Package 'causalweight'

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Title Estimation Methods for Causal Inference Based on Inverse
Probability Weighting

Version 1.1.0

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Description Various estimators of causal effects based on inverse probability weighting, doubly robust estimation, and double machine learning. Specifically, the package includes methods for estimating average treatment effects, direct and indirect effects in causal mediation analysis, and dynamic treatment effects. The models refer to studies of Froelich (2007) <doi:10.1016/j.jeconom.2006.06.004>, Huber (2012) <doi:10.3102/1076998611411917>, Huber (2014) <doi:10.1080/07474938.2013.806197>, Huber (2014) <doi:10.1002/jae.2341>, Froelich and Huber (2017) <doi:10.1111/rssb.12232>, Hsu, Huber, Lee, and Lettry (2020) <doi:10.1002/jae.2765>, and others.

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Imports mvtnorm, np, LARF, hdm, SuperLearner, glmnet, xgboost, e1071, fastDummies, grf, checkmate

NeedsCompilation no

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R topics documented:

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attrlateweight   *Local average treatment effect estimation in multiple follow-up peri-*
                          ods with outcome attrition based on inverse probability weighting

---

Description

Instrumental variable-based evaluation of local average treatment effects using weighting by the
inverse of the instrument propensity score.

Usage

```
attrlateweight(
  y1,
  y2,
  s1,
  s2,
  d,
  z,
  x0,
  x1,
  weightmax = 0.1,
  boot = 1999,
```

```
    cluster = NULL
)
```

Arguments

y1	Outcome variable in the first outcome period.
y2	Outcome variable in the second outcome period.
s1	Selection indicator for first outcome period. Must be one if y1 is observed (non-missing) and zero if y1 is not observed (missing).
s2	Selection indicator for second outcome period. Must be one if y1 is observed (non-missing) and zero if y1 is not observed (missing).
d	Treatment, must be binary (either 1 or 0), must not contain missings.
z	Instrument for the endogenous treatment, must be binary (either 1 or 0), must not contain missings.
x0	Baseline (pre-instrument) confounders of the instrument and outcome, must not contain missings.
x1	Confounders in outcome period 1 (may include outcomes of period 1 y1)
weightmax	Trimming rule based on the maximum relative weight a single observation may obtain in estimation - observations with higher weights are discarded. Default is 0.1 (no observation can be assigned more than 10 percent of weights)
boot	Number of bootstrap replications for estimating standard errors. Default is 1999.
cluster	A cluster ID for block or cluster bootstrapping when units are clustered rather than iid. Must be numerical. Default is NULL (standard bootstrap without clustering).

Details

Estimation of local average treatment effects of a binary endogenous treatment on outcomes in two follow up periods that are prone to attrition. Treatment endogeneity is tackled by a binary instrument that is assumed to be conditionally valid given observed baseline confounders x0. Outcome attrition is tackled by either assuming that it is missing at random (MAR), i.e. selection w.r.t. observed variables d, z, x0, x1 (in the case of y2), and s1 (in the case of y2); or by assuming latent ignorability (LI), i.e. selection w.r.t. the treatment compliance type as well as z, x0, x1 (in the case of y2), and s1 (in the case of y2). Units are weighted by the inverse of their conditional instrument and selection propensities, which are estimated by probit regression. Standard errors are obtained by bootstrapping the effect.

Value

An attrlateweight object contains one component results:

results: a 4X4 matrix containing the effect estimates in the first row ("effects"), standard errors in the second row ("se"), p-values in the third row ("p-value"), and the number of trimmed observations due to too large weights in the fourth row ("trimmed obs"). The first column provides the local average treatment effect (LATE) on y1 among compliers under missingness at random (MAR). The second column provides the local average treatment effect (LATE) on y2 under missingness at random (MAR). The third column provides the local average treatment effect (LATE) on y1 under

latent ignorability (LI). The forth column provides the local average treatment effect (LATE) on y2 under latent ignorability (LI).

References

Frölich, M., Huber, M. (2014): "Treatment Evaluation With Multiple Outcome Periods Under Endogeneity and Attrition", Journal of the American Statistical Association, 109, 1697-1711.

Examples

```
# A little example with simulated data (4000 observations)
## Not run:
n=4000
e=(rmvnorm(n,rep(0,3), matrix(c(1,0.3,0.3,  0.3,1,0.3,  0.3,0.3,1),3,3) ))
x0=runif(n,0,1)
z=(0.25*x0+rnorm(n)>0)*1
d=(1.2*z-0.25*x0+e[,1]>0.5)*1
y1_star=0.5*x0+0.5*d+e[,2]
s1=(0.25*x0+0.25*d+rnorm(n)>-0.5)*1
y1=s1*y1_star
x1=(0.5*x0+0.5*rnorm(n))
y2_star=0.5*x0+x1+d+e[,3]
s2=s1*((0.25*x0+0.25*x1+0.25*d+rnorm(n)>-0.5)*1)
y2=s2*y2_star
# The true LATEs on y1 and y2 are equal to 0.5 and 1, respectively.
output=attrlateweight(y1=y1,y2=y2,s1=s1,s2=s2,d=d,z=z,x0=x0,x1=x1,boot=19)
round(output$results,3)
## End(Not run)
```

---

coffeeleaflet   *Information leaflet on coffee production and environmental awareness*
                                 of high school / university students in Bulgaria

---

Description

A dataset on the impact of an information leaflet about coffee production on students' awareness about environmental issues collected at Bulgarian highschools and universities in the year 2015.

Usage

```
coffeeleaflet
```

Format

A data frame with 522 rows and 48 variables:

grade school grade

sex 1=male, 0=female

age age in years

mob month of birth

bulgnationality dummy for Bulgarian nationality

langbulg dummy for Bulgarian mother tongue

mumage mother's age in years

mumedu mother's education (1=lower secondary or less, 2=upper secondary, 3=higher)

mumprof mother's profession (1=manager, 2=specialist, 3=worker, 4=self-employed,5=not working,6=retired,7=other)

dadage father's age in years

dadedu father's education (1=lower secondary or less, 2=upper secondary, 3=higher)

dadprof father's profession (1=manager, 2=specialist, 3=worker, 4=self-employed,5=not working,6=retired,7=other)

material material situation of the family (1=very bad,...,5=very good)

withbothpar dummy for living with both parents

withmum dummy for living with mother only

withdad dummy for living with father only

withneither dummy for living with neither mother nor father

oldsiblings number of older siblings

youngsiblings numer of younger siblings

schoolmaths school dummy (for highschool with maths specialization)

schoolrakdelsve school dummy

schoolvazov school dummy

schoolfinance school dummy

schoolvarna school dummy (for highschool in city of Varna)

schoolspanish school dummy (for Spanish highschool)

schooltechuni school dummy (for technical university)

schoolvidin school dummy (for highschool in city of Vidin)

schooluni school dummy (for university)

citysofia dummy for the capital city of Sofia

cityvarna dummy for the city of Varna

cityvidin dummy for the city of Vidin

treatment treatment (1=leaflet on environmental impact of coffee growing, 0=control group)

drinkcoffee drinks coffee (1=never, 2=not more than 1 time per week,3=several times per week, 4=1 time per day, 5=several times per day)

cupsest outcome: guess how many cups of coffee per capita are consumed in Bulgaria per year

devi_cupsest outcome: deviation of guess from true coffee consumption per capita and year in Bulgaria

impworldecon outcome: assess the importance of coffee for world economy (1=not at all important,..., 5=very important)

impincome assess the importance of coffee as a source of income for people in Africa and Latin America (1=not at all important,..., 5=very important)

awarewaste outcome: awareness of waste production due to coffee production (1=not aware,..., 5=fully aware)

awarepesticide outcome: awareness of pesticide use due to coffee production (1=not aware,..., 5=fully aware)

awaredeforestation outcome: awareness of deforestation due to coffee production (1=not aware,..., 5=fully aware)

awarewastewater outcome: awareness of waste water due to coffee production (1=not aware,..., 5=fully aware)

awarebiodiversityloss outcome: awareness of biodiversity loss due to coffee production (1=not aware,..., 5=fully aware)

awareunfairworking outcome: awareness of unfair working conditions due to coffee production (1=not aware,..., 5=fully aware)

reusepurposeful outcome: can coffee waste be reused purposefully (1=no, 2=maybe, 3=yes)

reusesoil outcome: can coffee waste be reused as soil (1=no, 2=maybe, 3=yes)

choiceprice importance of price when buying coffee (1=not important at all,..., 5=very important, 6=I don't drink coffee)

choicetastepleasure importance of pleasure or taste when buying coffee (1=not important at all,..., 5=very important, 6=I don't drink coffee)

choiceenvironsocial importance of environmental or social impact when buying coffee (1=not important at all,..., 5=very important, 6=I don't drink coffee)

References

Faldzhiyskiy, S. (Ecosystem Europe, Bulgaria) and Huber, M. (University of Fribourg): "The impact of an information leaflet about coffee production on students' awareness about environmental issues".

Examples

```
## Not run:
data(coffeeleaflet)
attach(coffeeleaflet)
data=na.omit(cbind(awarewaste,treatment,grade,sex,age))
# effect of information leaflet (treatment) on awareness of waste production
treatweight(y=data[,1],d=data[,2],x=data[,3:5],boot=199)
## End(Not run)
```

---

coupon	*Data on daily spending and coupon receipt (selective subsample) This data set is a selective subsample of the data set "couponsretailer" which was constructed for illustrative purposes.*

Description

Data on daily spending and coupon receipt (selective subsample) This data set is a selective subsample of the data set "couponsretailer" which was constructed for illustrative purposes.

Usage

```
coupon
```

Format

A data frame with 1293 rows and 9 variables:

dailyspending outcome: customer's daily spending at the retailer in a specific period

coupons treatment: 1 = customer received at least one coupon in that period; 0 = customer did not receive any coupon

coupons_preperiod coupon reception in previous period: 1 = customer received at least one coupon; 0 = customer did not receive any coupon

dailyspending_preperiod daily spending at the retailer in previous period

income_bracket income group: 1 = lowest to 12 = highest

age_range age of customer: 1 = 18-25; 2 = 26-35; 3 = 36-45; 4 = 46-55; 5 = 56-70; 6 = 71 plus

married marital status: 1 = married; 0 = unmarried

rented dwelling type: 1 = rented; 0 = owned

family_size number of family members: 1 = 1; 2 = 2; 3 = 3; 4 = 4; 5 = 5 plus

---

couponsretailer	*Data on daily spending and coupon receipt A dataset containing information on the purchasing behavior of 1582 retail store customers across 32 coupon campaigns.*

Description

Data on daily spending and coupon receipt A dataset containing information on the purchasing behavior of 1582 retail store customers across 32 coupon campaigns.

