milestone	The milestone time at which to calculate the restricted mean survival time.
rmstH0	The restricted mean survival time under the null hypothesis.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda	A vector of hazard rates for the event in each analysis time interval by stratum under the alternative hypothesis.
gamma	The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout. Defaults to 0 for no dropout.

accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.

### Value

An S3 class rmpower1s object with 3 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - drift: The drift parameter, equal to  $(rmst - rmstH0) * \sqrt{\text{information}}$ .
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numbeOfSubjects: The total number of subjects.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - accrualDuration: The accrual duration.
  - followupTime: The follow-up duration.
  - fixedFollowup: Whether a fixed follow-up design is used.
  - kMax: The number of stages.
  - milestone: The milestone time relative to randomization.
  - rmstH0: The restricted mean survival time under the null hypothesis.
  - rmst: The restricted mean survival time under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfSubjects: The number of subjects.

- analysisTime: The average time since trial start.
  - efficacyRmst: The efficacy boundaries on the restricted mean survival time.
  - futilityRmst: The futility boundaries on the restricted mean survival time.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, accrualTime, accrualIntensity, piecewiseSurvivalTime, stratumFraction, lambda, gamma, and spendingTime.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### See Also

[rmstat](#)

### Examples

```
rmpower1s(kMax = 2, informationRates = c(0.8, 1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  milestone = 18, rmstH0 = 10,
  accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
  gamma = -log(1-0.05)/12, accrualDuration = 22,
  followupTime = 18, fixedFollowup = FALSE)
```

---

rmpowerequiv

*Power for equivalence in restricted mean survival time difference*

---

### Description

Obtains the power for equivalence in restricted mean survival time difference.

**Usage**

```

rmpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  milestone = NA_real_,
  rmstDiffLower = NA_real_,
  rmstDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)

```

**Arguments**

**kMax** The maximum number of stages.

**informationRates** The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha** The significance level for each of the two one-sided tests. Defaults to 0.05.

**typeAlphaSpending** The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending** The user defined alpha spending. Cumulative alpha spent up to each stage.

milestone	The milestone time at which to calculate the restricted mean survival time.
rmstDiffLower	The lower equivalence limit of restricted mean survival time difference.
rmstDiffUpper	The upper equivalence limit of restricted mean survival time difference.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
spendingTime	A vector of length $k\text{Max}$ for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of <code>accrualDuration</code> and <code>followupTime</code> . If provided, the value is allowed to be less than the sum of <code>accrualDuration</code> and <code>followupTime</code> .

### Value

An S3 class `rmpowerequiv` object with 3 components:

- `overallResults`: A data frame containing the following variables:
  - `overallReject`: The overall rejection probability.

- alpha: The overall significance level.
- attainedAlphaH10: The attained significance level under H10.
- attainedAlphaH20: The attained significance level under H20.
- numbeOfSubjects: The total number of subjects.
- studyDuration: The total study duration.
- information: The maximum information.
- expectedNumberOfSubjects: The expected number of subjects.
- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- kMax: The number of stages.
- milestone: The milestone time relative to randomization.
- rmstDiffLower: The lower equivalence limit of restricted mean survival time difference.
- rmstDiffUpper: The upper equivalence limit of restricted mean survival time difference.
- rmst1: The restricted mean survival time for the treatment group.
- rmst2: The restricted mean survival time for the control group.
- rmstDiff: The restricted mean survival time difference.
- accrualDuration: The accrual duration.
- followupTime: The follow-up duration.
- fixedFollowup: Whether a fixed follow-up design is used.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - efficacyRmstDiffLower: The efficacy boundaries on the restricted mean survival time difference scale for the one-sided null hypothesis at the lower equivalence limit.
  - efficacyRmstDiffUpper: The efficacy boundaries on the restricted mean survival time difference scale for the one-sided null hypothesis at the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accrualIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, and spendingTime.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**[rmstat](#)**Examples**

```

rmpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             milestone = 18,
             rmstDiffLower = -2, rmstDiffUpper = 2,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 100/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12, accrualDuration = 22,
             followupTime = 18, fixedFollowup = FALSE)

```

rmsamplesize

*Sample size for difference in restricted mean survival times***Description**

Obtains the needed accrual duration given power, accrual intensity, and follow-up time, the needed follow-up time given power, accrual intensity, and accrual duration, or the needed absolute accrual intensity given power, relative accrual intensity, accrual duration, and follow-up time in a two-group survival design.