Usage

```
couponsretailer
```

Format

A data frame with 50,624 rows and 27 variables:

customer_id customer identifier

period period of observation: 1 = 1st period to 32 = last period

age_range age of customer: 1 = 18-25; 2 = 26-35; 3 = 36-45; 4 = 46-55; 5 = 56-70; 6 = 71 plus

married marital status: 1 = married; 0 = unmarried

rented dwelling type: 1 = rented; 0 = owned

family_size number of family members: 1 = 1; 2 = 2; 3 = 3; 4 = 4; 5 = 5 plus

income_bracket income group: 1 = lowest to 12 = highest

dailyspending_preperiod customer's daily spending at the retailer in previous period

purchase_ReadyEatFood_preperiod purchases of ready-to-eat food in previous period: 1 = yes, 0 = no

purchase_MeatSeafood_preperiod purchases of meat and seafood products in previous period: 1 = yes, 0 = no

purchase_OtherFood_preperiod purchases of other food products in previous period: 1 = yes, 0 = no

purchase_Drugstore_preperiod purchases of drugstore products in previous period: 1 = yes, 0 = no

purchase_OtherNonfood_preperiod purchases of other non-food products in previous period: 1 = yes, 0 = no

coupons_Any_preperiod coupon reception in previous period: 1 = customer received at least one coupon; 0 = customer did not receive any coupon

coupons_ReadyEatFood_preperiod coupon reception in previous period: 1 = customer received at least one ready-to-eat food coupon; 0 = customer did not receive any ready-to-eat food coupon

coupons_MeatSeafood_preperiod coupon reception in previous period: 1 = customer received at least one meat/seafood coupon; 0 = customer did not receive any meat/seafood coupon

coupons_OtherFood_preperiod coupon reception in previous period: 1 = customer received at least one coupon applicable to other food items; 0 = customer did not receive any coupon applicable to other food items

coupons_Drugstore_preperiod coupon reception in previous period: 1 = customer received at least one drugstore coupon; 0 = customer did not receive any drugstore coupon

coupons_OtherNonfood_preperiod coupon reception in previous period: 1 = customer received at least one coupon applicable to other non-food items; 0 = customer did not receive any coupon applicable to other non-food items

coupons_Any_redeemed_preperiod coupon redemption in previous period: 1 = customer redeemed at least one coupon; 0 = customer did not redeem any coupon

coupons_Any treatment: 1 = customer received at least one coupon in current period; 0 = customer did not receive any coupon

coupons_ReadyEatFood treatment: 1 = customer received at least one ready-to-eat food coupon; 0 = customer did not receive any ready-to-eat food coupon

coupons_MeatSeafood treatment: 1 = customer received at least one meat/seafood coupon; 0 = customer did not receive any meat/seafood coupon

coupons_OtherFood treatment: 1 = customer received at least one coupon applicable to other food items; 0 = customer did not receive any coupon applicable to other food items

coupons_Drugstore treatment: 1 = customer received at least one drugstore coupon; 0 = customer did not receive any drugstore coupon

coupons_OtherNonfood treatment: 1 = customer received at least one coupon applicable to other non-food items; 0 = customer did not receive any coupon applicable to other non-food items

dailyspending outcome: customer's daily spending at the retailer in current period

References

Langen, Henrika, and Huber, Martin (2023): "How causal machine learning can leverage marketing strategies: Assessing and improving the performance of a coupon campaign." PLoS ONE, 18 (1): e0278937.

---

didweight | *Difference-in-differences based on inverse probability weighting*

Description

Difference-in-differences-based estimation of the average treatment effect on the treated in the post-treatment period, given a binary treatment with one pre- and one post-treatment period. Permits controlling for differences in observed covariates across treatment groups and/or time periods based on inverse probability weighting.

Usage

```
didweight(y, d, t, x = NULL, boot = 1999, trim = 0.05, cluster = NULL)
```

Arguments

y	Dependent variable, must not contain missings.
d	Treatment, must be binary (either 1 or 0), must not contain missings.
t	Time period, must be binary, 0 for pre-treatment and 1 for post-treatment, must not contain missings.
x	Covariates to be controlled for by inverse probability weighting. Default is NULL.
boot	Number of bootstrap replications for estimating standard errors. Default is 1999.
trim	Trimming rule for discarding observations with extreme propensity scores in the 3 reweighting steps, which reweight (1) treated in the pre-treatment period, (2) non-treated in the post-treatment period, and (3) non-treated in the pre-treatment period according to the covariate distribution of the treated in the post-treatment period. Default is 0.05, implying that observations with a probability lower than 5 percent of not being treated in some weighting step are discarded.
cluster	A cluster ID for block or cluster bootstrapping when units are clustered rather than iid. Must be numerical. Default is NULL (standard bootstrap without clustering).

Details

Estimation of the average treatment effect on the treated in the post-treatment period based Difference-in-differences. Inverse probability weighting is used to control for differences in covariates across treatment groups and/or over time. That is, (1) treated observations in the pre-treatment period, (2) non-treated observations in the post-treatment period, and (3) non-treated observations in the pre-treatment period are reweighted according to the covariate distribution of the treated observations in the post-treatment period. The respective propensity scores are obtained by probit regressions.

Value

A didweight object contains 4 components, eff, se, pvalue, and ntrimmed.

eff: estimate of the average treatment effect on the treated in the post-treatment period.

se: standard error obtained by bootstrapping the effect.

pvalue: p-value based on the t-statistic.

ntrimmed: total number of discarded (trimmed) observations in any of the 3 reweighting steps due to extreme propensity score values.

References

Abadie, A. (2005): "Semiparametric Difference-in-Differences Estimators", The Review of Economic Studies, 72, 1-19.

Lechner, M. (2011): "The Estimation of Causal Effects by Difference-in-Difference Methods", Foundations and Trends in Econometrics, 4, 165-224.

Examples

```
# A little example with simulated data (4000 observations)
## Not run:
n=4000                        # sample size
t=1*(rnorm(n)>0)              # time period
u=rnorm(n)                    # time constant unobservable
x=0.5*t+rnorm(n)              # time varying covariate
d=1*(x+u+rnorm(n)>0)          # treatment
y=d*t+d+t+x+u                 # outcome
# The true effect equals 1
didweight(y=y,d=d,t=t,x=x, boot=199)
## End(Not run)
```

---

dyntreatDML   *Dynamic treatment effect evaluation with double machine learning*

Description

Dynamic treatment effect estimation for assessing the average effects of sequences of treatments (consisting of two sequential treatments). Combines estimation based on (doubly robust) efficient score functions with double machine learning to control for confounders in a data-driven way.

Usage

```
dyntreatDML(
  y2,
  d1,
  d2,
  x0,
  x1,
  s = NULL,
  d1treat = 1,
  d2treat = 1,
  d1control = 0,
  d2control = 0,
  trim = 0.01,
  MLmethod = "lasso",
  fewsplits = FALSE,
  normalized = TRUE
)
```

Arguments

y2	Dependent variable in the second period (=outcome period), must not contain missings.
d1	Treatment in the first period, must be discrete, must not contain missings.
d2	Treatment in the second period, must be discrete, must not contain missings.
x0	Covariates in the baseline period (prior to the treatment in the first period), must not contain missings.
x1	Covariates in the first period (prior to the treatment in the second period), must not contain missings.
s	Indicator function for defining a subpopulation for whom the treatment effect is estimated as a function of the subpopulation's distribution of x0. Default is NULL (estimation of the treatment effect in the total population).
d1treat	Value of the first treatment in the treatment sequence. Default is 1.
d2treat	Value of the second treatment in the treatment sequence. Default is 1.
d1control	Value of the first treatment in the control sequence. Default is 0.
d2control	Value of the second treatment in the control sequence. Default is 0.
trim	Trimming rule for discarding observations with products of treatment propensity scores in the first and second period that are smaller than trim (to avoid too small denominators in weighting by the inverse of the propensity scores). Default is 0.01.
MLmethod	Machine learning method for estimating the nuisance parameters based on the SuperLearner package. Must be either "lasso" (default) for lasso estimation, "randomforest" for random forests, "xgboost" for xg boosting, "svm" for support vector machines, "ensemble" for using an ensemble algorithm based on all previously mentioned machine learners, or "parametric" for linear or logit regression.

fewsplits   If set to TRUE, the same training data are used for estimating a nested model of
                 conditional mean outcomes, namely `E[E[y2|d1,d2,x0,x1]|d1,x0]`. If `fewsplits`
                 is FALSE, the training data are split for the sequential estimation of the nested
                 model. Default of `fewsplits` is FALSE.

normalized   If set to TRUE, then the inverse probability-based weights are normalized such
                 that they add up to 1 within treatment groups. Default is TRUE.

Details

Estimation of the causal effects of sequences of two treatments under sequential conditional inde-
pendence, assuming that all confounders of the treatment in either period and the outcome of interest
are observed. Estimation is based on the (doubly robust) efficient score functions for potential out-
comes, see e.g. Bodory, Huber, and Laffers (2020), in combination with double machine learning
with cross-fitting, see Chernozhukov et al (2018). To this end, one part of the data is used for
estimating the model parameters of the treatment and outcome equations based machine learning.
The other part of the data is used for predicting the efficient score functions. The roles of the data
parts are swapped (using 3-fold cross-fitting) and the average dynamic treatment effect is estimated
based on averaging the predicted efficient score functions in the total sample. Standard errors are
based on asymptotic approximations using the estimated variance of the (estimated) efficient score
functions.

Value

A dyntreatDML object contains ten components, effect, se, pval, ntrimmed, meantreat, meancontrol,
psd1treat, psd2treat, psd1control, and psd2control :

effect: estimate of the average effect of the treatment sequence.

se: standard error of the effect estimate.

pval: p-value of the effect estimate.

ntrimmed: number of discarded (trimmed) observations due to low products of propensity scores.

meantreat: Estimate of the mean potential outcome under the treatment sequence.

meancontrol: Estimate of the mean potential outcome under the control sequence.

psd1treat: P-score estimates for first treatment in treatment sequence.

psd2treat: P-score estimates for second treatment in treatment sequence.

psd1control: P-score estimates for first treatment in control sequence.

psd2control: P-score estimates for second treatment in control sequence.

References

Bodory, H., Huber, M., Laffers, L. (2020): "Evaluating (weighted) dynamic treatment effects by
double machine learning", working paper, arXiv preprint arXiv:2012.00370.

Chernozhukov, V., Chetverikov, D., Demirer, M., Duflo, E., Hansen, C., Newey, W., Robins, J.
(2018): "Double/debiased machine learning for treatment and structural parameters", The Econo-
metrics Journal, 21, C1-C68.

van der Laan, M., Polley, E., Hubbard, A. (2007): "Super Learner", Statistical Applications in
Genetics and Molecular Biology, 6.

Examples

```
# A little example with simulated data (2000 observations)
## Not run:
n=2000
# sample size
p0=10
# number of covariates at baseline
s0=5
# number of covariates that are confounders at baseline
p1=10
# number of additional covariates in period 1
s1=5
# number of additional covariates that are confounders in period 1
x0=matrix(rnorm(n*p0),ncol=p0)
# covariate matrix at baseline
beta0=c(rep(0.25,s0), rep(0,p0-s0))
# coefficients determining degree of confounding for baseline covariates
d1=(x0%*%beta0+rnorm(n)>0)*1
# equation of first treatment in period 1
x1=matrix(rnorm(n*p1),ncol=p1)+matrix(0.1 * d1, nrow = n, ncol = p1)
# covariate matrix for covariates of period 1 (affected by 1st treatment d1)
beta1=c(rep(0.25,s1), rep(0,p1-s1))
# coefficients determining degree of confounding for covariates of period 1
d2=(x0%*%beta0+x1%*%beta1+0.5*d1+rnorm(n)>0)*1
# equation of second treatment in period 2
y2=x0%*%beta0+x1%*%beta1+1*d1+0.5*d2+rnorm(n)
# outcome equation in period 2
output=dyntreatDML(y2=y2,d1=d1,d2=d2,x0=x0,x1=x1,
        d1treat=1,d2treat=1,d1control=0,d2control=0)
cat("dynamic ATE: ",round(c(output$effect),3),", standard error: ",
    round(c(output$se),3), ", p-value: ",round(c(output$pval),3))
output$ntrimmed
# The true effect of the treatment sequence is 1.5
## End(Not run)
```

---

games   *Sales of video games*

Description

A dataset containing information on 3956 video games, including sales as well as expert and user ratings.

Usage

```
games
```

Format

A data frame with 3956 rows and 9 variables:

name factor variable providing the name of the video game

genre factor variable indicating the genre of the game (e.g. Action, Sports...)

platform factor variable indicating the hardware platform of the game (e.g. PC,...)

esrbrating factor variable indicating the age recommendation for the game(E is age 6+, T is 13+, M is 17+)

publisher factor variable indicating the publisher of the game

year numeric variable indicating the year the video game was released

metascore numeric variable providing a weighted average rating of the game by professional critics

userscore numeric variable providing the average user rating of the game

sales numeric variable indicating the total global sales (in millions) of the game up to the year 2018

References

Wittwer, J. (2020): "Der Erfolg von Videospielen - eine empirische Untersuchung moeglicher Erfolgsfaktoren", BA thesis, University of Fribourg.