**Usage**

```

rmsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,

```



```

milestone = NA_real_,
rmstDiffH0 = 0,
allocationRatioPlanned = 1,
accrualTime = 0L,
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
lambda1 = NA_real_,
lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
interval = as.numeric(c(0.001, 240)),
spendingTime = NA_real_,
rounding = 1L
)

```

## Arguments

**beta** Type II error. Defaults to 0.2.

**kMax** The maximum number of stages.

**informationRates** The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**efficacyStopping** Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

**futilityStopping** Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha** The significance level. Defaults to 0.025.

**typeAlphaSpending** The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending** The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds	Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to $\text{rep}(-6, \text{kMax}-1)$ if left unspecified. The futility bounds are non-binding for the calculation of critical values.
typeBetaSpending	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
parameterBetaSpending	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
userBetaSpending	The user defined beta spending. Cumulative beta spent up to each stage.
milestone	The milestone time at which to calculate the restricted mean survival time.
rmstDiffH0	The difference in restricted mean survival times under the null hypothesis. Defaults to 0 for superiority test.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.

fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
interval	The interval to search for the solution of accrualDuration, followupTime, or the proportionality constant of accrualIntensity. Defaults to $c(0.001, 240)$ .
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

**Value**

A list of two components:

- resultsUnderH1: An S3 class rmpower object under the alternative hypothesis.
- resultsUnderH0: An S3 class rmpower object under the null hypothesis.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[rmpower](#)

**Examples**

```
# Example 1: Obtains follow-up time given power, accrual intensity,
# and accrual duration for variable follow-up. Of note, the power
# reaches the maximum when the follow-up time equals milestone.
```

```
rmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
              alpha = 0.025, typeAlphaSpending = "sfOF",
              milestone = 18,
              allocationRatioPlanned = 1, accrualTime = seq(0, 8),
              accrualIntensity = 100/9*seq(1, 9),
              piecewiseSurvivalTime = c(0, 6),
              stratumFraction = c(0.2, 0.8),
              lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
              lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
              gamma1 = -log(1-0.05)/12,
              gamma2 = -log(1-0.05)/12, accrualDuration = 22,
              followupTime = NA, fixedFollowup = FALSE)
```

```
# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up time for variable follow-up
```

```
rmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
              alpha = 0.025, typeAlphaSpending = "sfOF",
              milestone = 18,
              allocationRatioPlanned = 1, accrualTime = seq(0, 8),
              accrualIntensity = 100/9*seq(1, 9),
              piecewiseSurvivalTime = c(0, 6),
              stratumFraction = c(0.2, 0.8),
```

```

lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
gamma1 = -log(1-0.05)/12,
gamma2 = -log(1-0.05)/12, accrualDuration = 22,
followupTime = 18, fixedFollowup = FALSE)

# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up time for fixed follow-up

rmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
alpha = 0.025, typeAlphaSpending = "sfOF",
milestone = 18,
allocationRatioPlanned = 1, accrualTime = seq(0, 8),
accrualIntensity = 100/9*seq(1, 9),
piecewiseSurvivalTime = c(0, 6),
stratumFraction = c(0.2, 0.8),
lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
gamma1 = -log(1-0.05)/12,
gamma2 = -log(1-0.05)/12, accrualDuration = NA,
followupTime = 18, fixedFollowup = TRUE)

```

---

rmsamplesize1s

*Sample size for one-sample restricted mean survival time*


---

### Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a one-group survival design.

### Usage

```

rmsamplesize1s(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,

```

```

userBetaSpending = NA_real_,
milestone = NA_real_,
rmstH0 = NA_real_,
accrualTime = 0L,
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
lambda = NA_real_,
gamma = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
interval = as.numeric(c(0.001, 240)),
spendingTime = NA_real_,
rounding = 1L
)

```

### Arguments

**beta** Type II error. Defaults to 0.2.

**kMax** The maximum number of stages.

**informationRates** The information rates. Defaults to  $(1:kMax) / kMax$  if left unspecified.

**efficacyStopping** Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

**futilityStopping** Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

**criticalValues** Upper boundaries on the z-test statistic scale for stopping for efficacy.

**alpha** The significance level. Defaults to 0.025.

**typeAlphaSpending** The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

**parameterAlphaSpending** The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

**userAlphaSpending** The user defined alpha spending. Cumulative alpha spent up to each stage.

**futilityBounds** Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to  $\text{rep}(-6, kMax-1)$  if left unspecified. The futility bounds are non-binding for the calculation of critical values.