Examples

```
## Not run:
#load data
data(games)
#select non-missing observations
games_nomis=na.omit(games)
#turn year into a factor variable
games_nomis$year=factor(games_nomis$year)
#attach data
attach(games_nomis)
#load library for generating dummies
library(fastDummies)
#generate dummies for genre
dummies=dummy_cols(genre, remove_most_frequent_dummy = TRUE)
#drop original variable
genredummies=dummies[,2:ncol(dummies)]
#make dummies numeric
genredummies=apply(genredummies, 2, function(genredummies) as.numeric(genredummies))
#generate dummies for year
dummies=dummy_cols(year, remove_most_frequent_dummy = TRUE)
#drop original variable
yeardummies=dummies[,2:ncol(dummies)]
#make dummies numeric
yeardummies=apply(yeardummies, 2, function(yeardummies) as.numeric(yeardummies))
# mediation analysis with metascore as treatment, userscore as mediator, sales as outcome
x=cbind(genredummies,yeardummies)
output=medweightcont(y=sales,d=metascore, d0=60, d1=80, m=userscore, x=x, boot=199)
round(output$results,3)
output$ntrimmed
## End(Not run)
```

---

identificationDML   *Testing identification with double machine learning*

Description

Testing identification with double machine learning

Usage

```
identificationDML(
  y,
  d,
  x,
  z,
  score = "DR",
  bootstrap = FALSE,
  ztreat = 1,
  zcontrol = 0,
  seed = 123,
  MLmethod = "lasso",
  k = 3,
  DR_parameters = list(s = NULL, normalized = TRUE, trim = 0.01),
  squared_parameters = list(zeta_sigma = min(0.5, 500/dim(y)[1])),
  bootstrap_parameters = list(B = 2000, importance = 0.95, alpha = 0.1, share = 0.5)
)
```

Arguments

y	Dependent variable, must not contain missings.
d	Treatment variable, must be discrete, must not contain missings.
x	Covariates, must not contain missings.
z	Instrument, must not contain missings.
score	Orthogonal score used for testing identification, either `"DR"` for using the average of the doubly robust (DR) score function (see Section 6 of Huber and Kueck, 2022) for testing, or `"squared"` for using squared differences in the conditional means outcomes (see Section 7 of Huber and Kueck, 2022). Default is `"DR"`. Note that this argument is ignored if `bootstrap=TRUE`.
bootstrap	If set to `TRUE`, testing identification is based on the DR score function within data-driven partitioning of the data (using a random forest with 200 trees) as described at the end of Sections 6 and 8 in Huber and Kueck (2022). Default is `FALSE`. Note that the argument `score` is ignored if `bootstrap=TRUE`.
ztreat	Value of the instrument in the "treatment" group. Default is 1.
zcontrol	Value of the instrument in the "control" group. Default is 0.
seed	Default is 123.

MLmethod   Machine learning method for estimating the nuisance parameters based on the
                    SuperLearner package. Must be either "lasso" (default) for lasso estimation,
                    "randomforest" for random forests, "xgboost" for xg boosting, "svm" for
                    support vector machines, "ensemble" for using an ensemble algorithm based
                    on all previously mentioned machine learners, or "parametric" for linear or
                    logit regression.

k   Number of folds in k-fold cross-fitting. Default is 3.

DR_parameters   List of input parameters to test identification using the doubly robust score: s:
                    Indicator function for defining a subpopulation for which the treatment effect is
                    estimated as a function of the subpopulation's distribution of x. Default is NULL
                    (estimation of the average treatment effect in the total population). normalized:
                    If set to TRUE, then the inverse probability-based weights are normalized such
                    that they add up to 1 within treatment groups. Default is TRUE trim: Trimming
                    rule for discarding observations with treatment propensity scores that are smaller
                    than trim or larger than 1-trim (to avoid too small denominators in weighting
                    by the inverse of the propensity scores). Default is 0.01.

squared_parameters
                    List of input parameters to test identification using the squared deviation: zeta_sigma:
                    standard deviation of the normal distributed errors to avoid degenerated limit
                    distribution. Default is min(0.05,500/n).

bootstrap_parameters
                    List of input parameters to test identification using the DR score and sample
                    splitting to detect heterogeneity (if bootstrap=TRUE): B: number of bootstrap
                    samples to be used in the multiplier bootstrap. Default is 2000. importance:
                    upper quantile of covariates in terms of their predictive importance for hetero-
                    geneity in the DR score function according to a random forest (with 200 trees).
                    The data are split into subsets based on the median values of these predictive
                    covariates (entering the upper quantile). Default is 0.95. alpha: level of the
                    statistical test. Default is 0.1. share: share of observations used to detect het-
                    erogeneity in the DR score function by the random forest (while the remaining
                    observations are used for hypothesis testing). Default is 0.5.

Details

Testing the identification of causal effects of a treatment d on an outcome y in observational data
using a supposed instrument z and controlling for observed covariates x.

Value

An identificationDML object contains different parameters, at least the two following:

effect: estimate of the target parameter(s).

pval: p-value(s) of the identification test.

References

Huber, M., & Kueck, J. (2022): Testing the identification of causal effects in observational data.
arXiv:2203.15890.

Examples

```
# Two examples with simulated data
## Not run:
set.seed(777)
n <- 20000  # sample size
p <- 50     # number of covariates
s <- 5  # sparsity (relevant covariates)
alpha <- 0.1     # level

control violation of identification
delta <- 2    # effect of unobservable in outcome on index of treatment - either 0 or 2
gamma <- 0   # direct effect of the instrument on outcome  - either 0 or 0.1

DGP - general
xcorr <- 1   # if 1, then non-zero covariance between regressors
if (xcorr == 0) {
 sigmax <- diag(1,p)}       # covariate matrix at baseline
if (xcorr != 0){
 sigmax = matrix(NA,p,p)
for (i in 1:p){
   for (j in 1:p){
     sigmax[i,j] = 0.5^(abs(i-j))
   }
 }}
sparse = FALSE # if FALSE, an approximate sparse setting is considered
beta = rep(0,p)
if (sparse == TRUE){
 for (j in 1:s){ beta[j] <- 1} }
if (sparse != TRUE){
 for (j in 1:p) beta[j] <- (1/j)}
noise_U <- 0.1 # control signal-to-noise
noise_V <- 0.1
noise_W <- 0.25
x <- (rmvnorm(n,rep(0,p),sigmax))
w <- rnorm(n,0,sd=noise_W)
z <- 1*(rnorm(n)>0)
d <- (x%*%beta+z+w+rnorm(n,0,sd=noise_V)>0)*1          # treatment equation

DGP 1 - effect homogeneity

y <- x%*%beta+d+gamma*z+delta*w+rnorm(n,0,sd=noise_U)

output1 <- identificationDML(y = y, d=d, x=x, z=z, score = "DR", bootstrap = FALSE,
ztreat = 1, zcontrol = 0 , seed = 123, MLmethod ="lasso", k = 3,
DR_parameters = list(s = NULL , normalized = TRUE, trim = 0.01))
output1$pval
output2 <- identificationDML(y=y, d=d, x=x, z=z, score = "squared", bootstrap = FALSE,
ztreat = 1, zcontrol =0 , seed = 123, MLmethod ="lasso", k = 3)
output2$pval
output3 <- identificationDML(y=y, d=d, x=x, z=z, score = "squared", bootstrap = TRUE,
ztreat = 1, zcontrol =0 , seed = 123, MLmethod ="lasso", k = 3,
DR_parameters = list(s = NULL , normalized = TRUE, trim = 0.005),
```

```
bootstrap_parameters = list(B = 2000, importance = 0.95, alpha = 0.1, share = 0.5))
output3$pval

DGP 2 - effect heterogeneity

y = x%*%beta+d+gamma*z*x[,1]+gamma*z*x[,2]+delta*w*x[,1]+delta*w*x[,2]+rnorm(n/2,0,sd=noise_U)

output1 <- identificationDML(y = y, d=d, x=x, z=z, score = "DR", bootstrap = FALSE,
ztreat = 1, zcontrol = 0 , seed = 123, MLmethod ="lasso", k = 3,
DR_parameters = list(s = NULL , normalized = TRUE, trim = 0.01))
output1$pval
output2 <- identificationDML(y=y, d=d, x=x, z=z, score = "squared", bootstrap = FALSE,
ztreat = 1, zcontrol =0 , seed = 123, MLmethod ="lasso", k = 3)
output2$pval
output3 <- identificationDML(y=y, d=d, x=x, z=z, score = "DR", bootstrap = TRUE,
ztreat = 1, zcontrol =0 , seed = 123, MLmethod ="lasso", k = 3,
DR_parameters = list(s = NULL , normalized = TRUE, trim = 0.005),
bootstrap_parameters = list(B = 2000, importance = 0.95, alpha = 0.1, share = 0.5))
output3$pval

## End(Not run)
```

---

india   *India's National Health Insurance Program (RSBY)*

Description

A dataset which is a subset of the data from the randomized evaluation of the India's National Health Insurance Program (RSBY).

Usage

```
india
```

Format

A data frame with 11'089 rows and 7 variables:

X individual identification

village_id village identification

DistrictId district identification

treat treatment status (insurance)

mech treatment assignment mechanism

enrolled enrolled

EXPhosp_1 hospital expenditure

References

Imai, Kosuke; Jiang, Zhichao; Malani, Anup, 2020, "Replication Data for: Causal Inference with Interference and Noncompliance in Two-Stage Randomized Experiments.", https://doi.org/10.7910/DVN/N7D9LS, Harvard Dataverse, V1

Examples

```
## Not run:
require(devtools)                      # load devtools package
install_github("szonszein/interference") # install interference package
library(interference)                  # load interference package
data(india)                            # load data
attach(india)                          # attach data
india=na.omit(india)                   # drop observations with missings
group=india$village_id                 # cluster id
group_tr=india$mech                    # indicator high treatment proportion
indiv_tr=india$treat                   # individual treatment (insurance)
obs_outcome=india$EXPhosp_1            # outcome  (hospital expenditure)
dat=data.frame(group,group_tr,indiv_tr,obs_outcome) # generate data frame
estimates_hierarchical(dat)
## End(Not run)          # run estimation
```

---

ivnr	*Instrument-based treatment evaluation under endogeneity and non-response bias*

Description

Non- and semiparaemtric treatment effect estimation under treatment endogeneity and selective non-response in the outcome based on a binary instrument for the treatment and a continous instrument for response.

Usage

```
ivnr(
  y,
  d,
  r,
  z1,
  z2,
  x = NULL,
  xpar = NULL,
  ruleofthumb = 1,
  wgtfct = 2,
  rtype = "ll",
  numresprob = 20,
  boot = 499,
  estlate = TRUE,
```

```
    trim = 0.01
)
```

Arguments

y	Dependent variable.
d	Treatment, must be binary and must not contain missings.
r	Response, must be a binary indicator for whether the outcome is observed.
z1	Binary instrument for the treatment, must not contain missings.
z2	Continuous instrument for response, must not contain missings.
x	A data frame of covariates to be included in the nonparametric estimation, must not contain missings. Factors and ordered varaibles must be appropriately defined as such by factor() and ordered(). Default is NULL (no covariates included). Covariates are only considered if both x and xpar are not NULL.
xpar	Covariates to be included in the semiparametric estimation, must not contain missings. Default is NULL (no covariates included). Covariates are only considered if both x and xpar are not NULL.
ruleofthumb	If 1, bandwidth selection in any kernel function is based on the Silverman (1986) rule of thumb. Otherwise, least squares cross-validation is used. Default is 1.
wgtfct	Weighting function to be used in effect estimation. If set to 1, equation (18) in Fricke et al (2020) is used as weight. If set to 2, equation (19) in Fricke et al (2020) is used as weight. If set to 3, the median of LATEs across values of response probabilities numresprob is used. Default is 2.
rtype	Regression type used for continuous outcomes in the kernel regressions. Either "ll" for local linear or "lc" for local constant regression. Default is "ll".
numresprob	number of response probabilities at which the effects are evaluated. An equidistant grid is constructed based on the number provided. Default is 20.
boot	Number of bootstrap replications for estimating standard errors of the effects. Default is 499.
estlate	If set to TRUE the local average treatment effect on compliers (LATE) is estimated, otherwise the average treatment effect (ATE) is estimated. Default is TRUE.
trim	Trimming rule for too extreme denominators in the weighting functions or inverses of products of conditional treatment probabilities. Values below trim are set to trim to avoid values that are too close to zero in any denominator. Default is 0.01.