<code>typeBetaSpending</code>	The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".
<code>parameterBetaSpending</code>	The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".
<code>userBetaSpending</code>	The user defined beta spending. Cumulative beta spent up to each stage.
<code>milestone</code>	The milestone time at which to calculate the restricted survival time.
<code>rmstH0</code>	The restricted mean survival time under the null hypothesis.
<code>accrualTime</code>	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, \text{Inf})$ .
<code>accrualIntensity</code>	A vector of accrual intensities. One for each accrual time interval.
<code>piecewiseSurvivalTime</code>	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
<code>stratumFraction</code>	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
<code>lambda</code>	A vector of hazard rates for the event in each analysis time interval by stratum under the alternative hypothesis.
<code>gamma</code>	The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout. Defaults to 0 for no dropout.
<code>accrualDuration</code>	Duration of the enrollment period.
<code>followupTime</code>	Follow-up time for the last enrolled subject.
<code>fixedFollowup</code>	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
<code>interval</code>	The interval to search for the solution of <code>accrualDuration</code> , <code>followupDuration</code> , or the proportionality constant of <code>accrualIntensity</code> . Defaults to $c(0.001, 240)$ .
<code>spendingTime</code>	A vector of length <code>kMax</code> for the error spending time at each analysis. Defaults to missing, in which case, it is the same as <code>informationRates</code> .
<code>rounding</code>	Whether to round up sample size. Defaults to 1 for sample size rounding.

## Value

A list of two components:

- `resultsUnderH1`: An S3 class `rmpower1s` object under the alternative hypothesis.
- `resultsUnderH0`: An S3 class `rmpower1s` object under the null hypothesis.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[rmpower1s](#)

**Examples**

```
# Example 1: Obtains follow-up duration given power, accrual intensity,  
# and accrual duration for variable follow-up
```

```
rmsamplesize1s(beta = 0.2, kMax = 2,  
  informationRates = c(0.8, 1),  
  alpha = 0.025, typeAlphaSpending = "sfOF",  
  milestone = 18, rmstH0 = 10,  
  accrualTime = seq(0, 8),  
  accrualIntensity = 26/9*seq(1, 9),  
  piecewiseSurvivalTime = c(0, 6),  
  stratumFraction = c(0.2, 0.8),  
  lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),  
  gamma = -log(1-0.05)/12, accrualDuration = 22,  
  followupTime = NA, fixedFollowup = FALSE)
```

```
# Example 2: Obtains accrual intensity given power, accrual duration, and  
# follow-up duration for variable follow-up
```

```
rmsamplesize1s(beta = 0.2, kMax = 2,  
  informationRates = c(0.8, 1),  
  alpha = 0.025, typeAlphaSpending = "sfOF",  
  milestone = 18, rmstH0 = 10,  
  accrualTime = seq(0, 8),  
  accrualIntensity = 26/9*seq(1, 9),  
  piecewiseSurvivalTime = c(0, 6),  
  stratumFraction = c(0.2, 0.8),  
  lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),  
  gamma = -log(1-0.05)/12, accrualDuration = 22,  
  followupTime = 18, fixedFollowup = FALSE)
```

```
# Example 3: Obtains accrual duration given power, accrual intensity, and  
# follow-up duration for fixed follow-up
```

```
rmsamplesize1s(beta = 0.2, kMax = 2,  
  informationRates = c(0.8, 1),  
  alpha = 0.025, typeAlphaSpending = "sfOF",  
  milestone = 18, rmstH0 = 10,  
  accrualTime = seq(0, 8),  
  accrualIntensity = 26/9*seq(1, 9),  
  piecewiseSurvivalTime = c(0, 6),  
  stratumFraction = c(0.2, 0.8),  
  lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
```

```
gamma = -log(1-0.05)/12, accrualDuration = NA,
followupTime = 18, fixedFollowup = TRUE)
```

---

rmsamplesizeequiv      *Sample size for equivalence in restricted mean survival time difference*

---

### Description

Obtains the sample size for equivalence in restricted mean survival time difference.

### Usage

```
rmsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  milestone = NA_real_,
  rmstDiffLower = NA_real_,
  rmstDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

### Arguments

beta	The type II error.
kMax	The maximum number of stages.



informationRates	The information rates. Defaults to $(1:kMax) / kMax$ if left unspecified.
criticalValues	Upper boundaries on the z-test statistic scale for stopping for efficacy.
alpha	The significance level for each of the two one-sided tests. Defaults to 0.05.
typeAlphaSpending	The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".
parameterAlphaSpending	The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".
userAlphaSpending	The user defined alpha spending. Cumulative alpha spent up to each stage.
milestone	The milestone time at which to calculate the restricted mean survival time.
rmstDiffLower	The lower equivalence limit of restricted mean survival time difference.
rmstDiffUpper	The upper equivalence limit of restricted mean survival time difference.
allocationRatioPlanned	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
accrualTime	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., $c(0, 3)$ breaks the time axis into 2 accrual intervals: $[0, 3)$ and $[3, Inf)$ .
accrualIntensity	A vector of accrual intensities. One for each accrual time interval.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, Inf)$ . Defaults to 0 for exponential distribution.
stratumFraction	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
interval	The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to $c(0.001, 240)$ .
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

**Value**

An S3 class `rmpowerequiv` object

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**See Also**

[rmpowerequiv](#)

**Examples**

```
rmsamplesizeequiv(beta = 0.1, kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF",
  milestone = 18,
  rmstDiffLower = -2, rmstDiffUpper = 2,
  allocationRatioPlanned = 1, accrualTime = seq(0, 8),
  accrualIntensity = 26/9*seq(1, 9),
  piecewiseSurvivalTime = c(0, 6),
  stratumFraction = c(0.2, 0.8),
  lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
  gamma1 = -log(1-0.05)/12,
  gamma2 = -log(1-0.05)/12, accrualDuration = NA,
  followupTime = 18, fixedFollowup = FALSE)
```

---

rmst

*Restricted mean survival time*

---

**Description**

Obtains the restricted mean survival time over an interval.

**Usage**

```
rmst(t1 = 0, t2 = NA_real_, piecewiseSurvivalTime = 0L, lambda = NA_real_)
```

**Arguments**

**t1** Lower bound of the analysis time interval.

**t2** Upper bound of the analysis time interval.

**piecewiseSurvivalTime** A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., `c(0, 6)` breaks the time axis into 2 event intervals: `[0, 6)` and `[6, Inf)`. Defaults to 0 for exponential distribution.

**lambda** A vector of hazard rates for the event. One for each analysis time interval.

**Value**

The integral of the survival function from `t1` to `t2`

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
rmst(t1 = 0, t2 = 7, piecewiseSurvivalTime = c(0, 6),
     lambda = c(0.0533, 0.0309))
```

---

 rmstat

*Stratified difference in restricted mean survival times*


---

**Description**

Obtains the stratified restricted mean survival times and difference in restricted mean survival times at given calendar times.

**Usage**

```
rmstat(
  time = NA_real_,
  milestone = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
```

```

lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L
)

```

## Arguments

<code>time</code>	A vector of calendar times at which to calculate the restricted mean survival time.
<code>milestone</code>	The milestone time at which to calculate the restricted mean survival time.
<code>allocationRatioPlanned</code>	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
<code>accrualTime</code>	A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., <code>c(0, 3)</code> breaks the time axis into 2 accrual intervals: <code>[0, 3)</code> and <code>[3, Inf)</code> .
<code>accrualIntensity</code>	A vector of accrual intensities. One for each accrual time interval.
<code>piecewiseSurvivalTime</code>	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., <code>c(0, 6)</code> breaks the time axis into 2 event intervals: <code>[0, 6)</code> and <code>[6, Inf)</code> . Defaults to 0 for exponential distribution.
<code>stratumFraction</code>	A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.
<code>lambda1</code>	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.
<code>lambda2</code>	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.
<code>gamma1</code>	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.
<code>gamma2</code>	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.
<code>accrualDuration</code>	Duration of the enrollment period.
<code>followupTime</code>	Follow-up time for the last enrolled subject.
<code>fixedFollowup</code>	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