Details

Non- and semiparametric treatment effect estimation under treatment endogeneity and selective non-response in the outcome based on a binary instrument for the treatment and a continuous instrument for response. The effects are estimated both semi-parametrically (using probit and OLS for the estimation of plug-in parameters like conditional probabilities and outcomes) and fully non-parametrically (based on kernel regression for any conditional probability/mean). Besides the instrument-based estimates, results are also presented under a missing-at-random assumption (MAR) when not using the instrument z2 for response (but only z1 for the treatment). See Fricke et al. (2020) for further details.

Value

A `ivnr` object contains one output component:

`output`: The first row provides the effect estimates under non- and semi-parametric estimation using both instruments, see ”`nonpara (L)ATE IV`” and ”`semipara (L)ATE IV`” as well as under a missing-at-random assumption for response when using only the first instrument for the treatment, see ”`nonpara (L)ATE MAR`” and ”`semipara (L)ATE MAR`”. The second row provides the standard errors based on bootstrapping the effects. The third row provides the p-values based on the t-statistics.

References

Fricke, H., Frölich, M., Huber, M., Lechner, M. (2020): "Endogeneity and non-response bias in treatment evaluation - nonparametric identification of causal effects by instruments", Journal of Applied Econometrics, forthcoming.

Examples

```
# A little example with simulated data (1000 observations)
## Not run:
n=1000           # sample size
e<-(rmvnorm(n,rep(0,3), matrix(c(1,0.5,0.5,  0.5,1,0.5,  0.5,0.5,1),3,3)))
# correlated error term of treatment, response, and outcome equation
x=runif(n,-0.5,0.5)          # observed confounder
z1<-(-0.25*x+rnorm(n)>0)*1    # binary instrument for treatment
z2<- -0.25*x+rnorm(n)         # continuous instrument for selection
d<-(z1-0.25*x+e[,1]>0)*1      # treatment equation
 y_star<- -0.25*x+d+e[,2]     # latent outcome
 r<-(-0.25*x+z2+d+e[,3]>0)*1  # response equation
 y=y_star                     # observed outcome
 y[r==0]=0                    # nonobserved outcomes are set to zero
 # The true treatment effect is 1
 ivnr(y=y,d=d,r=r,z1=z1,z2=z2,x=x,xpar=x,numresprob=4,boot=39)
## End(Not run)
```

`JC`   *Job Corps data*

Description

A dataset from the U.S. Job Corps experimental study with information on the participation of disadvantaged youths in (academic and vocational) training in the first and second year after program assignment.

Usage

```
JC
```

Format

A data frame with 9240 rows and 46 variables:

assignment 1=randomly assigned to Job Corps, 0=randomized out of Job Corps

female 1=female, 0=male

age age in years at assignment

white 1=white, 0=non-white

black 1=black, 0=non-black

hispanic 1=hispanic, 0=non-hispanic

educ years of education at assignment

educmis 1=education missing at assignment

geddegree 1=has a GED degree at assignment

hsdegree 1=has a high school degree at assignment

english 1=English mother tongue

cohabmarried 1=cohabiting or married at assignment

haschild 1=has at least one child, 0=no children at assignment

everwkd 1=has ever worked at assignment, 0=has never worked at assignment

mwearn average weekly gross earnings at assignment

hhsize household size at assignment

hhsizemis 1=household size missing

educmum mother's years of education at assignment

educmummis 1=mother's years of education missing

educdad father's years of education at assignment

educdadmis 1=father's years of education missing

welfarechild welfare receipt during childhood in categories from 1 to 4 (measured at assignment)

welfarechildmis 1=missing welfare receipt during childhood

health general health at assignment from 1 (excellent) to 4 (poor)

healthmis 1=missing health at assignment

smoke extent of smoking at assignment in categories from 1 to 4

smokemis 1=extent of smoking missing

alcohol extent of alcohol consumption at assignment in categories from 1 to 4

alcoholmis 1=extent of alcohol consumption missing

everwkdy1 1=has ever worked one year after assignment, 0=has never worked one year after assignment

earnq4 weekly earnings in fourth quarter after assignment

earnq4mis 1=missing weekly earnings in fourth quarter after assignment

pworky1 proportion of weeks employed in first year after assignment

pworky1mis 1=missing proportion of weeks employed in first year after assignment

health12 general health 12 months after assignment from 1 (excellent) to 4 (poor)

health12mis 1=missing general health 12 months after assignment

trainy1 1=enrolled in education and/or vocational training in the first year after assignment, 0=no education or training in the first year after assignment

trainy2 1=enrolled in education and/or vocational training in the second year after assignment, 0=no education or training in the second year after assignment

pworky2 proportion of weeks employed in second year after assignment

pworky3 proportion of weeks employed in third year after assignment

pworky4 proportion of weeks employed in fourth year after assignment

earny2 weekly earnings in second year after assignment

earny3 weekly earnings in third year after assignment

earny4 weekly earnings in fourth year after assignment

health30 general health 30 months after assignment from 1 (excellent) to 4 (poor)

health48 general health 48 months after assignment from 1 (excellent) to 4 (poor)

References

Schochet, P. Z., Burghardt, J., Glazerman, S. (2001): "National Job Corps study: The impacts of Job Corps on participants' employment and related outcomes", Mathematica Policy Research, Washington, DC.

Examples

```
## Not run:
data(JC)
# Dynamic treatment effect evaluation of training in 1st and 2nd year
# define covariates at assignment (x0) and after one year (x1)
x0=JC[,2:29]; x1=JC[,30:36]
# define treatment (training) in first year (d1) and second year (d2)
d1=JC[,37]; d2=JC[,38]
# define outcome (weekly earnings in fourth year after assignment)
y2=JC[,44]
# assess dynamic treatment effects (training in 1st+2nd year vs. no training)
output=dyntreatDML(y2=y2, d1=d1, d2=d2, x0=x0, x1=x1)
cat("dynamic ATE: ",round(c(output$effect),3),", standard error: ",
    round(c(output$se),3), ", p-value: ",round(c(output$pval),3))
## End(Not run)
```

---

lateweight	*Local average treatment effect estimation based on inverse probability weighting*

Description

Instrumental variable-based evaluation of local average treatment effects using weighting by the inverse of the instrument propensity score.

Usage

```
lateweight(
  y,
  d,
  z,
  x,
  LATT = FALSE,
  trim = 0.05,
  logit = FALSE,
  boot = 1999,
  cluster = NULL
)
```

Arguments

y	Dependent variable, must not contain missings.
d	Treatment, must be binary (either 1 or 0), must not contain missings.
z	Instrument for the endogenous treatment, must be binary (either 1 or 0), must not contain missings.
x	Confounders of the instrument and outcome, must not contain missings.
LATT	If FALSE, the local average treatment effect (LATE) among compliers (whose treatment reacts to the instrument) is estimated. If TRUE, the local average treatment effect on the treated compliers (LATT) is estimated. Default is FALSE.
trim	Trimming rule for discarding observations with extreme propensity scores. If LATT=FALSE, observations with $Pr(Z=1|X)<$trim or $Pr(Z=1|X)>(1-$trim$)$ are dropped. If LATT=TRUE, observations with $Pr(Z=1|X)>(1-$trim$)$ are dropped. Default is 0.05.
logit	If FALSE, probit regression is used for propensity score estimation. If TRUE, logit regression is used. Default is FALSE.
boot	Number of bootstrap replications for estimating standard errors. Default is 1999.
cluster	A cluster ID for block or cluster bootstrapping when units are clustered rather than iid. Must be numerical. Default is NULL (standard bootstrap without clustering).

Details

Estimation of local average treatment effects of a binary endogenous treatment based on a binary instrument that is conditionally valid, implying that all confounders of the instrument and the outcome are observed. Units are weighted by the inverse of their conditional instrument propensities given the observed confounders, which are estimated by probit or logit regression. Standard errors are obtained by bootstrapping the effect.

Value

A lateweight object contains 10 components, effect, se.effect, pval.effect, first, se.first, pval.first, ITT, se.ITT, pval.ITT, and ntrimmed:

effect: local average treatment effect (LATE) among compliers if LATT=FALSE or the local average treatment effect on treated compliers (LATT) if LATT=TRUE.

se.effect: bootstrap-based standard error of the effect.

pval.effect: p-value of the effect.

first: first stage estimate of the complier share if LATT=FALSE or the first stage estimate among treated if LATT=TRUE.

se.first: bootstrap-based standard error of the first stage effect.

pval.first: p-value of the first stage effect.

ITT: intention to treat effect (ITT) of z on y if LATT=FALSE or the ITT among treated if LATT=TRUE.

se.ITT: bootstrap-based standard error of the ITT.

pval.ITT: p-value of the ITT.

ntrimmed: number of discarded (trimmed) observations due to extreme propensity score values.

References

Frölich, M. (2007): "Nonparametric IV estimation of local average treatment effects with covariates", Journal of Econometrics, 139, 35-75.

Examples

```
# A little example with simulated data (10000 observations)
## Not run:
n=10000
u=rnorm(n)
x=rnorm(n)
z=(0.25*x+rnorm(n)>0)*1
d=(z+0.25*x+0.25*u+rnorm(n)>0.5)*1
y=0.5*d+0.25*x+u
# The true LATE is equal to 0.5
output=lateweight(y=y,d=d,z=z,x=x,trim=0.05,LATT=FALSE,logit=TRUE,boot=19)
cat("LATE: ",round(c(output$effect),3),", standard error: ",
            round(c(output$se.effect),3), ", p-value: ",
            round(c(output$pval.effect),3))
output$ntrimmed
## End(Not run)
```

---

medDML   *Causal mediation analysis with double machine learning*

Description

Causal mediation analysis (evaluation of natural direct and indirect effects) for a binary treatment and one or several mediators using double machine learning to control for confounders based on (doubly robust) efficient score functions for potential outcomes.

Usage

```
medDML(
  y,
  d,
  m,
  x,
  k = 3,
  trim = 0.05,
  order = 1,
  multmed = TRUE,
  fewsplits = FALSE,
  normalized = TRUE
)
```

Arguments

y	Dependent variable, must not contain missings.
d	Treatment, must be binary (either 1 or 0), must not contain missings.
m	Mediator, must not contain missings. May be a scalar or a vector of binary, categorical, or continuous variables if `multmed` is `TRUE`. Must be a binary scalar if `multmed` is `FALSE`.
x	(Potential) pre-treatment confounders of the treatment, mediator, and/or outcome, must not contain missings.
k	Number of folds in k-fold cross-fitting if `multmed` is `FALSE`. k-1 folds are used for estimating the model parameters of the treatment, mediator, and outcome equations and one fold is used for predicting the efficient score functions. The roles of the folds are swapped. Default for k is 3. If `multmed` is `TRUE`, then 3-fold cross-valdiation is used, irrespective of the number provided in k (i.e. k is ignored if `multmed` is `TRUE`).
trim	Trimming rule for discarding observations with extreme conditional treatment or mediator probabilities (or products thereof). Observations with (products of) conditional probabilities that are smaller than `trim` in any denominator of the potential outcomes are dropped. Default is 0.05.
order	If set to an integer larger than 1, then polynomials of that order and interactions (using the power series) rather than the original control variables are used in the estimation of any conditional probability or conditional mean outcome. Polynomials/interactions are created using the `Generate.Powers` command of the LARF package.
multmed	If set to `TRUE`, a representation of direct and indirect effects that avoids conditional mediator densities/probabilities is used, see Farbmacher, Huber, Langen, and Spindler (2019). This method can incorporate multiple and/or continuous mediators. If `multmed` is `FALSE`, the representation of Tchetgen Tchetgen and Shpitser (2012) is used, which involves mediator densities. In this case, the mediator must be a binary scalar. Default of `multimed` is `TRUE`.
fewsplits	If set to `TRUE`, the same training data are used for estimating nested models of nuisance parameters, i.e. `E[Y|D=d,M,X]` and `E[E[Y|D=d,M,X]|D=1-d,X]`. If

fewsplits is FALSE, the training data are split for the sequential estimation of nested models E[Y|D=d,M,X] and E[E[Y|D=d,M,X]|D=1-d,X]. This parameter is only relevant if multmed is TRUE. Default of fewsplits is FALSE.

normalized   If set to TRUE, then the inverse probability-based weights are normalized such that they add up to 1 within treatment groups. Default is TRUE.