**Value**

A data frame containing the following variables:

- `time`: The calendar time at which to calculate the restricted mean survival time.
- `subjects`: The number of enrolled subjects.
- `milestone`: The milestone time relative to randomization.
- `rmst1`: The restricted mean survival time for the treatment group.
- `rmst2`: The restricted mean survival time for the control group.
- `rmstDiff`: The difference in restricted mean survival times, i.e.,  $rmst1 - rmst2$ .
- `vrms1`: The variance for `rmst1`.
- `vrms2`: The variance for `rmst2`.
- `vrmsDiff`: The variance for `rmstDiff`.
- `information`: The information for `rmstDiff`, equal to  $1/vrmsDiff$ .
- `rmstDiffZ`: The Z-statistic value, i.e.,  $rmstDiff/\sqrt{vrmsDiff}$ .

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by  
# the end of 1 year.
```

```
rmstat(time = c(22, 40),  
       milestone = 18,  
       allocationRatioPlanned = 1,  
       accrualTime = seq(0, 8),  
       accrualIntensity = 26/9*seq(1, 9),  
       piecewiseSurvivalTime = c(0, 6),  
       stratumFraction = c(0.2, 0.8),  
       lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),  
       lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),  
       gamma1 = -log(1-0.05)/12,  
       gamma2 = -log(1-0.05)/12,  
       accrualDuration = 22,  
       followupTime = 18, fixedFollowup = FALSE)
```

---

rtpwexp	<i>Random number generation function of truncated piecewise exponential distribution</i>
---------	--

---

**Description**

Obtains random samples from a truncated piecewise exponential distribution.

**Usage**

```
rtpwexp(n, piecewiseSurvivalTime = 0, lambda = 0.0578, lowerBound = 0)
```

**Arguments**

n	The number of observations.
piecewiseSurvivalTime	A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., $c(0, 6)$ breaks the time axis into 2 event intervals: $[0, 6)$ and $[6, \text{Inf})$ . Defaults to 0 for exponential distribution.
lambda	A vector of hazard rates for the event. One for each analysis time interval.
lowerBound	The left truncation time point for the survival time. Defaults to 0 for no truncation.

**Value**

The random numbers from truncated piecewise exponential distribution.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
rtpwexp(n = 10, piecewiseSurvivalTime = c(0, 6, 9, 15),  
        lambda = c(0.025, 0.04, 0.015, 0.007))
```

---

`runShinyApp`*Run Shiny app*

---

**Description**

Runs the log-rank test power and sample size calculation Shiny app.

**Usage**

```
runShinyApp()
```

**Value**

No return value, called for side effects.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

---

`simon2stage`*Simon's two-stage design*

---

**Description**

Obtains Simon's two-stage minimax, admissible, and optimal designs.

**Usage**

```
simon2stage(  
  alpha = NA_real_,  
  beta = NA_real_,  
  piH0 = NA_real_,  
  pi = NA_real_,  
  n_max = 110L  
)
```

**Arguments**

<code>alpha</code>	Type I error rate (one-sided).
<code>beta</code>	Type II error rate (1-power).
<code>piH0</code>	Response probability under the null hypothesis.
<code>pi</code>	Response probability under the alternative hypothesis.
<code>n_max</code>	Upper limit for sample size, defaults to 110.

**Value**

A data frame containing the following variables:

- $\pi_{H0}$ : Response probability under the null hypothesis.
- $\pi_i$ : Response probability under the alternative hypothesis.
- $\alpha$ : The specified one-sided significance level.
- $\beta$ : The specified type II error.
- $n$ : Total sample size.
- $n_1$ : Stage 1 sample size.
- $r_1$ : Futility boundary for stage 1.
- $r$ : Futility boundary for stage 2.
- $EN_0$ : Expected sample size under the null hypothesis.
- $\text{attainedAlpha}$ : Attained type 1 error.
- $\text{power}$ : Attained power.
- $PET_0$ : Probability of early stopping under the null hypothesis.
- $w_{\text{lower}}$ : Lower bound of the interval for  $w$ .
- $w_{\text{upper}}$ : Upper bound of the interval for  $w$ .
- $\text{design}$ : Description of the design, e.g., minimax, admissible, or optimal.

Here  $w$  is the weight in the objective function:  $w*n + (1-w)*EN_0$ .

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
simon2stage(0.05, 0.15, 0.1, 0.3)
```

---

survQuantile

*Brookmeyer-Crowley confidence interval for quantiles of right-censored time-to-event data*

---

**Description**

Obtains the Brookmeyer-Crowley confidence interval for quantiles of right-censored time-to-event data.



**Usage**

```
survQuantile(  
  time = NA_real_,  
  event = NA_real_,  
  cilevel = 0.95,  
  transform = "loglog",  
  probs = c(0.25, 0.5, 0.75)  
)
```

**Arguments**

time	The vector of possibly right-censored survival times.
event	The vector of event indicators.
cilevel	The confidence interval level. Defaults to 0.95.
transform	The transformation of the survival function to use to construct the confidence interval. Options include "linear", "loglog", "log", "asinsqrt", and "logit". Defaults to "loglog".
probs	The vector of probabilities to calculate the quantiles. Defaults to c(0.25, 0.5, 0.75).

**Value**

A data frame containing the estimated quantile and confidence interval corresponding to each specified probability. It includes the following variables:

- prob: The probability to calculate the quantile.
- quantile: The estimated quantile.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.
- transform: The transformation of the survival function to use to construct the confidence interval.

**Author(s)**

Kaifeng Lu, <kaifengl@gmail.com>

**Examples**

```
survQuantile(  
  time = c(33.7, 3.9, 10.5, 5.4, 19.5, 23.8, 7.9, 16.9, 16.6,  
           33.7, 17.1, 7.9, 10.5, 38),  
  event = c(0, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 1, 1),  
  probs = c(0.25, 0.5, 0.75))
```

---

updateGraph	<i>Update graph for graphical approaches</i>
-------------	--

---

### Description

Updates the weights and transition matrix for graphical approaches.

### Usage

```
updateGraph(w = NA_real_, G = NA_real_, I = NA_integer_, j = NA_integer_)
```

### Arguments

w	The current vector of weights for elementary hypotheses.
G	The current transition matrix.
I	The set of indices for yet to be rejected hypotheses.
j	The hypothesis to remove from index set I.

### Value

A list containing the new vector of weights, the new transition matrix for the graph, and the new set of indices of yet to be rejected hypotheses.

### Author(s)

Kaifeng Lu, <kweifengl@gmail.com>

### Examples

```
updateGraph(w = c(0.5, 0.5, 0, 0),
            G = matrix(c(0, 0.5, 0.5, 0, 0.5, 0, 0, 0.5,
                        0, 1, 0, 0, 1, 0, 0, 0),
                      nrow=4, ncol=4, byrow=TRUE),
            I = c(1, 2, 3, 4),
            j = 1)
```

---

zstatOddsRatio	<i>Miettinen-Nurminen score test statistic for two-sample odds ratio</i>
----------------	--

---

**Description**

Obtains the Miettinen-Nurminen score test statistic for two-sample odds ratio possibly with stratification.

**Usage**

```
zstatOddsRatio(  
  oddsRatioH0 = 1,  
  n1 = NA_real_,  
  y1 = NA_real_,  
  n2 = NA_real_,  
  y2 = NA_real_  
)
```

**Arguments**

oddsRatioH0	The odds ratio under the null hypothesis. Defaults to 1.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

**Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

**Value**

The value of the score test statistic.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
zstatOddsRatio(oddsRatioH0 = 1, n1 = c(10,10), y1 = c(4,3),  
              n2 = c(20,10), y2 = c(2,0))
```

---

`zstatRateDiff`*Miettinen-Nurminen score test statistic for two-sample rate difference*

---

**Description**

Obtains the Miettinen-Nurminen score test statistic for two-sample rate difference possibly with stratification.