Details

Estimation of causal mechanisms (natural direct and indirect effects) of a treatment under selection on observables, assuming that all confounders of the binary treatment and the mediator, the treatment and the outcome, or the mediator and the outcome are observed and not affected by the treatment. Estimation is based on the (doubly robust) efficient score functions for potential outcomes, see Tchetgen Tchetgen and Shpitser (2012) and Farbmacher, Huber, Langen, and Spindler (2019), as well as on double machine learning with cross-fitting, see Chernozhukov et al (2018). To this end, one part of the data is used for estimating the model parameters of the treatment, mediator, and outcome equations based on post-lasso regression, using the rlasso and rlassologit functions (for conditional means and probabilities, respectively) of the hdm package with default settings. The other part of the data is used for predicting the efficient score functions. The roles of the data parts are swapped and the direct and indirect effects are estimated based on averaging the predicted efficient score functions in the total sample. Standard errors are based on asymptotic approximations using the estimated variance of the (estimated) efficient score functions.

Value

A medDML object contains two components, results and ntrimmed:

results: a 3X6 matrix containing the effect estimates in the first row ("effects"), standard errors in the second row ("se"), and p-values in the third row ("p-value"). The first column provides the total effect, namely the average treatment effect (ATE). The second and third columns provide the direct effects under treatment and control, respectively ("dir.treat", "dir.control"). The fourth and fifth columns provide the indirect effects under treatment and control, respectively ("indir.treat", "indir.control"). The sixth column provides the estimated mean under non-treatment ("Y(0,M(0))").

ntrimmed: number of discarded (trimmed) observations due to extreme conditional probabilities.

References

Chernozhukov, V., Chetverikov, D., Demirer, M., Duflo, E., Hansen, C., Newey, W., Robins, J. (2018): "Double/debiased machine learning for treatment and structural parameters", The Econometrics Journal, 21, C1-C68.

Farbmacher, H., Huber, M., Laffers, L., Langen, H., and Spindler, M. (2019): "Causal mediation analysis with double machine learning", working paper, University of Fribourg.

Tchetgen Tchetgen, E. J., and Shpitser, I. (2012): "Semiparametric theory for causal mediation analysis: efficiency bounds, multiple robustness, and sensitivity analysis", The Annals of Statistics, 40, 1816-1845.

Tibshirani, R. (1996): "Regression shrinkage and selection via the lasso", Journal of the Royal Statistical Society: Series B, 58, 267-288.

Examples

```
# A little example with simulated data (10000 observations)
## Not run:
n=10000                          # sample size
p=100                            # number of covariates
s=2                              # number of covariates that are confounders
x=matrix(rnorm(n*p),ncol=p)      # covariate matrix
beta=c(rep(0.25,s), rep(0,p-s))  # coefficients determining degree of confounding
d=(x%*%beta+rnorm(n)>0)*1        # treatment equation
m=(x%*%beta+0.5*d+rnorm(n)>0)*1  # mediator equation
y=x%*%beta+0.5*d+m+rnorm(n)      # outcome equation
# The true direct effects are equal to 0.5, the indirect effects equal to 0.19
output=medDML(y=y,d=d,m=m,x=x)
round(output$results,3)
output$ntrimmed
## End(Not run)
```

---

medlateweight	*Causal mediation analysis with instruments for treatment and mediator based on weighting*

Description

Causal mediation analysis (evaluation of natural direct and indirect effects) with instruments for a binary treatment and a continuous mediator based on weighting as suggested in Frölich and Huber (2017), Theorem 1.

Usage

```
medlateweight(
  y,
  d,
  m,
  zd,
  zm,
  x,
  trim = 0.1,
  csquared = FALSE,
  boot = 1999,
  cminobs = 40,
  bwreg = NULL,
  bwm = NULL,
  logit = FALSE,
  cluster = NULL
)
```

Arguments

y	Dependent variable, must not contain missings.
d	Treatment, must be binary (either 1 or 0), must not contain missings.
m	Mediator(s),must be a continuous scalar, must not contain missings.
zd	Instrument for the treatment, must be binary (either 1 or 0), must not contain missings.
zm	Instrument for the mediator, must contain at least one continuous element, may be a scalar or a vector, must not contain missings. If no user-specified bandwidth is provided for the regressors when estimating the conditional cumulative distribution function F(M|Z2,X), i.e. if bwreg=NULL, then zm must be exclusively numeric.
x	Pre-treatment confounders, may be a scalar or a vector, must not contain missings. If no user-specified bandwidth is provided for the regressors when estimating the conditional cumulative distribution function F(M|Z2,X), i.e. if bwreg=NULL, then x must be exclusively numeric.
trim	Trimming rule for discarding observations with extreme weights. Discards observations whose relative weight would exceed the value in trim in the estimation of any of the potential outcomes. Default is 0.1 (i.e. a maximum weight of 10 percent per observation).
csquared	If TRUE, then not only the control function C, but also its square is used as regressor in any estimated function that conditions on C. Default is FALSE.
boot	Number of bootstrap replications for estimating standard errors. Default is 1999.
cminobs	Minimum number of observations to compute the control function C, see the numerator of equation (7) in Frölich and Huber (2017). A larger value increases boundary bias when estimating the control function for lower values of M, but reduces the variance. Default is 40, but should be adapted to sample size and the number of variables in Z2 and X.
bwreg	Bandwidths for zm and x in the estimation of the conditional cumulative distribution function F(M|Z2,X) based on the np package by Hayfield and Racine (2008). The length of the numeric vector must correspond to the joint number of elements in zm and x and will be used both in the original sample for effect estimation and in bootstrap samples to compute standard errors. If set to NULL, then the rule of thumb is used for bandwidth calculation, see the np package for details. In the latter case, all elements in the regressors must be numeric. Default is NULL.
bwm	Bandwidth for m in the estimation of the conditional cumulative distribution function F(M|Z2,X) based on the np package by Hayfield and Racine (2008). Must be scalar and will be used both in the original sample for effect estimation and in bootstrap samples to compute standard errors. If set to NULL, then the rule of thumb is used for bandwidth calculation, see the np package for details. Default is NULL.
logit	If FALSE, probit regression is used for any propensity score estimation. If TRUE, logit regression is used. Default is FALSE.
cluster	A cluster ID for block or cluster bootstrapping when units are clustered rather than iid. Must be numerical. Default is NULL (standard bootstrap without clustering).

Details

Estimation of causal mechanisms (natural direct and indirect effects) of a binary treatment among
treatment compliers based on distinct instruments for the treatment and the mediator. The treatment
and its instrument are assumed to be binary, while the mediator and its instrument are assumed
to be continuous, see Theorem 1 in Frölich and Huber (2017). The instruments are assumed to
be conditionally valid given a set of observed confounders. A control function is used to tackle
mediator endogeneity. Standard errors are obtained by bootstrapping the effects.

Value

A medlateweight object contains two components, `results` and `ntrimmed`:

`results`: a 3x7 matrix containing the effect estimates in the first row ("effects"), standard errors
in the second row ("se"), and p-values in the third row ("p-value"). The first column provides
the total effect, namely the local average treatment effect (LATE) on the compliers. The second
and third columns provide the direct effects under treatment and control, respectively ("dir.treat",
"dir.control"). The fourth and fifth columns provide the indirect effects under treatment and control,
respectively ("indir.treat", "indir.control"). The sixth and seventh columns provide the parametric
direct and indirect effect estimates ("dir.para", "indir.para") without interaction terms, respectively.
For the parametric estimates, probit or logit specifications are used for the treatment model and OLS
specifications for the mediator and outcome models.

`ntrimmed`: number of discarded (trimmed) observations due to large weights.

References

Frölich, M. and Huber, M. (2017): "Direct and indirect treatment effects: Causal chains and me-
diation analysis with instrumental variables", Journal of the Royal Statistical Society Series B, 79,
1645–1666.

Examples

```
# A little example with simulated data (3000 observations)
## Not run:
n=3000; sigma=matrix(c(1,0.5,0.5,0.5,1,0.5,0.5,0.5,1),3,3)
e=(rmvnorm(n,rep(0,3),sigma))
x=rnorm(n)
zd=(0.5*x+rnorm(n)>0)*1
d=(-1+0.5*x+2*zd+e[,3]>0)
zm=0.5*x+rnorm(n)
m=(0.5*x+2*zm+0.5*d+e[,2])
y=0.5*x+d+m+e[,1]
# The true direct and indirect effects on compliers are equal to 1 and 0.5, respectively
medlateweight(y,d,m,zd,zm,x,trim=0.1,csquared=FALSE,boot=19,cminobs=40,
bwreg=NULL,bwm=NULL,logit=FALSE)
## End(Not run)
```

medweight   *Causal mediation analysis based on inverse probability weighting with*
                             optional sample selection correction.

Description

Causal mediation analysis (evaluation of natural direct and indirect effects) based on weighting by
the inverse of treatment propensity scores as suggested in Huber (2014) and Huber and Solovyeva
(2018).

Usage

```
medweight(
  y,
  d,
  m,
  x,
  w = NULL,
  s = NULL,
  z = NULL,
  selpop = FALSE,
  ATET = FALSE,
  trim = 0.05,
  logit = FALSE,
  boot = 1999,
  cluster = NULL
)
```

Arguments

y	Dependent variable, must not contain missings.
d	Treatment, must be binary (either 1 or 0), must not contain missings.
m	Mediator(s), may be a scalar or a vector, must not contain missings.
x	Pre-treatment confounders of the treatment, mediator, and/or outcome, must not contain missings.
w	Post-treatment confounders of the mediator and the outcome. Default is NULL. Must not contain missings.
s	Optional selection indicator. Must be one if y is observed (non-missing) and zero if y is not observed (missing). Default is NULL, implying that y does not contain any missings. Is ignored if w is not NULL.
z	Optional instrumental variable(s) for selection s. If NULL, outcome selection based on observables (x,d,m) - known as "missing at random" - is assumed.
selpop	Only to be used if both s and z are defined. If TRUE, the effects are estimated for the selected subpopulation with s=1 only. If FALSE, the effects are estimated for the total population.

ATET   If FALSE, the average treatment effect (ATE) and the corresponding direct and
                  indirect effects are estimated. If TRUE, the average treatment effect on the
                  treated (ATET) and the corresponding direct and indirect effects are estimated.
                  Default is FALSE.

trim   Trimming rule for discarding observations with extreme propensity scores. In
                  the absence of post-treatment confounders (w=NULL), observations with Pr(D=1|M,X)<trim
                  or Pr(D=1|M,X)>(1-trim) are dropped. In the presence of post-treatment con-
                  founders (w is defined), observations with Pr(D=1|M,W,X)<trim or Pr(D=1|M,W,X)>(1-
                  trim) are dropped. Default is 0.05. If s is defined (only considered if w is NULL!)
                  and z is NULL, observations with low selection propensity scores, Pr(S=1|D,M,X)<trim,
                  are discarded, too. If s and z are defined, the treatment propensity scores to be
                  trimmed change to Pr(D=1|M,X,Pr(S=1|D,X,Z)).

logit   If FALSE, probit regression is used for propensity score estimation. If TRUE,
                  logit regression is used. Default is FALSE.

boot   Number of bootstrap replications for estimating standard errors. Default is 1999.

cluster   A cluster ID for block or cluster bootstrapping when units are clustered rather
                  than iid. Must be numerical. Default is NULL (standard bootstrap without
                  clustering).

Details

Estimation of causal mechanisms (natural direct and indirect effects) of a binary treatment un-
der a selection on observables assumption assuming that all confounders of the treatment and the
mediator, the treatment and the outcome, or the mediator and the outcome are observed. Units
are weighted by the inverse of their conditional treatment propensities given the mediator and/or
observed confounders, which are estimated by probit or logit regression. The form of weighting
depends on whether the observed confounders are exclusively pre-treatment (x), or also contain
post-treatment confounders of the mediator and the outcome (w). In the latter case, only partial in-
direct effects (from d to m to y) can be estimated that exclude any causal paths from d to w to m to y,
see the discussion in Huber (2014). Standard errors are obtained by bootstrapping the effects. In the
absence of post-treatment confounders (such that w is NULL), defining s allows correcting for sample
selection due to missing outcomes based on the inverse of the conditional selection probability. The
latter might either be related to observables, which implies a missing at random assumption, or in
addition also to unobservables, if an instrument for sample selection is available. Effects are then
estimated for the total population, see Huber and Solovyeva (2018) for further details.

Value

A medweight object contains two components, results and ntrimmed:

results: a 3X5 matrix containing the effect estimates in the first row ("effects"), standard errors in
the second row ("se"), and p-values in the third row ("p-value"). The first column provides the total
effect, namely the average treatment effect (ATE) if ATET=FALSE or the average treatment effect on
the treated (ATET) if ATET=TRUE. The second and third columns provide the direct effects under
treatment and control, respectively ("dir.treat", "dir.control"). See equation (6) if w=NULL (no post-
treatment confounders) and equation (13) if w is defined, respectively, in Huber (2014). If w=NULL,
the fourth and fifth columns provide the indirect effects under treatment and control, respectively
("indir.treat", "indir.control"), see equation (7) in Huber (2014). If w is defined, the fourth and fifth

columns provide the partial indirect effects under treatment and control, respectively ("par.in.treat", "par.in.control"), see equation (14) in Huber (2014).

ntrimmed: number of discarded (trimmed) observations due to extreme propensity score values.

References

Huber, M. (2014): "Identifying causal mechanisms (primarily) based on inverse probability weighting", Journal of Applied Econometrics, 29, 920-943.

Huber, M. and Solovyeva, A. (2018): "Direct and indirect effects under sample selection and outcome attrition ", SES working paper 496, University of Fribourg.

Examples

```
# A little example with simulated data (10000 observations)
## Not run:
n=10000
x=rnorm(n)
d=(0.25*x+rnorm(n)>0)*1
w=0.2*d+0.25*x+rnorm(n)
m=0.5*w+0.5*d+0.25*x+rnorm(n)
y=0.5*d+m+w+0.25*x+rnorm(n)
# The true direct and partial indirect effects are all equal to 0.5
output=medweight(y=y,d=d,m=m,x=x,w=w,trim=0.05,ATET=FALSE,logit=TRUE,boot=19)
round(output$results,3)
output$ntrimmed
## End(Not run)
```

---

medweightcont *Causal mediation analysis with a continuous treatment based on weighting by the inverse of generalized propensity scores*

Description

Causal mediation analysis (evaluation of natural direct and indirect effects) of a continuous treatment based on weighting by the inverse of generalized propensity scores as suggested in Hsu, Huber, Lee, and Lettry (2020).

Usage

```
medweightcont(
  y,
  d,
  m,
  x,
  d0,
  d1,
  ATET = FALSE,
  trim = 0.1,
```

```
  lognorm = FALSE,
  bw = NULL,
  boot = 1999,
  cluster = NULL
)
```

Arguments

y	Dependent variable, must not contain missings.
d	Continuous treatment, must not contain missings.
m	Mediator(s), may be a scalar or a vector, must not contain missings.
x	Pre-treatment confounders of the treatment, mediator, and/or outcome, must not contain missings.
d0	Value of d under non-treatment. Effects are based on pairwise comparisons, i.e. differences in potential outcomes evaluated at d1 and d0.
d1	Value of d under treatment. Effects are based on pairwise comparisons, i.e. differences in potential outcomes evaluated at d1 and d0.
ATET	If FALSE, the average treatment effect (ATE) and the corresponding direct and indirect effects are estimated. If TRUE, the average treatment effect on the treated (ATET) and the corresponding direct and indirect effects are estimated. Default is FALSE.
trim	Trimming rule for discarding observations with too large weights in the estimation of any mean potential outcome. That is, observations with a weight>trim are dropped from the sample. Default is a maximum weight of 0.1 (or 10 percent) per observation.
lognorm	If FALSE, a linear model with normally distributed errors is assumed for generalized propensity score estimation. If TRUE, a lognormal model is assumed. Default is FALSE.
bw	Bandwith for the second order Epanechnikov kernel functions of the treatment. If set to NULL, bandwidth computation is based on the rule of thumb for Epanechnikov kernels, determining the bandwidth as the standard deviation of the treatment times $2.34/(n^{0.25})$, where n is the sample size. Default is NULL.
boot	Number of bootstrap replications for estimating standard errors. Default is 1999.
cluster	A cluster ID for block or cluster bootstrapping when units are clustered rather than iid. Must be numerical. Default is NULL (standard bootstrap without clustering).

Details

Estimation of causal mechanisms (natural direct and indirect effects) of a continuous treatment under a selection on observables assumption assuming that all confounders of the treatment and the mediator, the treatment and the outcome, or the mediator and the outcome are observed. Units are weighted by the inverse of their conditional treatment densities (known as generalized propensity scores) given the mediator and/or observed confounders, which are estimated by linear or loglinear regression. Standard errors are obtained by bootstrapping the effects.

Value

A medweightcont object contains two components, `results` and `ntrimmed`:

`results`: a 3X5 matrix containing the effect estimates in the first row ("effects"), standard errors in the second row ("se"), and p-values in the third row ("p-value"). The first column provides the total effect, namely the average treatment effect (ATE) if `ATET=FALSE` or the average treatment effect on the treated (ATET), i.e. those with D=d1, if `ATET=TRUE`. The second and third columns provide the direct effects under treatment and control, respectively ("dir.treat", "dir.control"). The fourth and fifth columns provide the indirect effects under treatment and control, respectively ("indir.treat", "indir.control").

`ntrimmed`: number of discarded (trimmed) observations due to extreme propensity score values.

References

Hsu, Y.-C., Huber, M., Lee, Y.-Y., Lettry, L. (2020): "Direct and indirect effects of continuous treatments based on generalized propensity score weighting", Journal of Applied Econometrics, forthcoming.

Examples

```
# A little example with simulated data (10000 observations)
## Not run:
n=10000
x=runif(n=n,min=-1,max=1)
d=0.25*x+runif(n=n,min=-2,max=2)
d=d-min(d)
m=0.5*d+0.25*x+runif(n=n,min=-2,max=2)
y=0.5*d+m+0.25*x+runif(n=n,min=-2,max=2)
# The true direct and indirect effects are all equal to 0.5
output=medweightcont(y,d,m,x,d0=2,d1=3,ATET=FALSE,trim=0.1,
        lognorm=FALSE,bw=NULL,boot=19)
round(output$results,3)
output$ntrimmed
## End(Not run)
```

RDDcovar   *Sharp regression discontinuity design conditional on covariates*

Description

Nonparametric (kernel regression-based) sharp regression discontinuity controlling for covariates that are permitted to jointly affect the treatment assignment and the outcome at the threshold of the running variable, see Frölich and Huber (2019).

Usage

```
RDDcovar(
  y,
  z,
  x,
  boot = 1999,
  bw0 = NULL,
  bw1 = NULL,
  regtype = "ll",
  bwz = NULL
)
```

Arguments

y	Dependent variable, must not contain missings.
z	Running variable. Must be coded such that the treatment is zero for z being smaller than zero and one for z being larger than or equal to zero. Must not contain missings.
x	Covariates, must not contain missings.
boot	Number of bootstrap replications for estimating standard errors. Default is 1999.
bw0	Bandwidth for a kernel regression of y on z and x below the threshold (for treatment equal to zero), using the Epanechnikov kernel. Default is NULL, implying that the bandwidth is estimated by least squares cross-validation.
bw1	Bandwidth for a kernel regression of y on z and x above the threshold (for treatment equal to one), using the Epanechnikov kernel. Default is NULL, implying that the bandwidth is estimated by least squares cross-validation.
regtype	Defines the type of the kernel regressions of y on z and x below and above the threshold. Must either be set to "ll" for local linear regression or to "ll" for local constant regression. Default is "ll".
bwz	Bandwidth for the (Epanechnikov) kernel function on z. Default is NULL, implying that the bandwidth is estimated by least squares cross-validation.

Details

Sharp regression discontinuity design conditional on covariates to control for observed confounders jointly affecting the treatment assignment and outcome at the threshold of the running variable as discussed in Frölich and Huber (2019). This is implemented by running kernel regressions of the outcome on the running variable and the covariates separately above and below the threshold and by applying a kernel smoother to the running variable around the threshold. The procedure permits choosing kernel bandwidths by cross-validation, even though this does in general not yield the optimal bandwidths for treatment effect estimation (checking the robustness of the results by varying the bandwidths is therefore highly recommended). Standard errors are based on bootstrapping.

Value

effect: Estimated treatment effect at the threshold.

se: Bootstrap-based standard error of the effect estimate.

pvalue: P-value based on the t-statistic.

bw0: Bandwidth for kernel regression of y on z and x below the threshold (for treatment equal to zero).

bw1: Bandwidth for kernel regression of y on z and x above the threshold (for treatment equal to one).

bwz: Bandwidth for the kernel function on z.

References

Frölich, M. and Huber, M. (2019): "Including covariates in the regression discontinuity design", Journal of Business & Economic Statistics, 37, 736-748.

Examples

```
## Not run:
# load unemployment duration data
data(ubduration)
# run sharp RDD conditional on covariates with user-defined bandwidths
output=RDDcovar(y=ubduration[,1],z=ubduration[,2],x=ubduration[,c(-1,-2)],
 bw0=c(0.17, 1, 0.01, 0.05, 0.54, 70000, 0.12, 0.91, 100000),
 bw1=c(0.59, 0.65, 0.30, 0.06, 0.81, 0.04, 0.12, 0.76, 1.03),bwz=0.2,boot=19)
cat("RDD effect estimate: ",round(c(output$effect),3),", standard error: ",
 round(c(output$se),3), ", p-value: ", round(c(output$pvalue),3))
## End(Not run)
```

---

rkd   *Swedish municipalities*

Description

A dataset containing information on Swedish municipalities in the years 1996-2004

Usage

```
rkd
```

Format

A data frame with 2511 rows and 53 variables:

code Municipality code

year Year

municipality Minicipality name

pop_1 Population, lagged 1 year

pop Population

partpop06 Share of population aged 0-6

partpop7_15 Share of population aged 7-15

partpop80_ Share of population aged 80+

partforeign Share of foreign born population

costequalgrants Cost-equalizing grants

popchange_10y 10 year out-migration, lagged 2 years

pers_admin Personnel, administration

pers_child Personnel, child care

pers_school Personnel, schools

pers_elder Personnel, elderly care

pers_total Personnel, total (full time equivalents pers 1,000 capita)

pers_social Personnel, social welfare

pers_tech Personnel, technical services

expenditures_total Total per capita public expenditures

wage_admin Average montly wage, administration

wage_child Average monthly wage, child care

wage_school Average monthly wage, schools

wage_elder Average monthly wage, elderly care

wage_total Average monthly wage, total

wage_social Average monthly wage, social welfare

wage_tech Average monthly wage, technical services

pers_officials Personnel, high administrative officials

pers_assistants Personnel, administrative assistants

pers_priv_school Outsourced personnel, schools

pers_priv_elder Outsourced personnel, elderly care

pers_priv_social Outsourced personnel, social welfare

pers_priv_child Outsourced personnel, child care

migrationgrant round(abs((popchange_10y+2)*100)) if popchange_10y <= -2, 0 otherwise

migpop migrationgrant*pop_1

summigpop sum(migpop) by year

sumpop sum(pop_1) by year

migrationmean summigpop/sumpop

exp_total Annual expenditures on personnel in 100SEK/capita

exp_admin Annual expenditures on personnel in 100SEK/capita

exp_child Annual expenditures on personnel in 100SEK/capita

exp_school Annual expenditures on personnel in 100SEK/capita

exp_elder Annual expenditures on personnel in 100SEK/capita

exp_social Annual expenditures on personnel in 100SEK/capita

exp_tech Annual expenditures on personnel in 100SEK/capita

expshare_total exp_total*100/expenditures_total

expshare_admin exp_admin*100/expenditures_total

expshare_child exp_child*100/expenditures_total

expshare_school exp_school*100/expenditures_total

expshare_elder exp_elder*100/expenditures_total

expshare_social exp_social*100/expenditures_total

expshare_tech exp_tech*100/expenditures_total

outmigration -popchange_10y

forcing outmigration-2

References

Lundqvist, Heléne, Dahlberg, Matz and Mörk, Eva (2014): "Stimulating Local Public Employment: Do General Grants Work?" American Economic Journal: Economic Policy, 6 (1): 167-92.