**Usage**

```
zstatRateDiff(  
  rateDiffH0 = 0,  
  t1 = NA_real_,  
  y1 = NA_real_,  
  t2 = NA_real_,  
  y2 = NA_real_  
)
```

**Arguments**

<code>rateDiffH0</code>	The rate difference under the null hypothesis. Defaults to 0.
<code>t1</code>	The exposure for the active treatment group.
<code>y1</code>	The number of events for the active treatment group.
<code>t2</code>	The exposure for the control group.
<code>y2</code>	The number of events for the control group.

**Details**

The Mantel-Haenszel weights are used for stratified samples.

**Value**

The value of the score test statistic.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
zstatRateDiff(rateDiffH0 = 0, t1 = c(10,10), y1 = c(4,3),  
              t2 = c(20,10), y2 = c(2,0))
```

---

zstatRateRatio	<i>Miettinen-Nurminen score test statistic for two-sample rate ratio</i>
----------------	--

---

### Description

Obtains the Miettinen-Nurminen score test statistic for two-sample rate ratio possibly with stratification.

### Usage

```
zstatRateRatio(  
  rateRatioH0 = 1,  
  t1 = NA_real_,  
  y1 = NA_real_,  
  t2 = NA_real_,  
  y2 = NA_real_  
)
```

### Arguments

rateRatioH0	The rate ratio under the null hypothesis. Defaults to 1.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

### Details

The Mantel-Haenszel weights are used for stratified samples.

### Value

The value of the score test statistic.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### Examples

```
zstatRateRatio(rateRatioH0 = 1, t1 = c(10,10), y1 = c(4,3),  
               t2 = c(20,10), y2 = c(2,0))
```

---

`zstatRiskDiff`*Miettinen-Nurminen score test statistic for two-sample risk difference*

---

**Description**

Obtains the Miettinen-Nurminen score test statistic for two-sample risk difference possibly with stratification.

**Usage**

```
zstatRiskDiff(  
  riskDiffH0 = 0,  
  n1 = NA_real_,  
  y1 = NA_real_,  
  n2 = NA_real_,  
  y2 = NA_real_  
)
```

**Arguments**

<code>riskDiffH0</code>	The risk difference under the null hypothesis. Defaults to 0.
<code>n1</code>	The sample size for the active treatment group.
<code>y1</code>	The number of responses for the active treatment group.
<code>n2</code>	The sample size for the control group.
<code>y2</code>	The number of responses for the control group.

**Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

**Value**

The value of the score test statistic.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
zstatRiskDiff(riskDiffH0 = 0, n1 = c(10,10), y1 = c(4,3),  
              n2 = c(20,10), y2 = c(2,0))
```

---

zstatRiskRatio	<i>Miettinen-Nurminen score test statistic for two-sample risk ratio</i>
----------------	--

---

**Description**

Obtains the Miettinen-Nurminen score test statistic for two-sample risk ratio possibly with stratification.

**Usage**

```
zstatRiskRatio(  
  riskRatioH0 = 1,  
  n1 = NA_real_,  
  y1 = NA_real_,  
  n2 = NA_real_,  
  y2 = NA_real_  
)
```

**Arguments**

riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

**Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

**Value**

The value of the score test statistic.

**Author(s)**

Kaifeng Lu, <kaifenglu@gmail.com>

**Examples**

```
zstatRiskRatio(riskRatioH0 = 1, n1 = c(10,10), y1 = c(4,3),  
              n2 = c(20,10), y2 = c(2,0))
```