Examples

```
## Not run:
require(rdrobust)                       # load rdrobust package
require(causalweight)                   # load causalweight package
data(rkd)                               # load rkd data
attach(rkd)                             # attach rkd data
Y=pers_total                            # define outcome (total personnel)
R=forcing                               # define running variable
D=costequalgrants                       # define treatment (grants)
results=rdrobust(y=Y, x=R, fuzzy=D, deriv=1)  # run fuzzy RKD
summary(results)
## End(Not run)                         # show results
```

---

swissexper   *Correspondence test in Swiss apprenticeship market*

Description

A dataset related to a field experiment (correspondence test) in the Swiss apprenticeship market 2018/2019. The experiment investigated the effects of applicant gender and parental occupation in applications to apprenticeships on callback rates (invitations to interviews, assessment centers, or trial apprenticeships)

Usage

```
swissexper
```

Format

A data frame with 2928 rows and 18 variables:

city agglomeration of apprenticeship: 1=Bern,2=Zurich,3=Basel,6=Lausanne

foundatdate date when job add was found

employees (estimated) number of employees: 1=1-20; 2=21-50; 3=51-100; 4=101-250; 5=251-500; 6=501-1000; 7=1001+

sector 1=public sector; 2=trade/wholesale; 3=manufacturing/goods; 4=services

uniqueID ID of application

sendatdate date when application was sent

job_father treatment: father's occupation: 1=professor; 2=unskilled worker; 3=intermediate commercial; 4=intermediate technical

job_mother treatment: mother's occupation: 1= primary school teacher; 2=homemaker

tier skill tier of apprenticeship: 1=lower; 2=intermediate; 3=upper

hasmoved applicant moved from different city: 1=yes; 0=no

contgender gender of contact person in company: 0=unknown; 1=female; 2=male

letterback 1: letters sent from company to applicant were returned; 0: no issues with returned letters

outcome_invite outcome: invitation to interview, assessment center, or trial apprenticeship: 1=yes; 0=no

female_appl treatment: 1=female applicant; 0=male applicant

antidiscrpolicy 1=explicit antidiscrimination policy on company's website; 0=no explicit antidiscrimination policy

outcome_interest outcome: either invitation, or asking further questions, or keeping application for further consideration

gender_neutrality 0=gender neutral job type; 1=female dominated job type; 2=male dominated type

company_activity scope of company's activity: 0=local; 1=national; 2=international

References

Fernandes, A., Huber, M., and Plaza, C. (2019): "The Effects of Gender and Parental Occupation in the Apprenticeship Market: An Experimental Evaluation", SES working paper 506, University of Fribourg.

---

treatDML	*Binary or multiple discrete treatment effect evaluation with double machine learning*

Description

Treatment effect estimation for assessing the average effects of discrete (multiple or binary) treatments. Combines estimation based on (doubly robust) efficient score functions with double machine learning to control for confounders in a data-driven way.

Usage

```
treatDML(
  y,
  d,
  x,
  s = NULL,
  dtreat = 1,
  dcontrol = 0,
  trim = 0.01,
  MLmethod = "lasso",
  k = 3,
  normalized = TRUE
)
```

Arguments

y	Dependent variable, must not contain missings.
d	Treatment variable, must be discrete, must not contain missings.
x	Covariates, must not contain missings.
s	Indicator function for defining a subpopulation for whom the treatment effect is estimated as a function of the subpopulation's distribution of x. Default is NULL (estimation of the average treatment effect in the total population).
dtreat	Value of the treatment in the treatment group. Default is 1.
dcontrol	Value of the treatment in the control group. Default is 0.
trim	Trimming rule for discarding observations with treatment propensity scores that are smaller than trim or larger than 1-trim (to avoid too small denominators in weighting by the inverse of the propensity scores). Default is 0.01.
MLmethod	Machine learning method for estimating the nuisance parameters based on the SuperLearner package. Must be either "lasso" (default) for lasso estimation, "randomforest" for random forests, "xgboost" for xg boosting, "svm" for support vector machines, "ensemble" for using an ensemble algorithm based on all previously mentioned machine learners, or "parametric" for linear or logit regression.
k	Number of folds in k-fold cross-fitting. Default is 3.

normalized   If set to TRUE, then the inverse probability-based weights are normalized such
                  that they add up to 1 within treatment groups. Default is TRUE.

Details

Estimation of the causal effects of binary or multiple discrete treatments under conditional indepen-
dence, assuming that confounders jointly affecting the treatment and the outcome can be controlled
for by observed covariates. Estimation is based on the (doubly robust) efficient score functions
for potential outcomes in combination with double machine learning with cross-fitting, see Cher-
nozhukov et al (2018). To this end, one part of the data is used for estimating the model parameters
of the treatment and outcome equations based machine learning. The other part of the data is used
for predicting the efficient score functions. The roles of the data parts are swapped (using k-fold
cross-fitting) and the average treatment effect is estimated based on averaging the predicted efficient
score functions in the total sample. Standard errors are based on asymptotic approximations using
the estimated variance of the (estimated) efficient score functions.

Value

A treatDML object contains eight components, effect, se, pval, ntrimmed, meantreat, meancontrol,
pstreat, and pscontrol:

effect: estimate of the average treatment effect.

se: standard error of the effect.

pval: p-value of the effect estimate.

ntrimmed: number of discarded (trimmed) observations due to extreme propensity scores.

meantreat: Estimate of the mean potential outcome under treatment.

meancontrol: Estimate of the mean potential outcome under control.

pstreat: P-score estimates for treatment in treatment group.

pscontrol: P-score estimates for treatment in control group.

References

Chernozhukov, V., Chetverikov, D., Demirer, M., Duflo, E., Hansen, C., Newey, W., Robins, J.
(2018): "Double/debiased machine learning for treatment and structural parameters", The Econo-
metrics Journal, 21, C1-C68.

van der Laan, M., Polley, E., Hubbard, A. (2007): "Super Learner", Statistical Applications in
Genetics and Molecular Biology, 6.

Examples

```
# A little example with simulated data (2000 observations)
## Not run:
n=2000                        # sample size
p=100                         # number of covariates
s=2                           # number of covariates that are confounders
x=matrix(rnorm(n*p),ncol=p)   # covariate matrix
beta=c(rep(0.25,s), rep(0,p-s))  # coefficients determining degree of confounding
d=(x%*%beta+rnorm(n)>0)*1      # treatment equation
```

```
y=x%*%beta+0.5*d+rnorm(n)        # outcome equation
# The true ATE is equal to 0.5
output=treatDML(y,d,x)
cat("ATE: ",round(c(output$effect),3),", standard error: ",
    round(c(output$se),3), ", p-value: ",round(c(output$pval),3))
output$ntrimmed
## End(Not run)
```

---

treatselDML	*Binary or multiple treatment effect evaluation with double machine learning under sample selection/outcome attrition*

Description

Average treatment effect (ATE) estimation for assessing the average effects of discrete (multiple or binary) treatments under sample selection/outcome attrition. Combines estimation based on Neyman-orthogonal score functions with double machine learning to control for confounders in a data-driven way.

Usage

```
treatselDML(
  y,
  d,
  x,
  s,
  z = NULL,
  selected = 0,
  dtreat = 1,
  dcontrol = 0,
  trim = 0.01,
  MLmethod = "lasso",
  k = 3,
  normalized = TRUE
)
```

Arguments

y	Dependent variable, may contain missings.
d	Treatment variable, must be discrete, must not contain missings.
x	Covariates, must not contain missings.
s	Selection indicator. Must be 1 if y is observed (non-missing) and 0 if y is not observed (missing).
z	Optional instrumental variable(s) for selection s. If NULL, outcome selection based on observables (x,d) - known as "missing at random" - is assumed. If z is defined, outcome selection based on unobservables - known as "non-ignorable missingness" - is assumed. Default is NULL.

selected   Must be 1 if ATE is to be estimated for the selected population without missing
                  outcomes. Must be 0 if the ATE is to be estimated for the total population.
                  Default is 0 (ATE for total population). This parameter is ignored if z is NULL
                  (under MAR, the ATE in the total population is estimated).

dtreat   Value of the treatment in the treatment group. Default is 1.

dcontrol   Value of the treatment in the control group. Default is 0.

trim   Trimming rule for discarding observations with (products of) propensity scores
                  that are smaller than trim (to avoid too small denominators in weighting by
                  the inverse of the propensity scores). If selected is 0 (ATE estimation for
                  the total population), observations with products of the treatment and selection
                  propensity scores that are smaller than trim are discarded. If selected is 1
                  (ATE estimation for the subpopulation with observed outcomes), observations
                  with treatment propensity scores smaller than trim are discarded. Default for
                  trim is 0.01.

MLmethod   Machine learning method for estimating the nuisance parameters based on the
                  SuperLearner package. Must be either "lasso" (default) for lasso estimation,
                  "randomforest" for random forests, "xgboost" for xg boosting, "svm" for
                  support vector machines, "ensemble" for using an ensemble algorithm based
                  on all previously mentioned machine learners, or "parametric" for linear or
                  logit regression.

k   Number of folds in k-fold cross-fitting. Default is 3.

normalized   If set to TRUE, then the inverse probability-based weights are normalized such
                  that they add up to 1 within treatment groups. Default is TRUE.

Details

Estimation of the causal effects of binary or multiple discrete treatments under conditional independence, assuming that confounders jointly affecting the treatment and the outcome can be controlled for by observed covariates, and sample selection/outcome attrition. The latter might either be related to observables, which implies a missing at random assumption, or in addition also to unobservables, if an instrument for sample selection is available. Estimation is based on Neyman-orthogonal score functions for potential outcomes in combination with double machine learning with cross-fitting, see Chernozhukov et al (2018). To this end, one part of the data is used for estimating the model parameters of the treatment and outcome equations based machine learning. The other part of the data is used for predicting the efficient score functions. The roles of the data parts are swapped (using k-fold cross-fitting) and the average treatment effect is estimated based on averaging the predicted efficient score functions in the total sample. Standard errors are based on asymptotic approximations using the estimated variance of the (estimated) efficient score functions.

Value

A treatDML object contains eight components, effect, se, pval, ntrimmed, meantreat, meancontrol, pstreat, and pscontrol:

effect: estimate of the average treatment effect.

se: standard error of the effect.

pval: p-value of the effect estimate.

ntrimmed: number of discarded (trimmed) observations due to extreme propensity scores.

meantreat: Estimate of the mean potential outcome under treatment.

meancontrol: Estimate of the mean potential outcome under control.

pstreat: P-score estimates for treatment in treatment group.

pscontrol: P-score estimates for treatment in control group.

References

Bia, M., Huber, M., Laffers, L. (2020): "Double machine learning for sample selection models", working paper, University of Fribourg.

Chernozhukov, V., Chetverikov, D., Demirer, M., Duflo, E., Hansen, C., Newey, W., Robins, J. (2018): "Double/debiased machine learning for treatment and structural parameters", The Econometrics Journal, 21, C1-C68.

van der Laan, M., Polley, E., Hubbard, A. (2007): "Super Learner", Statistical Applications in Genetics and Molecular Biology, 6.

Examples

```
# A little example with simulated data (2000 observations)
## Not run:
n=2000                              # sample size
p=100                               # number of covariates
s=2                                 # number of covariates that are confounders
sigma=matrix(c(1,0.5,0.5,1),2,2)
e=(2*rmvnorm(n,rep(0,2),sigma))
x=matrix(rnorm(n*p),ncol=p)         # covariate matrix
beta=c(rep(0.25,s), rep(0,p-s))     # coefficients determining degree of confounding
d=(x%*%beta+rnorm(n)>0)*1           # treatment equation
z=rnorm(n)
s=(x%*%beta+0.25*d+z+e[,1]>0)*1     # selection equation
y=x%*%beta+0.5*d+e[,2]              # outcome equation
 y[s==0]=0
# The true ATE is equal to 0.5
output=treatselDML(y,d,x,s,z)
cat("ATE: ",round(c(output$effect),3),", standard error: ",
    round(c(output$se),3), ", p-value: ",round(c(output$pval),3))
output$ntrimmed
## End(Not run)
```

---

treatweight	*Treatment evaluation based on inverse probability weighting with optional sample selection correction.*

Description

Treatment evaluation based on inverse probability weighting with optional sample selection correction.

Usage

```
treatweight(
  y,
  d,
  x,
  s = NULL,
  z = NULL,
  selpop = FALSE,
  ATET = FALSE,
  trim = 0.05,
  logit = FALSE,
  boot = 1999,
  cluster = NULL
)
```

Arguments

y	Dependent variable.
d	Treatment, must be binary (either 1 or 0), must not contain missings.
x	Confounders of the treatment and outcome, must not contain missings.
s	Selection indicator. Must be one if y is observed (non-missing) and zero if y is not observed (missing). Default is NULL, implying that y does not contain any missings.
z	Optional instrumental variable(s) for selection s. If NULL, outcome selection based on observables (x,d) - known as "missing at random" - is assumed. If z is defined, outcome selection based on unobservables - known as "non-ignorable missingness" - is assumed. Default is NULL. If s is NULL, z is ignored.
selpop	Only to be used if both s and z are defined. If TRUE, the effect is estimated for the selected subpopulation with s=1 only. If FALSE, the effect is estimated for the total population. (note that this relies on somewhat stronger statistical assumptions). Default is FALSE. If s or z is NULL, selpop is ignored.
ATET	If FALSE, the average treatment effect (ATE) is estimated. If TRUE, the average treatment effect on the treated (ATET) is estimated. Default is FALSE.
trim	Trimming rule for discarding observations with extreme propensity scores. If ATET=FALSE, observations with $Pr(D=1|X)<$trim or $Pr(D=1|X)>(1$-trim$)$ are dropped. If ATET=TRUE, observations with $Pr(D=1|X)>(1$-trim$)$ are dropped. If s is defined and z is NULL, observations with extremely low selection propensity scores, $Pr(S=1|D,X)<$trim, are discarded, too. If s and z are defined, the treatment propensity scores to be trimmed change to $Pr(D=1|X,Pr(S=1|D,X,Z))$. If in addition selpop is FALSE, observation with $Pr(S=1|D,X,Z)<$trim are discarded, too. Default for trim is 0.05.
logit	If FALSE, probit regression is used for propensity score estimation. If TRUE, logit regression is used. Default is FALSE.
boot	Number of bootstrap replications for estimating standard errors. Default is 1999.

cluster   A cluster ID for block or cluster bootstrapping when units are clustered rather
                     than iid. Must be numerical. Default is NULL (standard bootstrap without
                     clustering).

Details

Estimation of treatment effects of a binary treatment under a selection on observables assumption
assuming that all confounders of the treatment and the outcome are observed. Units are weighted
by the inverse of their conditional treatment propensities given the observed confounders, which are
estimated by probit or logit regression. Standard errors are obtained by bootstrapping the effect. If
s is defined, the procedure allows correcting for sample selection due to missing outcomes based on
the inverse of the conditional selection probability. The latter might either be related to observables,
which implies a missing at random assumption, or in addition also to unobservables, if an instrument
for sample selection is available. See Huber (2012, 2014) for further details.

Value

A treatweight object contains six components: effect, se, pval, y1, y0, and ntrimmed.

effect: average treatment effect (ATE) if ATET=FALSE or the average treatment effect on the treated
(ATET) if ATET=TRUE.

se: bootstrap-based standard error of the effect.

pval: p-value of the effect.

y1: mean potential outcome under treatment.

y0: mean potential outcome under control.

ntrimmed: number of discarded (trimmed) observations due to extreme propensity score values.

References

Horvitz, D. G., and Thompson, D. J. (1952): "A generalization of sampling without replacement
from a finite universe", Journal of the American Statistical Association, 47, 663–685.

Huber, M. (2012): "Identification of average treatment effects in social experiments under alterna-
tive forms of attrition", Journal of Educational and Behavioral Statistics, 37, 443-474.

Huber, M. (2014): "Treatment evaluation in the presence of sample selection", Econometric Re-
views, 33, 869-905.

Examples

```
# A little example with simulated data (10000 observations)
## Not run:
n=10000
x=rnorm(n); d=(0.25*x+rnorm(n)>0)*1
y=0.5*d+0.25*x+rnorm(n)
# The true ATE is equal to 0.5
output=treatweight(y=y,d=d,x=x,trim=0.05,ATET=FALSE,logit=TRUE,boot=19)
cat("ATE: ",round(c(output$effect),3),", standard error: ",
    round(c(output$se),3), ", p-value: ",round(c(output$pval),3))
output$ntrimmed
## End(Not run)
```

```
# An example with non-random outcome selection and an instrument for selection
## Not run:
n=10000
sigma=matrix(c(1,0.6,0.6,1),2,2)
e=(2*rmvnorm(n,rep(0,2),sigma))
x=rnorm(n)
d=(0.5*x+rnorm(n)>0)*1
z=rnorm(n)
s=(0.25*x+0.25*d+0.5*z+e[,1]>0)*1
y=d+x+e[,2]; y[s==0]=0
# The true ATE is equal to 1
output=treatweight(y=y,d=d,x=x,s=s,z=z,selpop=FALSE,trim=0.05,ATET=FALSE,
        logit=TRUE,boot=19)
cat("ATE: ",round(c(output$effect),3),", standard error: ",
    round(c(output$se),3), ", p-value: ",round(c(output$pval),3))
output$ntrimmed
## End(Not run)
```

---

ubduration   *Austrian unemployment duration data*

Description

A dataset containing unemployed females between 46 and 53 years old living in an Austrian region where an extension of the maximum duration of unemployment benefits (from 30 to 209 weeks under particular conditions) for job seekers aged 50 or older was introduced.

Usage

```
ubduration
```

Format

A data frame with 5659 rows and 10 variables:

y Outcome variable: unemployment duration of the jobseeker in weeks (registered at the unemployment office). Variable is numeric.

z Running variable: distance to the age threshold of 50 (implying an extended duration of unemployment benefits), measured in months divided by 12. Variable is numeric.

marrstatus Marital status: 0=other, 1=married, 2=single. Variable is a factor.

education Eductation: 0=low education, 1=medium education, 2=high education. Variable is ordered.

foreign Migrant status: 1=foreigner, 0=Austrian. Variable is a factor.

rr Replacement rate (of previous earnings by unemployment benefits). Variable is numeric.

lwagejob Log wage in last job. Variable is numeric.

experience Ratio of actual to potential work experience. Variable is numeric.

whitecollar 1=white collar worker, 0=blue collar worker. Variable is a factor.

industry Industry: 0=other, 1=agriculture, 2=utilities, 3=food, 4=textiles, 5=wood, 6=machines, 7=other manufacturing, 8=construction, 9=tourism, 10=traffic, 11=services. Variable is a factor.

References

Lalive, R. (2008): "How Do Extended Benefits Affect Unemployment Duration? A Regression Discontinuity Approach", Journal of Econometrics, 142, 785–806.

Frölich, M. and Huber, M. (2019): "Including covariates in the regression discontinuity design", Journal of Business & Economic Statistics, 37, 736-748.

Examples

```
## Not run:
# load unemployment duration data
data(ubduration)
# run sharp RDD conditional on covariates with user-defined bandwidths
output=RDDcovar(y=ubduration[,1],z=ubduration[,2],x=ubduration[,c(-1,-2)],
 bw0=c(0.17, 1, 0.01, 0.05, 0.54, 70000, 0.12, 0.91, 100000),
 bw1=c(0.59, 0.65, 0.30, 0.06, 0.81, 0.04, 0.12, 0.76, 1.03),bwz=0.2,boot=19)
cat("RDD effect estimate: ",round(c(output$effect),3),", standard error: ",
 round(c(output$se),3), ", p-value: ", round(c(output$pvalue),3))
## End(Not run)
```

---

wexpect	*Wage expectations of students in Switzerland*

Description

A dataset containing information on wage expectations of 804 students at the University of Fribourg and the University of Applied Sciences in Bern in the year 2017.

Usage

```
wexpect
```

Format

A data frame with 804 rows and 39 variables:

wexpect1 wage expectations after finishing studies: 0=less than 3500 CHF gross per month; 1=3500-4000 CHF; 2=4000-4500 CHF;...; 15=10500-11000 CHF; 16=more than 11000 CHF

wexpect2 wage expectations 3 years after studying: 0=less than 3500 CHF gross per month; 1=3500-4000 CHF; 2=4000-4500 CHF;...; 15=10500-11000 CHF; 16=more than 11000 CHF

wexpect1othersex expected wage of other sex after finishing studies in percent of own expected wage

wexpect2othersex expected wage of other sex 3 years after studying in percent of own expected wage

male 1=male; 0=female

business 1=BA in business

econ 1=BA in economics

communi 1=BA in communication

businform 1=BA in business informatics

plansfull 1=plans working fulltime after studies

planseduc 1=plans obtaining further education (e.g. MA) after studies

sectorcons 1=planned sector: construction

sectortradesales 1=planned sector: trade and sales

sectortransware 1=planned sector: transport and warehousing

sectorhosprest 1=planned sector: hospitality and restaurant

sectorinfocom 1=planned sector: information and communication

sectorfininsur 1=planned sector: finance and insurance

sectorconsult 1=planned sector: consulting

sectoreduscience 1=planned sector: education and science

sectorhealthsocial 1=planned sector: health and social services

typegenstratman 1=planned job type: general or strategic management

typemarketing 1=planned job type: marketing

typecontrol 1=planned job type: controlling

typefinance 1=planned job type: finance

typesales 1=planned job type: sales

typetechengin 1=planned job type: technical/engineering

typehumanres 1=planned job type: human resources

posmanager 1=planned position: manager

age age in years

swiss 1=Swiss nationality

hassiblings 1=has one or more siblings

motherhighedu 1=mother has higher education

fatherhighedu 1=father has higher education

motherworkedfull 1=mother worked fulltime at respondent's age 4-6

motherworkedpart 1=mother worked parttime at respondent's age 4-6

matwellbeing self-assessed material wellbeing compared to average Swiss: 1=much worse; 2=worse; 3=as average Swiss; 4=better; 5=much better

homeowner 1=home ownership

treatmentinformation 1=if information on median wages in Switzerland was provided (randomized treatment)

treatmentorder 1=if order of questions on professional plans and personal information in survey has been reversed (randomized treatment), meaning that personal questions are asked first and professional ones later

References

Fernandes, A., Huber, M., and Vaccaro, G. (2020): "Gender Differences in Wage Expectations", arXiv preprint arXiv:2003.11496.

Examples

```
data(wexpect)
attach(wexpect)
# effect of randomized wage information (treatment) on wage expectations 3 years after
# studying (outcome)
treatweight(y=wexpect2,d=treatmentinformation,x=cbind(male,business,econ,communi,
businform,age,swiss,motherhighedu,fatherhighedu),boot=199)
# direct effect of gender (treatment) and indirect effect through choice of field of
# studies (mediator) on wage expectations (outcome)
medweight(y=wexpect2,d=male,m=cbind(business,econ,communi,businform),
x=cbind(treatmentinformation,age,swiss,motherhighedu,fatherhighedu),boot=199)
```

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