# Index

- \* **datasets**
  - rawdata, 295
- accrual, 5
- adaptDesign, 6, 32, 35
- BOINTable, 10
- caltime, 12
- ClopperPearsonCI, 13
- covrmst, 14
- errorSpent, 16
- exitprob, 17
- fadjpbon, 18
- fadjpdun, 19
- fadjpsim, 20
- fmodmix, 21
- fquantile, 22
- fseqbon, 23
- fstdmix, 25
- fstp2seq, 26
- ftrunc, 27
- fwgmat, 28
- getAccrualDurationFromN, 29
- getADCI, 30
- getADRCI, 33
- getBound, 37
- getCI, 38
- getCP, 40
- getDesign, 9, 43, 44
- getDesignAgreement, 48
- getDesignANOVA, 50
- getDesignANOVAContrast, 52
- getDesignEquiv, 53
- getDesignFisherExact, 58
- getDesignLogistic, 60
- getDesignMeanDiff, 63
- getDesignMeanDiffCarryover, 66
- getDesignMeanDiffEquiv, 70
- getDesignMeanDiffMMRM, 73
- getDesignMeanDiffXO, 78
- getDesignMeanDiffXOEquiv, 81
- getDesignMeanRatio, 84
- getDesignMeanRatioEquiv, 88
- getDesignMeanRatioXO, 91
- getDesignMeanRatioXOEquiv, 94
- getDesignOddsRatio, 97
- getDesignOddsRatioEquiv, 101
- getDesignOneMean, 104
- getDesignOneMultinom, 107
- getDesignOneProportion, 109
- getDesignOneRateExact, 112
- getDesignOneSlope, 114
- getDesignOrderedBinom, 117
- getDesignPairedMeanDiff, 119
- getDesignPairedMeanDiffEquiv, 122
- getDesignPairedMeanRatio, 125
- getDesignPairedMeanRatioEquiv, 129
- getDesignPairedPropMcNemar, 131
- getDesignRepeatedANOVA, 135
- getDesignRepeatedANOVAContrast, 137
- getDesignRiskDiff, 138
- getDesignRiskDiffEquiv, 142
- getDesignRiskDiffExact, 145
- getDesignRiskDiffExactEquiv, 146
- getDesignRiskRatio, 148
- getDesignRiskRatioEquiv, 151
- getDesignRiskRatioExact, 154
- getDesignRiskRatioExactEquiv, 156
- getDesignRiskRatioFM, 157
- getDesignSlopeDiff, 161
- getDesignSlopeDiffMMRM, 165
- getDesignTwoMultinom, 170
- getDesignTwoOrdinal, 172
- getDesignTwoWayANOVA, 173
- getDesignUnorderedBinom, 175
- getDesignUnorderedMultinom, 176



getDesignWilcoxon, 177  
getDurationFromNevents, 181  
getNeventsFromHazardRatio, 183  
getRCI, 185

hedgesg, 187

kmdiff, 189  
kmest, 191  
kmpower, 192, 206  
kmpower1s, 196, 210  
kmpowerequiv, 200, 213  
kmsamplesize, 204  
kmsamplesize1s, 208  
kmsamplesizeequiv, 211  
kmstat, 199, 203, 214

lpower, 216, 228  
lpowerequiv, 221, 232  
lrsamplesize, 225  
lrsamplesizeequiv, 229  
lrsim, 232  
lrsim2e, 237  
lrsim2e3a, 241  
lrsim3a, 246  
lrstat, 250  
lrtest, 253

mnOddsRatioCI, 254  
mnRateDiffCI, 256  
mnRateRatioCI, 257  
mnRiskDiffCI, 258  
mnRiskRatioCI, 259  
mTPI2Table, 261

nbpower, 262, 279  
nbpower1s, 267, 282  
nbpowerequiv, 271, 285  
nbsamplesize, 276  
nbsamplesize1s, 280  
nbsamplesizeequiv, 283  
nbstat, 266, 270, 275, 286

ptpexp, 291  
pwexpcuts, 292  
pwexploglik, 293

qtpwexp, 294

rawdata, 295

remlOddsRatio, 295  
remlRateDiff, 296  
remlRateRatio, 297  
remlRiskDiff, 298  
remlRiskRatio, 299  
repeatedPValue, 300  
riskDiffExactCI, 301  
riskDiffExactPValue, 302  
riskRatioExactCI, 303  
riskRatioExactPValue, 304  
rmdiff, 305  
rmest, 307  
rmpower, 308, 323  
rmpower1s, 313, 327  
rmpowerequiv, 316, 330  
rmsamplesize, 320  
rmsamplesize1s, 324  
rmsamplesizeequiv, 328  
rmst, 330  
rmstat, 225, 316, 320, 331  
rtpwexp, 334  
runShinyApp, 335

simon2stage, 335  
survQuantile, 336

updateGraph, 338

zstatOddsRatio, 339  
zstatRateDiff, 340  
zstatRateRatio, 341  
zstatRiskDiff, 342  
zstatRiskRatio, 343